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(54) Title: RAPID METHOD OF ANALYSIS FOR CORRELATION OF ASSET RETURN TO FUTURE FINANCIAL LI-**ABILITIES** 

PREPARE INDUT: CREATE FILES WHICH CONTAIN RETURN DEFORMATION ON THE SECURITIES TO BE USED, THE TARGET RETURNS, SECURITY IDENTIFIERS, CURRENT PRICE, MARKET CAPITALIZATION AND CURRENT PORTFOLIO WEIGHTS. "ESTABLISH STATISTICAL PROPERTIES OF LIABILITIES."

SET UP PROBLEM: SPECIFY NUMBER AND TYPE OF SECURITIES, THE PERIOD, RUNGER OF RETURNS USED TO CALCILATE COVARIANCE AND TO ACCULATE AVERAGES, DISTANCE TO MOYE OF AND DOWN COVARIANCE BULLET SCALING FACTOR FOR TARGET, AND FACTOR FOR CONTROLLING TURNOVER.

READ IN NECESSARY INFORMATION SECURITY NAMES. IDENTIFIERS, INDUSTRY CODES, PRICES, MARKET CAPITALIZATION, WEIGHT IN CURRENT PORTFOLIO, PERIOD RETURNS; TARGET NAMES, TARGET PERIOD RETURNS.

CALCULATE SPAINTING COVARIANCE ARRAY: DEFINED AS THE ARTANCE OF SECURITY RETURN LESS TARGET RETURN WITH ALL OTHER SECURITIES RETURNS LESS TARGET RETURNS IN SPECIFIED RETURN PERIOD.

CALCULATE AVERAGE RETURN FOR EACH SECURITY.

SET UP CONSTRAINTS ON SECURITY TYPE SECTOR TYPE, INDIVIDUAL SECURITY WEIGHTS.

FORMAT PROBLEM IN STANDARD FORM FOR SOLUTION BY GENERALIZED QUADRATIC PROGRAMMING TECHNIQUE.

SOLVE FOR OPTIMUM OF PROBLEM WITH QUADRATIC PROGRAMMING SOLUTION ALGORITHM. CHECK SOLUTION FOR FEASIBILITY.

CALCULATE STATISTICS: COVARIANCE OF PORTFOLIO, ALPHA, BETA, AND STAMDADD ERROR WITH TARRET IN SIMULATION PERIOD, PORTFOLIO RETURNS ON RETURN PERIOD, PORTFOLIO RETURNS IN SIZULATION PERIOD, TURNOVER, SECTOR WEIGHTS, AND SECURITY TYPE WEIGHTS.

PRINT OUTPUT FILE: SECURITY WEIGHTS, SENSITIVITIES, IDENTIFIERS, AND MANES: STATISTICS, INPUT PARAMETERS, SORTED BUYS AND SELLS, AND SECTOR WEIGHTS.

(57) A hotroot

A method and system for correlating an expected asset return of a portfolio to changes in future financial liabilities and also to other financial indices. Management of asset portfolios often requires precise matching of liability streams, such as is the insurance industry and for pension funds. The method selects the weight percentages of assets by achieving optimum statistical correlation between asset returns and liability returns.

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RAPID METHOD OF ANALYSIS FOR CORRELATION OF ASSET RETURN TO FUTURE FINANCIAL LIABILITIES

The present invention is related generally interpretation.

and system for selecting a portfolio of assets for achieving optimum correlation of asset return to a selected standard financial index. More particularly, the invention is related to a highly efficient, rapid method and system for choosing an asset portfolio having the optimum correlation of the asset return to a time dependent financial index, such as a financial liability, at each of a number of selectable asset return levels.

Management of portfolios of assets has historically emphasized maximizing the return on assets with the objective of at least outperforming the market. However, in some financial industries the objective, or the figure of merit, is also related to meeting future liabilities rather than just achieving high return on assets. Frequently, an institution will have a future intended use of the assets which requires their availability at some future time. If assets are performing differently than liability requirements, substantial financial hardship can result. For example, insurance companies and corporate pension plans have well defined future financial liabilities which must be met. Consequently, although return on assets is one important objective, meeting future liabilities is also important and can be even more

important in many instances. In fact, many pension plan managers are now required to meet the standards set forth in FASB Statement 87 (Financial Accounting Standards Board) on pension fund accounting. Under the FASB Statement a market interest rate return on pension funds is the standard index and is to be based on A-rated ten year corporate bonds. Under this FASB Statement any deficit in corporate pension funds are now reflected on the balance sheet. Any such deficit would therefore have substantial adverse effect on the apparent net worth of the subject corporation. Consequently, this FASB Statement standard strongly encourages maintenance of a surplus for a pension fund. As an example of the importance of matching the liability requirements under the FASB Statement, consider the percentage change possible for pension plan liabilities, as measured by the accumulated benefit obligation (ABO). If, for example, interest rates increase by 1% in one year over the present rates, the present value of the ABO would decline by 10% if the ABO has a duration of 10 years. Likewise, if interest rates were to drop by 1% in one year, the present value of the ABO would increase by 10%. The potential for such dramatic fluctuations in liabilities clearly deserves careful attention by parties obligated to meet future liability streams.

In order to timely meet future financial liabilities and maintain a proper surplus fund for a pension plan, a number

of methodologies have arisen including "immunization", "cash matching"; and some preliminary efforts have even been directed to utilizing stock funds.

The "immunization" method of meeting future financial liabilities uses bonds having substantially the same duration as the liability stream. Duration is a measure of volatility expressed in years, which is similar to, but more precise than, average life. The duration is calculated as the weighted average amount of time to the receipt of the payout. There are however significant drawbacks to "immunization", with one primary disadvantage being the relatively low excess return on assets generally achieved by the method. Additional limitations are imposed by the two major assumptions made by the strategy: The yield curve (a plot of yield to maturity on bonds versus their time to maturity) will only make parallel shifts. Consequently, regardless of maturity, when market conditions change, all bonds allegedly move exactly the same amount in yield. This clearly is not the case since there have been substantial inconsistencies in the past for the difference in rates for short-term bonds and long-term bonds. Secondly, all cash flows in excess of required annual payments can allegedly be reinvested at the yield to maturity of the portfolio. This presumption is also clearly not true since sharply declining or rising interest rate environments will make it extremely difficult to carry out reinvestment.

Furthermore, this strategy does require more ongoing management of the portfolio in order to sell or buy more securities to match the actuarial schedule and maintain a proper asset/liability match.

The "cash matching" method utilizes a bond portfolio having numerous component bonds with various maturity dates and payout rates to precisely match the liability requirements of the pension plan. Such an approach has the same primary disadvantage as the "immunization" method and further requires additional effort to assemble the portfolio. Frequently, the "cash matching" method demands payment of a premium to achieve the correct mix of bond rates and maturity. Both of the first strategies ("immunization" and "cash matching") must invest in fixed income securities to provide the assurance of receiving the necessary cash flows. In fact, they must primarily invest in U.S. treasury obligations since investments in corporate or mortgage securities increase the chance for default or for call risks which can have the effect of changing the projected cash flow.

Pension plan liabilities or other future liabilities, such as are present in the insurance industry, are long term in nature. Therefore, a future liability stream can greatly benefit from the compounding effect of investment in higher returning assets, such as common stocks. However, attempts to characterize stocks in terms of a time duration parameter or

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otherwise have not been successful. In the last few years many unsuccessful attempts have been made to develop a system whereby a portfolio of equities is linearly optimized relative to a liability stream. There have been attempts to parallel the "cash matching" techniques with the use of stocks, instead of bonds. This approach has involved matching the expected dividend flow of the portfolio to the liability stream.

Unfortunately, stock dividend yields are unpredictable, particularly beyond 3 years in the future. Another major effort in equities has been directed to an "immunization" type treatment. In this effort an attempt was made to calculate the duration of stocks on an individual basis, as well as on a portfolio basis; but these attempts also have been unsuccessful, primarily due to the long term unpredictability of stock dividends.

In a related patent application, incorporated by reference herein and having serial number 281,560 and filed December 8, 1988, an improved method and system were set forth directed to correlating return on assets to a financial objective over time. In performing the analysis to determine the optimum assets of a portfolio to track the financial objective, the machine time and efficiency of the evaluation process can limit the number of assets considered in constructing the portfolio. Such limitations on the number of assets which are considered for inclusion in the optimum

portfolio can also limit the performance of the selected portfolio.

It is therefore an object of the invention to provide an improved method and system for determining the optimum portfolio of assets for tracking a financial index.

It is another object of the invention to provide a new method and system of efficiently selecting the optimum portfolio of assets for tracking a financial index.

It is an additional object of the invention to provide an improved method and system of rapidly analyzing a large number of potential assets to select the optimum portfolio of assets to track a financial index.

It is a further object to provide a new method and system of enlarging the number of potential assets under consideration for inclusion in a portfolio of assets, while reducing the time required to select the portfolio of assets which best track the behavior of a financial index.

It is another object of the invention to provide a rapid, more efficient method and system of selecting the weighted values for assets selected from a universe of possible assets for a portfolio designed to track a financial index.

It is an additional object of the invention to provide an improved method and system for reinvesting cash flow from a portfolio starting with that current portfolio of assets.

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Further objects and advantages of the present invention, together with the organization and manner of operation thereof, will become apparent from the following description when taken in conjunction with the accompanying drawings described hereinbelow.

### BRIEF DESCRIPTION OF THE DRAWINGS

FIGURE 1A is a functional flow chart illustrating operation of one method of portfolio construction and FIG. 1B is a flow chart illustrating operation of a particular method of the invention;

FIGURE 2A illustrates simulation results of annual total liability returns of a pension plan (dashed) and annual total asset returns (solid line) for a preferred form of the invention and FIG. 2B shows annual total liability returns of the simulated pension plan (dashed) and annual total asset returns (solid line) for the Standard & Poors 500;

FIGURE 3A is a bar graph of simulation results for funded status returns over time for a preferred method of the invention and FIGURE 3B is a bar graph of funded status returns over time for the Standard & Poors 500;

FIGURE 4 a comparative plot of cumulative funding status for simulation results over time for a pension plan liabilities (dashed), a portfolio derived by a preferred method of the invention (solid line) and the Standard & Poors 500 index (dashed and dotted):

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FIGURE 5A shows the correlation between asset return and liability return for a preferred method of the invention and FIG. 5B illustrates correlation between asset return and liability return for the Standard & Poors 500 index; and

FIGURE 6 illustrates the boundary line of minimum risk for various future asset return levels.

### DETAILED DESCRIPTION OF PREFERRED EMBODIMENTS

Broadly stated, a method and system are described for selecting a portfolio of assets and correlating a future asset return of the portfolio to a financial index, such as, a liability index, an inflation index, or any other accepted index and mixtures thereof. Specific examples of indices are liability indices, such as, individual corporate pension plan liabilities and insurance company liabilities. The consumer price index and wage growth index are examples of an inflation index, and other indices can include accepted stock price indices and futures markets indices. The method includes selecting asset portfolios which optimally correlate portfolio returns to the future desired payouts or payments needed over time to fulfill the desired financial objective. In the general case the user selects a standard index to which optimum correlation is desired for the selected portfolio having a future asset return over time. The process of selecting the

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standard index can involve obtaining input (such as actuarial) in terms of the characteristics of future cash payments discounted to present value based on a range of discount rate and wage (inflation) values. This information can be used to construct a functional behavior for the present value of the liability. A decision is then made, such as by a company pension fund manager, that certain discount rates and inflation assumptions should be made. On this basis the current liabilities are projected back in time using these assumptions and a plurality of assets are examined to determine their sensitivity to the past behavior of the liability returns. the most general sense if one can determine an index to which a portfolio of assets has a strong correlation, this sensitivity can be used to select a set of assets which will match the behavior of the index as it changes over time. As a particular example an actuary can provide specific ranges of present value liability for a range of discount rates and inflation rates. The change over time of the liability from month to month over a twenty four month period can yield a liability return. The analysis to be described in more detail hereinafter determines which selected ones of a plurality of assets track the liability returns with best correlation. The resulting weighted set of assets form the portfolio to follow the future liability returns. An analysis using the selected standard index can be performed on a plurality of assets, such as, for

example, at least one of the following categories of assets: stock securities, real estate investments, futures contracts, options, commodities, currencies and precious metals. The analysis allows the identification of the combination of weight percentages of selected ones of the plurality of assets yielding the optimum correlation of the future asset return to the standard index. Optimum correlation is thus achieved by calculating a minimum standard deviation or a variance for the difference between the return of the portfolio of assets and the selected standard index return. This method and system are particularly applicable for, but not limited to, the insurance industry and management of pension fund liabilities.

the procedures followed in carrying out two forms of the invention. In the first method shown in FIG. 1A (and described previously in pending application having serial number 281,560) the correlation of the expected asset return of a portfolio to a standard index one is initiated by input of various basic information. This information includes, for example, establishing the fundamental statistical characteristics of liability returns, and future payment schedules for matching a desired index, such as the future stream of financial liabilities of a pension plan. As described hereinbefore, the future payment schedule for a pension plan can be determined by using actuarial data. These future liabilities can be

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characterized in terms of an accumulated benefit obligation (ABO), that is, the price you would have to pay if the liabilities were sold at a selected time. The total outlay required to pay retirement wages for the pension plan are discounted back to the present value at the market rate interest (currently 10%). Other related characterizations can be used, such as a projected benefit obligation (PBO), by accounting for inflation in the growth of wages at retirement. This amount is converted to a percentage and an expected salary at retirement, discounted to present value. Therefore, although the ABO is affected primarily by interest rates, additional standard measures, such as the PBO, account for inflation. Therefore, the method is also generally effective for calculating the convolution of complex effects with one another. The method only requires optimizing correlation of the time behavioral performance of future asset return relative to the particular standard index, which includes any conceivable selected characteristic which assets are found to be sensitive to.

In the manner illustrated in step 1 of FIG. 1A, various input files are therefore created to begin the analysis. These input files can include, for example, asset return information for the universe or plurality of assets to be sampled in the analysis. Also established as data files are the data representative of the standard asset return over time,

such as target returns for a future liability stream of a pension plan or an insurance company. The future liability stream can depend on interest rates and/or inflation rates and other variables which can affect the liability stream. For example, as described hereinbefore, a surface can be generated which describes the behavior of liability return as a function of both interest rates and inflation rates. Other information in the data files can be identification information for the plurality of assets, current price and market capitalization of the assets, as well as the characteristic weight percentages of assets in a previously selected portfolio. Weight percentages, for example, from a prior period would be used in the most preferred embodiment.

As illustrated in the second box of FIG. 1A, the number and type of the plurality of assets should be specified, the time period for matching the standard, the number of returns used to calculate a statistical correlation and the number of asset returns used to calculate averages for the plurality of securities to be analyzed to select the optimum set of weighted assets.

The method in FIG. lA then initializes information preparatory to analyzing the plurality of assets, such as, establishing names of securities, associated identifier information, industry codes, prices of securities, market capitalization, weight and percent of the previously calculated

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prior portfolio, the period for the asset return, the name of the target or standard for measuring a standard asset return and the time period for the standard returns.

In the next box in FIG. 1A the correlation between the future asset return and the standard index is optimized by first generating a covariance array. While other nonlinear statistical analyses are possible, this method being described is a preferred method of carrying out the analysis. For example, another useful statistical method of analysis is correlation parameterization which is embodied in the computer software program Appendix III. As shown in the next step in FIG. 1A, the average return of each security is calculated followed by imposing certain constraints on the calculation, such as setting a range of weight percentages to be tried. The calculation is then implemented to a solution by a standard computer program quadratic technique (see Appendix I). This step is then followed by determination of various statistical parameters, such as X and B, standard error, portfolio returns over various time periods and for selected weights. The analysis is then completed by printing output (see attachment to Appendix I) such as asset weights, sensitivity factors for selected assets of the portfolio, statistical parameters, sorted buy and sell orders and sector weights.

A simple example of utilizing the preferred statistical method is illustrated for a portfolio containing

three stocks (designated 1, 2, and 3). In order to find the optimum weight percent for each of the three stocks in the portfolio, the minimum standard deviation (square root of variance) is calculated for the differences between the assets of the portfolio and the future liabilities as represented by the standard asset return over time. The risk is therefore defined as the standard deviation of differences:

Risk = 
$$[X \mid R_{pi} \mid R_{T} \mid 1) - n \mid R_{p} \mid R_{t}]^{1/2} = \sigma[R_{p} - R_{t}] = variance^{1/2}$$

where:  $R_{pi}$  = total return on the portfolio during period i;  $R_{ri}$  = total return on target or standard in period i,

= standard deviation;

 $R_p$  = average return on portfolio, i = 1,n; and  $R_T$  = average return on target or standard portfolio of assets,

i = 1, ..., n...

The portfolio return equals percentage weight for each stock times the return on that stock:

$$R_{pi} = \sum_{j=1}^{3} x_j R_{sj, i}$$

x<sub>j</sub> = the weight in the portfolio of the stock j

R<sub>sj,i</sub> - the return on stock j in periods i

Now in the definition of risk, as set forth above, we can substitute the following:

$$R_{pi} = \sum_{j=1}^{3} x_j R_{sj, i}$$

Making this substitution, a determination of risk in the manner set forth above results in the calculation of the covariance of the stock with each of the other stocks in the portfolio after subtracting the return of the target, or standard index, from the future asset return of each stock.

The covariance of stock 1 with stock 2 is therefore:

$$(R_1, R_2) = \sum_{s=1}^{n} (R_{s1i} - R_{Ti}) (R_{s2i} - R_{Ti}) - n (R_1 - R_T) (R_2 - R_T)$$

We calculate all the spanning covariances and put them in a matrix form:

Cov 
$$[(R_1 - R_T), (R_1 - R_T)]$$
 Cov  $[(R_1 - R_T), (R_s - R_T)]$ 

Cov  $[(R_3 - R_T), (R_1 - R_T)]$  Cov  $[(R_3 - R_T), (R_3 - R_T)]$ 

In order to calculate the risk, we add up all the Cov terms times the weights in each stock:

Risk = 
$$\mathbb{C}(R_p - R_T) = \left\{ \left[ \sum_{i=1}^{3} \sum_{j=1}^{3} X_i X_j \text{Cov} \left[ (R_i - R_T), (R_j - R_T) \right] \right\}^{1/2}$$

In order to minimize this "risk" function, we determine the combination of weight percentages for stocks 1 thru 3 which produces the smallest statistical risk. The above described risk can readily be calculated by various means, such

as, by a computer program (which is included in Appendix I). The output (see attachment to Appendix I) of the calculation includes the weight percent of each stock and the associated overall risk level. This calculation can be repeated for a range of expected asset return levels and results in generating a nonlinear type "bullet" shape defining the limits of minimum risk over a range of asset return levels for associated standard deviations of funding level (see FIG. 6). The method uses historical returns for the plurality of stocks analyzed in order to calculate the resulting covariance between the standard liability returns and the future returns of the potential portfolio of assets. Appendix II illustrates an example of a computer program for calculating typical liability return data. The method of analysis results in choosing a selected set of assets for the portfolio with a strong inclination of the selected set of assets to respond in a manner such as the standard asset returns over time, which alone can be valuable output. As mentioned hereinbefore, in other embodiments, the nonlinear analysis of a plurality of assets can involve other methods, such as, index correlation parametrization for matching the performance of a target index return (see Appendix III).

In one embodiment of the invention illustrated in FIG. 1B, the method is a simplification of the more formal procedure of FIG. 1A. The method of FIG. 1B accomplishes,

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however, the same result as in FIG. 1A but with much greater efficiency and speed.

The method of FIG. 1B is broken into eleven steps, and the first three steps are substantially the same as the method of FIG. 1A. The eleven steps and details of each each step are described below:

- numbers (thousands of securities) can be utilized in this procedure. An input file contains the returns for each security in the prior periods, such as the previous 24 months. Various data is included, such as, security name, industry groups code, market capitalization, trading volume, recent prices, specific identifiers and estimated bid/ask price spreads. The effect of transaction costs associated with the spread in the bid/ask price can be included in the performance analysis.
- II. Read in Returns of Target Index to Track. If a portfolio is to be constructed for tracking a specific financial target index, the returns to that target for the relevant period are read into memory arrays. Additional identifying information is also read in from the target data file.
- III. Set-up Constraints on Upper and Lower Bounds
  in Terms of Percent of Portfolio for each Security and each
  Sector or Industry. A maximum and minimum percentage weight of

the portfolio for each security can be specified to constrain the portfolio. This can be used to insure portfolio diversification and to control costs associated with trading. In addition, sectors of the universe, for example, utility stock, can be constrained by maximum and minimum boundaries. If one has a single target, one can "short" a stock and take a negative minimum position.

- IV. Calculate the Covariance of Each Security with the Target Index. If a target is used the covariance is calculated for each security and stored in an array. If no target index is used, a zero value for each security is stored in the array.
- V. Create an Initial Portfolio by Selecting

  Highest Covariance Securities and Weighting Them at their Upper

  Limits as Defined by Selected Constraints. This step creates

  an initial feasible solution to the problem by filling the

  vector of portfolio weights according to the constraints and in

  order of highest covariance.
- Initial Portfolio Weightings. The objective function can be defined in a number of ways. The computer program allows monthly or moving quarterly returns to be used for optimization. Transaction costs can be considered and their importance magnified or reduced relative to other objectives. With minor changes, other such goals can be incorporated into

the objective function. The key is that once the objective function is specified, partial derivatives can be used to guide the search for an optimal portfolio. Any example of a preference that can be created is an increased weighting for a stock with a likely dividend versus one with no dividend.

VII. Calculate Partial Derivatives for Each Security at Initial Portfolio Weightings. A partial derivative is calculated for each variable (in this case each security), and a direction can be determined in which to move the individual security weights in order to obtain an improved portfolio solution. The partial derivatives are also used to determine if the weights are optimal. In the prior art, the solution techniques require storage of a full covariance matrix array. This storage requirement has limited the practical number of securities which could be considered at one time in the past methodologies. Indeed, the storage requirements, and to a large degree the processing time, varies as the square of the number of securities in the portfolio under consideration. See the example discussed hereinafter in which the previous methodology is compared to the invention.

In addition, the methods of solution for these problems in the prior art were slow and cumbersome and subject to failure when the full covariance array was sensitive or a nonunique set of solutions were achievable. This current method requires much less storage, uses a rapid solution

technique and allows control of the tolerance used for optimality. Consequently, the improved methods will select a portfolio when several combinations are equally desirable.

Not only is the amount of necessary memory reduced and the computer calculational time greatly reduced, there is substantial flexibility in defining the objective, assurance of the solution is enhanced and simultaneous considerations of large number of securities allows substantial improvement in optimizing the expected return of the portfolio compared to the target index.

- Direction of Improvement is Indicated by Partial Derivatives.

  Adjustment of the portfolio weights is achieved by a search technique which moves along the constraints and changes in a proper direction of improvement of the objective function. The objective function is calculated at the new weights and a test of improvement is made.
- Defined by the Kuhn-Tucker Conditions. If the objective function is not improving or if the step size used to adjust the portfolio weights becomes extremely small, the search is terminated. This solution is normally a Kuhn-Tucker point (conventional method of establishing optimality conditions) or extremely close thereto within an acceptable epsilon to such a point.

X. Recycling Conditions. If the termination conditions are not satisfied then one re-calculates the objective function value, re-calculates the partial derivatives, makes changes in the portfolio weightings to achieve an improved solution and test for convergence.

The process is by nature iterative and continues cycling until a solution is reached in which diminishing returns are achieved by further cycling.

XI. <u>Output of Information</u>. Relevant portfolio information is output with security weightings, objective function values, purchases and sales necessary to achieve the optimum portfolio and industry weightings.

The detailed output is written into a computer file which then can be examined for relevant information. Order to buy and sell securities can be developed from the information in the output file.

Included in Appendix IV is an exemplary computer software (source output) program illustrating critical steps of the method of FIG. 1B. Table XI shows exemplary results for a program simulation wherein the target index is the Standard and Poors 500 stock index. Appendix VI illustrates significant distinctions from the optimizer methodology used in the copending patent application having serial number 281,560.

Quantifying Magnitude of Reduced Computation Time

A test was performed on an IBM compatible PC to

compare the solution speeds of two portfolio optimization systems. In a prior system, the problem of handling large numbers of securities in a portfolio selection process increased in proportion to the number of securities squared. Thus, a problem involving one hundred securities would take approximately one hundred times as many calculations to solve as a problem with ten securities.

In the current system the solution difficulty increases by a factor of less than one times the number of securities. In addition, the computing memory required to solve the problem is proportional to the number of securities rather than, as in the prior system, that number squared.

Solution Time Comparison

Hardware:

IMB compatible PC, 386-20Mhz CPU, 80387

co-processor

Problem Size: 100 securities

3% portfolio weight upper bound on each security

0% portfolio weight lower bound on each security

Time to solution:

Prior system - 9 minutes 34 seconds

Current system - 52 seconds

Overall speed-up: 11.0 x prior system

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This speed increase is actually of a larger magnitude since approximately 40% of the 52 seconds to solution with the current system is spent reading information from external files and writing information to other files. The solution time speed-up, allowing for reading and writing files, is approximately 17.3 x prior system. This speed-up ratio increases in proporation to the number of securities considered squared.

The speed increase and the reduced computer memory requirements by the current system allow large problems to be solved in a short time, requires limited computer memory, and uses computer hardware which is relatively inexpensive.

Circumstances arise regularly in the investment field which rapidly change the prospects for securities. The impact of these sudden changes must be incorporated into the security valuation system so that rational alternations in the investment portfolios may be made.

Examples of sudden changes include: a company is presented with a buy-out offer by another firm; a disaster occurs, such as an oil spill, which may impact a firm's stock price; monetary or fiscal policy changes are implemented by the government. It is important for an investment system to be flexible and fast enough to evaluate the impact these changes may have on a security portfolio.

The current system allows for estimates of partial monthly returns to be calculated on any day of the month, for these returns to be used in the optimization process, and for the results of the analysis to be completed within a few minutes.

One advantage of the current system is that analysis of the current investment opportunities can be completed rapidly and recommendations for buying and selling securities can be quickly generated. This allows investment decisions to be made and implemented quickly with confidence.

Further illustrations of the invention are exemplified by various historical simulations shown in FIGS. 2-4 and Tables I-III which are taken over the time period of 1975 to 1987. As listed in Table I and in FIGS. 2 and 3, the liability stream for a selected pension plan can undergo substantial variation with time. A portfolio of assets has been analyzed in accordance with the preferred statistical method described hereinbefore, and details of the selected portfolio are set forth in Tables IV-X. Over the 1975-1987 time period, the resulting portfolio of assets shows substantially better correlation to the liability stream as compared to the Standard & Poors 500 return. Moreover, as seen in Table II and FIG. 4, the overall cumulative return for the portfolio of assets selected by the preferred method is far better than the Standard & Poors 500. The greatly enhanced stability and good

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Year	Total Spanning Return (A)	Total S&P 500 Return (B)	Liability Return (C)	Spanning Funded Status Return (1+A)/(1+C)	Status Return (1+B)/(1+C)
1975	28.85%	37.36%	7.43%	19.94%	27.86%
1976	34.96	23.94	15.53	16.83	7.28
1977	-4.16	-7.29	1.16	-5.25	-8.35
1978	4.76	6.42	-0.27	5.05	6.71
1979	21.84	18.36	-0.56	22.52	19.03
1980	13.68	32.34	-2.64	16.76	35.92
1981	16.01	-4.95	2.23	13.49	-7.02
1982	32.60	21.49	39.64	-5.04	-13.00
1983	22.15	22.43	0.46	21.59	21.87
1984	6.86	6.18	14.97	-7.05	-7.65
1985	40.95	31.59	31.33	7.33	0.20
1986	30.04	18.64	26.07	3.15	-5.89
1987	0.87	5.28	-5.05	6.24	10.88

TABLE I

Funding Return Analysis

TABLE II

Spanning Technology

Historic Simulation

Cumulative Surplus Analysis

نو نو		Spanning Portfolio	ortfolio	 S&P 500 Index	Index
	•	Cumulative	Cumulative	Cumulative	Cumulative
	±*	Dollar	Funded	Value	Position
rear		\$100.00	100.00%	\$100.00	100.00%
1076		118.78	119.65	127.12	128.65
6761		149.36	140.49	147.26	130.52
1977		133,59	133.82	126.88	127.10
1078		130.14	141.83	125.03	136.25
1979		148.14	177.42	137.62	164.83
1980		157.98	216.50	170.79	234.06
1981		173.32	263.84	152.84	232.66
1982		218,19	267.96	173.99	213.68
1983		256.52	348.87	202.88	275.93
1984		263.48	350.40	205.10	272.76
1985		359,74	403.26	258.85	290.17
1986		457.65	438.20	297.13	284.50
1987		453.01	496.15	304.26	333.22

Note: The above cumulative values reflect monthly payments to beneficiaries.

13.68 16.01 32.60

1980 1982 1983 1984 1985 1986

52.15 6.86 40.95 30.04

TABLE III

Spanning Portfolio

Return

28.85x

1975 1976

34.96 -4.16 4.76 21.84

> 1978 1979

1977

Electric, Gas, and Sanitation Utilities and Banking Restricted to 10% of Portfolio.

# SPANNING PORTFOLIO COMPOSITION 1987 Portfolio

TABLE IV

# Industry

% of Portfolio

Wholesale Trade-Nondur. Goods **Mholesale Trade-Durable Goods** Meas. Anol. & Cont. Inst. Etc. Transportation By Air Electirc Gas And Sanit. Serv. Machinery Except Electrical Ele. and Ele. Mach. printing Publishing and A.P hemical and Allied Prod primary Metal Industries urniture and Fixtures op. & Oth. Fin. Prod Food Kindred Product ob. Metal Industries extile Mill Products Communication

Miscellaneous Services Nonclassifiable Establishments

lealth Services

lotels Room. Houses Camp AOLP

told, and Other Inv. Comp.

nsurance Carriers

Cred. Agen. Olh. Than Banks

**Eating And Drinking Places** 

Banking

Seneral Merch. Stores

ood Stores

29

### TABLE V

### SIMULATION RESULTS 1975 HISTORIC SIMULATION:

# LIABILITY STREAM USED LONG TERM STUDY ABO

NUMBER	WEIGHT	SIC #	IDC	SECURITY NAME
1	3.00	67.	BTC	BELL CANADA ENTERPRISES
2 3 4 5 6 7	3.00	63	CBB	CHUBB CORP
3	3.00	33	X	USX CORP
4	3.00	35	HR	NAVISTAR INTL CORP WINN DIXIE STORES INC
5	3.00	54	WIN	CBI INDS INC
5	3.00	13	CBI WWP	WASHINGTON WTR PWR CO
/	3.00 .	49 29	AHC9	AMERADA HESS CORP
8 9	3.00 3.00	35	UT	UNITED TELECOMMUNICATIONS
10	3.00	10	AMX	AMAX INC
11	3.00	67	ASA	ASA LTD
12	3.00	49	PGN	PORTLAND GEN CORP
13	3.00	64	AXD	ALEXANDER & ALEXANDER SVCS
14	3.00	13	KMG	KERR MCGEE CORP
15	3.00	48	T	AMERICAN TEL & TELEG CO
16	3.00	63	ĊIC	CONTINENTAL CORP
17	3.00	60	FBG1	BANC ONE CORP
18	3.00	33	NS	NATIONAL INTERGROUP INC
19	3.00	26	KMB	KIMBERLY CLARK CORP
20	3.00	36	MSU9	MATSUSHITA ELEC INDL
21	3.00	13	GAS	NICOR INC
22	3.00	49	CPL	CAROLINA PWR & LT CO
23	3.00	37	UA	UNITED TECHNOLOGIES CORP
24	3.00	64	MMC	MARSH & MCLENNAN COS INC
25	3.00	12	BNI	BURLINGTON NORTHN INC
26	3.00	20	K	KELLOGG CO
27	3.00	63	UFY	USF&G CORP
· 28	3.00	34	AC .	PRIMERICA CORP
29	3.00	13	SN	AMOCO CORP
30	3.00	27	DNY	DONNELLEY RR & SONS CO
31	2.23	10	AL	ALCAN ALUM LTD
32	• 1.92	33	IAD	INLAND STL INDS INC
33	1.63	32	PPG	PPG INDS INC
34	1.41	60	FML	FIRST BK SYS INC PACIFIC LTG CORP
35	1.00	49	PLT	LEHMAN CORP
36	0.83	67 10	LEM Unp	UNION PAC CORP
37	0.51	10		OCCIDENTAL PETE CGPCR
38	0.48	13	OXY	OCCIDENTAL PETE COPCE

30

TABLE VI

### SIMULATION RESULTS 1980 HISTORIC SIMULATION:

# LIABILITY STREAM USED LONG TERM ABO

NUMBER	WEIGHT	SIC #	IDC	SECURITY NAME
1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 27 28 29 30 31 31 31 31 31 31 31 31 31 31 31 31 31	3.00 3.00 3.00 3.00 3.00 3.00 3.00 3.00	49 28 60 36 60 26 28 20 49 28 26 60 20 30 49 13 28 53 33 26 20 34 28 37 37 36 49 36 37 37 36 49 36 37 37 37 38 38 38 38 38 38 38 38 38 38 38 38 38	NKF KHOBBALLER CHL TOWN STANK WHOBBALLER CHL POLY POLY POLY POLY POLY POLY POLY POL	NIAGARA MOHAWK PWR CORP INTERNATIONAL FLAVORS & FR MELLON BANK CORPORATION WHIRLPOOL CORP NORWEST CORP KIMBERLY CLARK CORP WARNER LAMBERT CO RALSTON PURINA CO KANSAS GAS & ELEC CO BORG WARNER CORP UNION CAMP CORP CHEMICAL NEWYORK CORP KELLOGG CO GOODYEAR TIRE & RUBR CO POTOMAC ELEC PWR CO LOUISIANA LD & EXPL CO PROCTER & GAMBLE CO FEDERATED DEPT STORES INC NATIONAL INTERGROUP INC FORT HOWARD CORP BORDEN INC GENERAL MLS INC PRIMERICA CORP GLAXO HLDGS PLC GILLETTE CO GENERAL MTRS CORP INTERCO INC AMERICAN TEL & TELEG CO CAMPBELL SOUP CO GOULD INC MARTIN MARIETTA CORP FORD MTR CO DEL CHRYSLER HLDG CO PENNSYLVANIA PWR & LT CO AMERICAN EXPRESS CO OWENS CORNING FIBERGLAS CO PILLSBURY CO

### TABLE VII

### 1975 INDUSTRY WEIGHTINGS

Electric, Gas and Sanitation Utilities, and Banking Restricted to 10% of Portfolio.

Code	Industry	% of Portfolio
10 12 13 20 26 27 29 32 33 34 35 36 37 48 49 54 60 63 64 67	Metal Mining Bituminous Coal & Lignite Min. Oil & Gas Extraction Food Kindred Products Paper and Allied Products Printing Publishing and A.P. Petroleum Refin. & Rel. Prod. Stone Clay Glass & Conc. Prod. Primary Metal Industries Fab. Metal Prod. Ex. M.&T.E. Machinery Except Electrical Ele. and Ele. Mach. Transportations Equipment Communication Electric Gas and Sanit. Serv. Food Stores Banking Insurance Carriers Ins. Agents Brok. Serv. Hold. and Other Inv. Comp.	5.74% 3.00 12.48 3.00 3.00 3.00 1.63 7.92 3.00 6.00 3.00 3.00 3.00 4.41 9.00 6.00 6.00

# SPANNING PORTFOLIO 1/1/75

Market Capitalization Average High Low	(000,000) \$1,203 \$8,393 \$ 137
Shares Outstanding Average	(000) 74,840 shares
Dividend Yield	5.1%
Price Earning Ratio	13.1x
Number of Stocks	38
Turnover 1975-1976	21.3%

Turnover 1980-1981

### TABLE VIII

# 1980 INDUSTRY WEIGHTINGS

Electric, Gas and Sanitation Utilities, and Banking Restricted to 10% of Portfolio.

Code	Industry	% of Portfolio
13 20 23 26 28 30 32 33 34 36 37 48 49 53 60	Food Kindred Products App. & Oth. Fin. Prod. Paper and Allied Products Chemical and Allied Prod. Rubber and Misc. Plast. Prod. Stone Clay Glass & Conc. Prod. Primary Metal Industries Fab. Metal Prod. Ex. M.&T.E. Ele. and Ele. Mach. Transportations Equipment Communication Electric Gas and Sanit. Serv. General Merch. Stores Banking	3.00% 15.62 3.00 9.00 15.00 3.00 6.00 8.05 7.38 3.00 10.00
•	SPANNING PORTFOLIO 1/1/80	•
A H	talization verage igh ow	(000,000) \$1,790 \$13,311 \$ 247
Shares Outs		(000) 130,229 shares
Dividend Yi		6.9%
Price Earni		6.6x
Number of S		37
number of 3		30.4%

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### TABLE IX

### SIMULATION RESULTS 1985 HISTORIC SIMULATION:

# LIABILITY STREAM USED LONG TERM STUDY ABO

NUMBER	WEIGHT	SIC #	IDC	SECURITY NAME
NUMBER  1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40	WEIGHT  3.00 3.00 3.00 3.00 3.00 3.00 3.00 3.	SIC # 53 49 58 60 23 28 60 99 45 20 38 78 28 20 45 78 28 28 28 28 28 28 28 28 28 28 28 28 28	JCP HCD SEMIPTILL SEMIPTIL	PENNEY J C INC HAWAIIAN ELEC I MCDONALDS CORP SOUTHEAST BKG C RUSSELL CORP AVON PRODS INC MANUFACTURERS HAN CASH: TBILLS 0.0 DPL INC MILLIPORE CORP UNILVER PLC EASTMAN KODAK C COMMERCE CLEARI SQUIBB CORP PFIZER IND COCA COLA CO DELTA AIR LINES NEW ENGLAND ELE STONE & WEBSTER GREAT WESTN FIN SMITHKLINE BECKMAN SCHERING PLOUGH SYSCO CORP MINNESOTA MNG & DISNEY WALT CO HILLENBRAND IND BALTIMORE GAS & ELE MEDTRONIC INC KELLY SYCS INC PRIME COMPUTER SYNTEX CORP FLUOR CORP BANC ONE CORP AHMANSON H F & ALLEGHENY PWR SYS CENTEL CORP CPC INTL INC PROCTER & GAMBLE AMERICAN HOME PRODS GILLETTE CO DAYTON HUDSON C
41 42	0.41 0.13	53 47	FEDX	FEDERAL EXPRESS

### TABLE X

# 1985 INDUSTRY WEIGHTINGS

Electric, Gas and Sanitation Utilities, and Banking Restricted to 10% of Portfolio.

		% of
Code	Industry	Portfolio
0000		1.76%
16	Const. Oth Than B.CG.C.	7.09
20	Food Kindred Products	3.00
23	: Ann & Oth. Fin. Prog.	2.68
25	Emplifier and FIXTURES	3.00
25 27 28	péinting Publishing and A.r.	18.13
20	Chamical and Aliled Proo.	0.54
34	Fah Metal Prod. EX. M.&I.E.	5.05
34 35	Machinery Fycent Electrical	8.53
35	Mase Anal & Lont. Inst. Ltc.	
38	Transportation By Air	3.00
45		0.13
47	Communication Communication Clockeric Gas and Sanit. Serv.	1.22
48	Electric Gas and Sanit. Serv.	10.00
49	Wholesale Trade-Nondur. Goods	3.00
51	General Merch. Stores	3.41
53	Eating and Drinking Places	3.00
58	Eating and Drinking ridges	7.70
60 ·	Banking Oth Than Banks	3.00
61	cred. Agen. Oth. Than Banks	1.54
63 67	Insurance Carriers	3.00
67	Hold. And Other Inv. Comp.	2.30
73	Business Services	2.93
78	Motion Pictures	3.00
89	Miccollanguic Services	3.00
99	Monclassifiable Establishments	<b>3.00</b>
••		

# SPANNING PORTFOLIO 1/1/85

Market Capitalization Average High Low	(000,000) \$3,045 \$11,689 \$ 373
Shares Outstanding Average	(000) 97,120 shares
Dividend Yield	4.0%
Price Earning Ratio	11.0x
Number of Stocks	41
Turnover 1985-1986	15.0%

Index

Index Diff

-23.31

.00

-670.98

35

### Table XI ANALYSIS OF PROGRAM SIMULATION

Target & Index represent the Standard & Poors 500 Stock Index portfolio represent optimizer chosen portfolio. One example of the benefits of the technique are seen in the monthly statistics, where the annualized standard deviation of returns is 14.6% for the optimized portfolio vs. 16.04 for the S&P 500.

# ANNUALIZED MONTHLY STATISTICS

	MEAN	STD DEV	SKEW * 10^6
Target	15.88%	16.04%	-50.00
Portfolio	17.97%	14.60%	-19.72
Portfolio Diff	2.09%	4.40%	.01
Index	15.88%	16.04%	-50.00
Index Diff	.00%	.00%	.00
ANNUALIZED QUART	ERLY STATISTION	cs	
	MEAN	STD DEV	SKEW * 10^6
Target	16.18%	17.04%	-172.12
Portfolio	18.40%	16.19%	-41.29
Portfolio Diff	2.23%	3.99%	1.58
Index	16.18%	17.04%	-172.12
Index Diff	.00%	.00%	.00
ANNUAL STATISTICS	5		
	MEAN	STD DEV	SKEW * 10^6
Target	16.38%	13.63%	-670.98
Portfolio	19.01%	13.43%	-61.67
Portfolio Diff	2.63%	4.43%	-23.31

.00%

13.63%

.00%

16.38%

statistical correlation with the liability return is further evident in Table III and FIG. 5, wherein detailed comparisons are made between the selected portfolio of assets and the standard liability return.

In FIG. 6 a range of simulation funding returns for the portfolio of assets are compared with a typical pension fund a mixture of stocks, bonds, real estate and treasury bills. Clearly, the risk is much higher for the typical pension fund; and dramatic improvement in the return, or reduction of risk, results when only 35% of the standard pension fund is modified using the method of the invention.

In another embodiment, a portfolio of assets can be constructed by selecting a portion of a total portfolio with assets having optimal correlation of asset return to a liability or financial index. The remainder of the portfolio comprises futures contracts which are combined with the correlated portfolio portion to achieve in effect an optimum correlation for the entire portfolio of assets. Further details are set forth in Appendix IV.

In another aspect of one embodiment, control can be exerted over pension plan surplus by adjusting the level of risk selected for a portfolio of assets. As illustrated in FIG. 6, the expected return can be selected at various levels with the degree of risk, or standard deviation of the funding level, generally increasing as one moves from a position of

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minimum risk at the top of the "bullet" to higher future returns. Control over a pension plan surplus, or for that matter any plan for which you wish to respond dynamically to control risk/return in concert, can be accomplished over a wide range of risk and return values. Such an approach can be used to manage return under variable risk positions and minimize insurance costs for protecting against underfunding of a plan, such as falling below a predetermined minimum floor. Consequently, as the funding level approaches 100% a minimum risk portfolio of assets should be constructed using the methods described hereinbefore. As the surplus accumulates, the acceptable risk level can be increased for the portfolio of assets by dynamic modification of the portfolio asset components. One can utilize futures contracts as an overlay for an underlying portfolio of assets, having been selected by the basic invention described previously, to create in effect an optimum statistical correlation for the entire portfolio, including the futures contracts. As the surplus approaches 10% - 20% excess, a portfolio of assets can be constructed resulting in a much higher level of future return. For example, in FIG. 6, the change in future return from minimum risk to the highest return data point is about a 35% greater return but with an accompanying 70% - 80% increase in standard deviation compared to the minimum risk point.

In a further embodiment of the invention one can overcome problems associated with an indefinite covariant matrix. The current system and method does not use the full covariance matrix to extract a partial derivative to guide the search process, and thus it is not subject to one of the failures that results using standard quadratic programming.

To us standard quadratic programming algorithums the covariance matrix must be positive semi-definite, or positive definite. This means technically that no row of the matrix can be replicated by a linear combination of other rows.

However, this condition occurs when there are fewer returns than the number of securities under consideration.

This is a significant shortcoming of the standard methodlogy.

For example, to consider five hundred securities

simultaneously, the user must supply at least five hundred and one returns for each security being considered. If monthly data is being used for the return series, at least forty-one years of data must be available for each security under consideration. Most securities have not been in existence for this period of time.

If not enough returns are available or if the matrix is indefinite, the standard quadratic solution techniques will fail to find a solution point that is optimal.

The current system allows a solution, which is at least as good as any other feasible solution, to be achieved without regard to the sensitivity of the covariance matrix.

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Problems that otherwise could not be solved by standard technologies are solved by the current system. This allows practical portfolios to be selected even though there is limited available return information.

In another aspect of the invention involving practical applications of the current methodology to managing security portfolios, the ability to invest dividend income and other cash flows efficiently is also an important element in effective management. The current system allows a portfolio manager to invest available cash in the most efficient securities while considering the current portfolio holdings. Effectively this allows the manager to invest in securities which best enhance the current portfolio position without selling any of the current holdings. In a practical portfolio management system the ability to reinvest cash flows efficiently is always an important consideration. The current system provides this ability. An illustration of a reinvestment solution is provided in Appendix V which lists data used and results obtained in performing the reinvestment method.

In addition to finding optimal portfolios for tracking financial targets, the current system allows other objectives to be considered and incorporated in the solution. Examples include supplementing the basic objective function with an income objective, tax impact objective, or a company cash flow

objective. The system is flexible enough to allow the objective function to be customized for particular applications.

As an example, an investor who has a preference for securities with high dividend yields will specify an objective function which explicitly states the trade off between portfolio tracking and dividend income. The computer routine to optimize a portfolio (the optimizer) will extract the partial derivatives of this objective function and proceed to select an optimal portfolio which exactly incorporates the specified trade-off between dividend income and tracking. This investor then has a custom solution which addresses his particular concerns and requirements.

The consideration of transaction costs associated with buying and selling securities is incorporated into the portfolio optimization system to control expenses due to trading. The trade off between tracking accuracy and transaction costs can be specified by the investor. This allows for a customized objective function, with regard to expected transaction costs, for each client.

Investors may also have tax effects to consider when trading from one security to another. The taxable gains and losses and their impact on expected return can be specified by the investor so as to control these costs.

Another preference which can be incorporated into the objective function and handled explicitly by the optimization

system is the consideration of cash flows. An investor may have a preference for investing in companies which have large and positive cash flows. This objective can be incorporated into the system and resulting portfolios will reflect this investment goal.

While preferred embodiments of the present invention have been illustrated and described, it will be understood that changes and modifications can be made therein without departing from the invention to its broader aspects. Various features of the invention are defined in the following claims.

#### APPENDICES TO SPECIFICATION

- APPENDIX I Spanning Program for creating an optimal target tracking portfolio of securities (Appendix I pp. 1-27;). Also includes 4 pages of Output.
- APPENDIX II Liability Return Program for creating a return series for a liability stream from yields (Appendix II pp. 1-2).
- APPENDIX III Correlation Portfolio Program for creating an optimal index correlation portfolio with securities (Appendix III pp. 1430).
- APPENDIX IV "Fasttrack" Program for analyzing large numbers of securities in a rapid, efficient manner to provide optimum correlation of asset return to a time dependent financial index. Substantial computer memory storage reduction is also achieved.
- APPENDIX V Data listing of method for reinvestment of available cash flow beginning from a current portfolio.
- APPENDIX VI Example illustrating distinctions between current system and prior art.

## APPENDIX I

## SPANNING PROGRAM

To create an optimal target tracking portfolio of securities.

(Appendix I pp. 1-27)

IF (HOLDEX . EQVFALSE.) THEN  WRITE(*,*) FILE NOT FOUND ., HOLD  END IF  END IF  ELSE  WRITE(*,*) FILE NOT FOUND ., HOLD  CALL HULTRUM(1SKIP)  END IF  END IF  CALL HULTRUM(1SKIP)  CALL SAVDAT  CALL SAVDAT	NM = NMSAVE NM = (INT(NM/100)-80)*12+(NM-INT(NM/100)*100) IREAD = NSTATHNSIMS IF(NSTOCKS.GT.O)THEN XBUPPER = SMAX END IF C************************************	NUM = NSTOCKS+NBONDS  IF(NUM,GT.MD)THEN  MRITE(*,*)' WARNING NUM >',ND,' TOO BIG FOR PROGRAM'  STOP  ENDIF  ICOL = ID  KE = KEQ  KKK = KE  IA = ND	22 L	BULLET BULLET BULLET)/1000.	ELSE WRITE(**):INPUT NUMERATOR' C REACK(**):XNUM C REACK(**):XNUM XNUM = 0.10
TURN = XNUM*(100./(TURN1+.01)-100.0/100.01)  END IF  CALL CO/IN (NUM, IREAD, IFIRST, ILAST)  CALL HOLDING (NUM, HOLD, IPORT)  WRITE(* 101)'CALLING MATRIX  CALL MA'RIX (NUM, IREAD)  ***********************************	CALL BOLNDS (NIM.ICCL, MAN)  ***********************************	MAXMS = :*(2*NUM+ID)*(2*NUM+ID)+8*(2*NUM+ID)+6 ITURN = :) CALL QSE' ( NUM, MAXMS, ITURN ) ********* IF TURNOVER IS CONSIDERED, CALL TURNOV IF(TURN GT. 0.0) THEN ITURN = 1 CALL (ISET (NUM, MAXMS, ITURN) END IF	**************************************	**************************************	WRITE(*, 1)1) CALLING BAL

	UPDATE December 6, 1988
c	PROGRAM SPAN
•	INCLUDE 'COMMON.F' CHARACTER*30 HOLD LOGICAL ICOUNT LOGICAL HOLDEX
c c	********* WRITE COPYRIGHT TO SCREEN **********
	INCLUDE 'COPYRIGHT.F'
С	**************
С	**************************************
5	CONTINUE
C	DEFAULT READ IN OF 24 MONTHS PRIOR = NSTAT, NRESTS FOR B( ) ****
	NSTAT = 24 NRETS = 24 BULLET = 0.0 TARGET = 1. TURN = 100. ITYPE = 1 ICHANGE = 0 XBLOWER = .ODO XBUPPER = 3.0DO SMAX = XBUPPER
C	CALL FLASH  CALL FLASH  CALL FLASH TO INTRODUCE S P A N ****
С	*********** IF 'COUNTS' EXISTS THIS IS A MULTIPLE RUN ****  INQUIRE (FILE = 'COUNTS', EXIST = ICOUNT)
c c c	IF (ICOUNT .EQVFALSE.) THEN  CALL INTRO  CALL INTRO  CALL MODIFY  CALL MODIFY  CALL MODIFY  READ IN THE HOLDINGS FILE  WRITE(*,*)'INPUT PORTFOLIO #, AND NAME OF HOLDINGS FILE'  READ(*,*)IPORT,HOLD  INQUIRE (FILE = HOLD,EXIST = HOLDEX)
_	·

IF (ICOUNT.EQY. TRUE.) THEN WRITE(*,102)'DONE WITH RUN NUMBER ',1SKIP GO TO 5 END 1F		END END OF MAIN PROGRAM SPANI  C ***********************************	INCLUDE 'COMMON.F' CHARACTER*30 XTITL,XFLOUT,XLIBIN,XSTKIM,XBNDIN	OPEN (13,FILE = MULTIN',STATUS = 'OLD') IF (ISKIP.EQ.0) GO TO 30	DO 10 I = 1, ISKIP DO 20 J = 1,18 READ113, (A1)', END = 99)GARB CONTINUE CONTINUE	CONTINUE READ(13, 101, END = 99) TI READ(13, 101, END = 99) READ(13, 101, END = 99) READ(13, 101, END = 99)	READ(13, 101, END = 99) BONDIN READ(13, *, END = 99) MYSAVE READ(13, *, END = 99) NSINS READ(13, *, END = 99) NSOCKS READ(13, *, END = 99) NDONDS READ(13, *, END = 99) STOCKMIN READ(13, *, END = 99) STOCKMIN	READ(13,*, END = 99) SNAX READ(13,*, END = 99) NRSTAT READ(13,*, END = 99) BULLET READ(13,*, END = 99) BULLET READ(13,*, END = 99) TARGET READ(13,*, END = 99) TURN	01 FORMAT (A20) ISKIP = ISKIP+1
	101	TRUM ************************************		ISE: OLD OR HOLDINGS RUN **	25	. e			101
CLOSE(13) RETURN	****: STOP DONE WITH MULTI RUN ******** 9 CLOSE(13) WRITE(*,*)'DONE WITH MULTIPLE RUN ***********************************	END  ***********************************	DIMENSION VAL(ND) CHARACTER+9 SYMBL, IDCSYM(ND) CHARACTER+30 HOLD	C **** IHOLD IS READ FROM-FIRST SCREEN RESPONSE: OLD OR IF (IHOLD .EQ. 0) GO TO 999	OPEN (25,FILE - HOLD,STATUS - '0LD') (PORT - REAL(IPORT)	IEAD(25,*, END = 44)SYMBL, VALUE  IF (SYMBL . EQ . IDCSYMBL) THEN  IF (VALUE . EQ . X-PORT) THEN  READ(25,*, END = 44)SYMBL, VALUE  READ(25,*, END = 44)SYMBL, VALUE  IF (SYMBL . EQ . IDCSYMBL,) GO TO 44	iDCSMII) = SYMBL VAL(I) = VALUE GO TO 33 FEAD(25,*, END = 44) GARB END IF GO TO 22	CONTINUE NIDC - I I (NIDC . EQ. 0)THEN WRITE(*,*) PORTFOLIO NUMBER NOT FOUND ', IPORT WRITE(*,*) ENTER PORTFOLIO NUMBER AGAIN' READ(*,*) IPORT	REVIND(25) GO TO 11 E (D 1F
	66			:	Ξ	33 %		4	

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```
IFIRST IS FIRST MONTH OF DATA NEEDED FOR MATRIX ILAST IS LAST MONTH OF SIMULATION
                                                                                                                                                                                                                                                                                                                                                                                                                                                    READ IN STOCK DATA
                                                                                                                                                        C *************** READ IN LIABILITY RETURNS ******
                                                                                                                                                                                                                                                                                                                                                                                                                                                          IF (NSTOCKS.GT.O) THEN
OPEN (4,FILE = STOCKIN, STATUS = 'OLD')
                                                 SUBROUTINE COVIN (NUM, IREAD, IFIRST, ILAST)
                                                                                                                                                                                    OPEN (9, FILE - LIABIN, STATUS - 'OLD')
                                                                                                                                                                                                                                                                                                                     DO 300 I - 1, IFIRST-ISTART
READ (9,111) GARB
CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    DO 700 I - 1, NSTOCKS
                                                                                                                                                                                                                                                                                                                                                                       DO 400 I = 1, IREAD
READ (9,*) ANIM(1)
CONTINUE
                                                                                                                                                                                                                                   CONTINUE (9,111) GARB
                                                                                                                                       INCLUDE 'COMMON.F'
                                                                                                                                                                                                                                                                                   READ (9,*) ISTART
READ (9,*) ISTOP
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      600 CONTINUE
1111 FORMAT (A40)
                                                                                                                                                                                                                                                                                                                                                                                                                       CLOSE(9)
                                                                                                                                                                                                            READ (
                                                                                                                                                                                                                                                                                                                                                                                                 400
                                                                                                                                                                                                                                                            200
                                                                                                                                                                                                                                                                                                                                                 300
                                                                                                                                                                                                                                                                                                                                                                                                                                (IDCTEST.EQ.1) THEN
RITE(*,*)NIDC-NCOUNT-1,'SYMBOLS NOT FOUND..PROGRAM STOPPING'
                                                                                                                                                                                                                                                                                                                                                                                RITE(*,*)IDCSYM(1),": SYMBOL NOT INCLUDED IN RETURN FILE"
                                                                                                                                                            (ICASH .Eq. 0) THEN
WRITE(*,*)'NO CASH INCLUDED....PROGRAM STOPPING'
                                                                                                                                                                                                                                                                         ) J = 1,NUM
10C(J)(1:4) .EQ. IDCSYM(I)) THEN
ITEST = 1
                                                                                                                                                                                                                                                                                                          NCCUNT - NCOUNT+1
OLDWT(J) - VAL(I) / PORTVAL
                                                                                                                                                                                                                                                                                                                                                          ST Eq. 0) THEN
                                                                                                                                                                                                                                                                                                                                                                                             END 1F
CCNTINUE
                                                                                                                                                                                                N IF
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   OP! N(21,
DO 90 I
                                                                                                                                                                                                                                                                                                                                                                                                                                                                    EN.) IF
                                                                                                                                               2
                                                                                                                                                                                                                                                                                                                                              30
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   666
                                                                                                                                                                                                                                                                                                                                                                                                         20
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             8
```

```
END OF SUBROUTINE MATRIX
                                                                                                                                                                                                                                                                              A{1,3} = A{1,3}+(RET(K,1)-AVE(1))*(RET(K,3)-AVE(3)) / XXX
A{3,1} = A{1,3}
                               ***** CALCULATE COVARIANCE MATRIX *********
DO 215 I = 1,NUM
DO 215 J = 1,NUM
A(1,J) = 0
DO 215 K = 1,NSTAT
                                                                                                                                                                    IF(A(1,3).GT.50)WRITE(*,*)'COV TOO BIG',A(1,3),1,3 CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                       DO 80 1 = 1,NUM

BDL(1) = XBLOWER/100.0

BDU(1) = XBUPPER/100.0

IF(OLDMT(1).GT.BDU(1))THEN

IF(OLDMT(1).GT.SCAL*BDU(1)) THEN

ELSE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      END IF
IF (1.GT.NSTOCKS) BDU(1) = 1.
                                                                                                      XXX = DBLE (NSTAT-1)
213 CONTINUE AVE(1)*BULLET
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             BOU(1) = OLDWT(1)
END 1F
                                                                                                                                                                                                                                                                                                                               INCLUDE 'COMMON.F'
                                                                                                                                                                                                        RETURN
                                                                                                                                                                                                                                ENG
                                                                                                                                                                                 215
                                                                                                                                                                                                                                                                                                                                        END OF SUBROUTINE COVIN
                                                                                                                                                                                                                                                                                                                                                                         IF END OF FILE WAS HIT ON STOCKS - RESET NUM AND CONTINUE ***
NUI = NSTOCKS+NBONDS
G(TO 1400
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     DO 214 J = 1,NRETS
AVE(1) = AVE(1)+RET(J,1)/DBLE(NRETS)
CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                        DO ::33 1 = 1,NUN

iO 244 3 = 1,NSTAT

RET(3,1) = RET(3,1)-ANIM(3)+TARGET

CONTINUE

CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                          IREAD - NSTAT+NSIMS
NUM - NSTOCKS+NBONDS
           DO 1001 J = 1,NRETS-NSTAT
READ(7,*)GARB
CONTINUE
                                                                                                                                            DO 1300 J = 1,1STOP-ILAST
READ (7,111) GARB
CONTINUE
                                                                                  DO 1010 K =1, IREAD
READ (7,*) RET(K,1)
J = JJ + K
CONTINUE
                                                           JJ - NRETS-NSTAT
                                                                                                                                                                                                                   ENDIF
CL 3SE(7)
RE TURN
                                                                                                                                                                                              CC NT INUE
                                                                                                                                                                                                                                                                 C ***
785
                                                                                                                     1010
                                   100
                                                                                                                                                                    1300
                                                                                                                                                                                             900
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                214
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              244
```

	C **************** BEGIN OUTPUT PROCEDURES ************ UANIM = 0.0 DO 129 I = 1.NRETS UANIM = UANIM + ANIM(I)/DBLE(NRETS)	×6	-XTOT+X(I) -X(I) -X(I) -X(I):LI0.001) THEN	WRITE(*,*)**********************************	,	IF (ABS.KIU1-I.O) .GI. 0.005) IHEN WRITE(**):**********************************	MRITE (* * ) * *****************************		TAIN STANNING SITULIAN STANNING SITULIAN KESULIS	OPENIO,FILE-FILEGUT,STATUS-'UNKNOWN') REWIND(10)	WRITE(10,*)' NATIONAL INVESTMENT SERVICES SPANNING TECHNOLOGY' WRITE(10,*)' NATIONAL INVESTMENT SERVICES SPANNING TECHNOLOGY' WRITE(10,*)' A SIMULATION RESULTS'		E(10,*)' LIABILITY ST E(10,*)	E 50.	
Ξ	D(4) = -Y MAX/100.0 D(5) = -Y MAX/100.0 D(6) = -Y MAX/100.0	SICEDS. = SICED+SICE3+SICE7 IF(SIC49*100.6T.YIMAX.AND.SIC49*100.LT.SCAL*YIMAX)D(4) = -SIC49 IF(SIC60\$*100.GT.YIMAX.AND.SICEDS*100.LT.SCAL*YIMAX)D(5)=-SICEOS IF(SICE07*100.GT.YIMAX.AND.SICE7*100.LT.SCAL*YIMAX)D(6) = -SICE7	IF( \$1C48*100.GT.SCAL*YIMAX) D(4) = D(4)*SCAL IF( \$1C608*100.GT.SCAL*YIMAX) D(5) = D(5)*SCAL IF( \$1C67*100.GT.SCAL*YIMAX) D(6) = D(6)*SCAL		(J. Eq. 4. AND. 151C(1). Eq. 49) (C(1, J) = (J. Eq. 48) (C(1, J) = (J. Eq. 5. AND. 151C(1). Eq. 48) (C(1, J) = (J. Eq. 5. AND. 151C(1). Eq. 60) (C(1, J) =	IF (J. EQ. S. AND. ISIC(I). EQ. 63) C(I; J) = -1.0 IF (J. EQ. S. AND. ISIC(I). EQ. 67) C(I; J) = -1.0 IF (J. EQ. 6. AND. ISIC(I). EQ. 67) C(I; J) = -1.0	52 CONTINUE 51 CONTINUE	C CLOSE (6)	WWW = Z*NUM+1COL	RETURII	END C ***********************************	C ************************************	TOOLO TITL TOOL (TOOL)	INCLUIE "COMMON.F"	C ******* RESET THE RETURNS TO ORIGINAL STATE ***************

```
WRITE(10,649) STD, XRET
FORMAT(1X, MINIMUM STD DEV =',F10.4,' EXPECTED RETURN =',F10.4)
WRITE(10,*)
                                                                                                                                                                                                                                                                 SUBROUTINE TRACKER (NUM. IREAD)
                                                                                                                                                                                                                  END OF SUBROUTINE PORT
                                                                                                                                                                                                                                                                                                                            SET STAT ARRAY 1 - LIABILITY, 2 - PORTFOLIO, 3 - DIFFERENCES
DO 250 1-1, READ
STAT(1,1)-ANIM(1)
                                                                                                                IF(ITYPE.EO.1.AND.XTOT.LT..995)WRITE(10,*)' ERROR ***** '
.' SUN OF X S = X',XTOT*100.
IF(ITYPE.EQ.1.AND.XTOT.GT.1.005)WRITE(10,*)' ERROR *****
. SUM OF X S = X',XTOT*100.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           CALCULATE AVERAGES

*** CALCULATE AVERAGES

*** SET NSIM TO 2 FOR STATISTICS IF NSIMS.LT.1

IF (NSIMS.LT.1) NSIM = 2

DO 260 I=NSTAT.*
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        F (NSIMS.LT.3)GOTO 318
                                                                                                                                                                                                                                                                                                                                                                                                                                                               STAT(I,3)-(PREH(1)-ANIM(1))
                              STD=(XVAR*12)**(0.5)*100
XRET = XRET*12.0*100.0
   WRITE(10,*)
                                                                                                                                                                                                                                                                                                                                                                                            400 CONTINUE
                                                                                                                                                                              RETURN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           ***** 3
                                                                                                                                                                                                                                                                                                                                                                                                                   *** 3
                                                                              649
                                                                                                                                                                                                                                                     u
WINTE OUT THE NEW WEIGHTS TO A FILE CALLED 'OLD'*******

OPIN(15, FILE = 'OLD', STATUS = 'OLD')

REHIND(15)

DO 140 1 = 1, NUM

WRITE(15,940) CUM(1)*100

CON TINUE

CLORT(IX,F15.8)

CLC SE(15)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        WRITE(10.16) ICOUNT X(1)*100, CUM(1)*100, C(1,1)*100, ISIC(1), IDC(1), NAME(1)
                                                                                                                                                                                                                                                                                                                                     XVAR-0.0
XVAR-0.0
XRET = 0.0
ICO.NT=0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             (RETI = AVE(1) + UANIM
(RET = XRET + X(1)*XRETI
CONTINUE
FORMIT(1X,14,1X,2F6.3,F7.3,14,1X,A9,1X,A36)
                                   PRET(1) = 0.0

DO 900 J = 1,NUM

PRET(1) = PRET(1) + RET(1,J)*X(J)
                                                                                                                                                                                                                                                                                                                                                                                                            DO 131 1-1,NUM
C(1,1)--8(1)
DO 132 -1,NUM
C(1,1)-(1,1)+X(J)*A(1,3)*2
XVAR-XVAR+X(1)*X(J)*A(1,3)
CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    ICOUNT-ICOUNT+1
IF(I.GT.NSTOCKS)ICOUNT-I
                                                                                                                                                                                               1001
801
                                                                                                                                                                                                                                   ***
                                                                                                                                                                                                                                                                                                 140
940
ںں
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     133
```

W ITE (10,\*)

132

|SIMS.LT.1) NSIM = 2 |SIMS.LT.1] NSIM = 2 |GO I=NSIMT+1, IREAD |AVE(1)=AVE(1)+ANIM(1)/DBLE(NSIM)

```
C ***** WRITE MONTH, LIABILITY RET, PORTFOLIO RET, DIFFERENCE **** DO 700 I=NSTAT+1,IREAD
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       WRITE(10,*)
WRITE(10,*)'**********
WRITE(10,985)NM,NM+NSIMS-1
FORMAT(/, STATISTICS BASED ON MONTHS ',14,' THROUGH',14)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         WRITE(10,*)
WRITE(10,486)
WRITE(10,486)
FORMAT(1X,*CUMMULATIVE VALUES OF LIABILITIES AND ASSETS'/,
** MONTH LIABILITIES PORTFOLIO',/)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         WRITE STATISTICS BASED ON SIMULATIONS MONTHS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 WRITE ALPHA, BETA, STDERR, CORREL, AND R-SQUARED,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 'ALPHA', ALPHA, 'ANNUAL', ALPHA*1200
                                                                                                                                                                                                                                                                                                                                                     ISTAT = 1-(NSTAT+1)
MR.TE(10,612)ISTAT+NN,(STAT(1,J),J=1,3)
612 FORMAT(1X,3X,14,3F13.10)
700 CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  FORMAT (1X, 15, 7X, F7.3, 10X, F7.3)
CONTINUE
CONTINUE
BEGIN WRITING THE TRACKER OUTPUT
                                                                              WRITE(10,*) TRACKER OUTPUT FILE '
WRITE(10,*) MONTH LIA
WRITE(10,*)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      DO 847 I-NSTA
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              ***** 3
                                                                                      318
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       886
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 328
847
837
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  989
989
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     #SPAT+1, IREAD
-COV(1.J]+{(STÁT(K,I)-AVE(I))*(STAT(K,J)-AVE(J)))
                                                                                                                                                                                                                                                                                                                                                                             CALCULATE THE COVARIANCE MATRIX'S UPPER OFF DIAGONAL
                                                                         D(+ 950 I-1,3
VAR(1)-0.0
DO 950 K-HSTAT+1, IREAD
VAR(1)-VAR(1)+(STAT(K,1)-AVE(1))**2/DBLE(NSIM-1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   IF(|'AR(1).NE. 0.0) BETA = COV(1,2)/VAR(1)
ALPIA = AVE(2) - BETA*AVE(1)
                    CALCULATE COVARIANCES *****
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             CALCULATE CORRELATIONS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      74 ( [ ] -PRET ( ] - ] * ( ] +XX ( ) - ( ] +XX ( ] +XX ( ) +XX ( ] +XX ( ) +XX
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              SST = 0
SSE = 0
DO 552 I = 5
SST = 5
SST = 5
CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             269
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                952
```

		FORMAT(1X,.17) TARGET FORMAT(1X,.18) TURNOVER FACTOR **** WRITE HISTORICAL DATA USED TO MAKE B	WRITE(10,*) WRITE(10,*) WRITE(10,*) WRITE(10,*) WRITE(10,*) WRITE(10,*) DO 300 1=1, WSTAT	RETURN  END  C ***********************************	CC(1,1) CC(1,1) CC(1,2) CC(1,2
C ***** WRITE AVERAGES AND VARIANCES OF 1-LIAB, 2-PORT, 3-DIFFS **	STD DEV		WRITE(10,916) 'LIABILITY', AVE(1), VAR(1) WRITE(10,916) 'PORTFOLIO', AVE(2), VAR(2) WRITE(10,916) 'DIFFERINCE', AVE(3), VAR(3) 916 FORMAT(1X,3X,A11,9X,F9.2, 'K', 10X,F9.2', 'K')  C ****** WRITE PARAMETERS FOR THE RUN ***********************************	WRITE(10.*) WRITE(10.*) WRITE(10.*) WRITE(10.*) WRITE(10.101) WRITE(10.102) FILEOUT WRITE(10.103) LIABIN WRITE(10.104) STOCKIN WRITE(10.105) BONDIN WRITE(10.105) BONDIN WRITE(10.105) WSAVE WRITE(10.105) NASAVE WRITE(10.105) NASAVE WRITE(10.105) NASAVE WRITE(10.105) NASAVE WRITE(10.110) STOCKNIN WRITE(10.110) STOCKNIN WRITE(10.111) STOCKNIN WRITE(10.111) STOCKNIN WRITE(10.114) WSTOCK WRITE(10.115) WINAX WRITE(10.115) WINAX WRITE(10.115) WINAX WRITE(10.115) WINAX WRITE(10.115) WINAX	TARGI TURNI UNFULT FILENAME  1ABILITY STRAM FILE  1ABILITY STRAM FILE

```
CALL INDÚST
MRITE(10.*)
MRITE(10.*)
MRITE(10.*)
MRITE(10.102)(**,1-1,78)
MRITE(10.*), CODÉ
MRITE(10.*), CODÉ
MRITE(10.102)(**,1-1,78)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        DO 133 1 = 1,55
CUM(1) = 0.0
DO 134 J = 1,NUH
IF (ISIC(J).Eq.1) CUM(I) = CUM(I) + X(J)
                                                                                                                                                                                                                                                                                                                                                                                WRITE OUT THE INDUSTRY WEIGHTS INDUST
                                                                                                                                                                                                                                                                                                                                               FORMAT(1X, 4F7.3, 14, 4X, A9, 2X, A30) FORMAT(1X, 80A1)
                                                                                                                                                                                                                                                                  DO 90 I - 1, ISELL
XOLD - OLDWI(SELL(
XNEW - X(SELL(1))
WRITE(10,101) XOL
                                                                                                                                                                                                                                     MRITE(10,102)('*'
WRITE(10,*);
A
WRITE(10,102)(''
                                              DO 80 I - 1 IE

XOLD - OLDWT(E

XNEW - X(BUY(L)

WRITE(10,101)
                                                                                                                                                                                                                     WRITE(10,*)
                                                                                                                                                                                                                                                                                                                            CONT INUE
                                                                                                     CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                    ******* 3
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         133
                                                                                                                                                                                                                                                                                                                                                 101
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            134
                                                                                                                                                                                                                                                                                                                             8
                                                                                                                                                                                                                                                                                                                                                                                                                                                TURNOVER - ', TURNOV*50,' %
                                                                                                                                                                                                                                                                                                                   CC(SELL(I), KVAR)
                                                                                                                TURNOV - TURNOV + ABS(X(I)-OLDWT(I))
GONIINUE
                                      F(1)).GT.0.001) THEN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            WRITE THE BUYS
                                                                                                                                                                                                                                                                                                                                                                                                            CONT INUE
                                                                                                                                                                                                                                                                                                                                                                                    2
                                                                                                                                                                                                                                                                                                                                                                                                     9
```

```
135 FORMAT(1X,15,3X,A30,F10.2,' %')

SUWGHT - 0.0

DO 136 1 - 1,NMH

136 CONTINE 1 - 1,NMH

137 FORMAT(1X,A38,F10.2,' %')

FORMAT(1X,A38,F10.2,' %')

CLOSE(10)

FRIUGA

END FLEL(10)

FRIUGA

END OF SUBROUTINE BAL

SUBROUTINE INDUST

INCLUDE 'COMPON' F'

SIC(1) - AGRICULTINAL PRODUCTION-CROPS'

SIC(2) - AGRICULTINAL SERVICES'

SIC(3) - FISHING MINING'

SIC(1) - AGRICULTINAL SERVICES'

SIC(3) - FISHING MINING'

SIC(1) - AGRICULTINAL SERVICES'

SIC(1) - AGRICULTINAL SERVICES'

SIC(2) - FISHING MINING'

SIC(2) - FISHING MINING'

SIC(2) - FISHING MINING'

SIC(2) - FISHING MINING MINING MINING'

SIC(2) - FISHING MINING MINING MINING'

SIC(2) - FISHING MINING MINING
```

RETURN END C	THIS GOUTINE INTRODUCES THE SPANNING PROGRAM AND ASKS EOR SCREEN OR FILE INPUT OPTION INCLINE SCREEN OF FILE INPUT OPTION	IMFEREN RESPON	PARAMETER (MAXTXT = .60 % INES = .84) CHARACTER HEAD*(MAXTXT), LAST*(MAXTXT), OPTION(LINES)*(MAXTXT)	HEAD WELCOME TO THE NISA SPANNING OPTIMIZER'	NBROPT = 2 OPTION (1) = 'SINGLE RUN WITH WEIGHTS IN FILE: OLD' OPTION (2) = 'UPDATE RUN WITH WEIGHTS CALCUATED FROM HOLDINGS'	CALL NENU(LINES, HEAD, LAST, NBROPT, OPTION, RESPON)	IF (RESPON.EQ.1) THEN IHOLD = 0 CALL REDPAST	ELSE IF (RESPON.EQ.2) THEN IHOLD = 1 CALL REDPAST	ELSE WRITE(*,*)'NO OPTION SELECTED - PLEASE TRY AGAIN' GO TO 10	END 1F	C RETURN  ***********************************
00		• •	74 - 2			2					u !! !uuuu
MASA 16 BOND RETURNS FILE NASA 16 FIRST MONTH OF SIMULATION NSTRY: NSTOCKS NUMBER OF MONTHS TO SIMULATE NSTOCKS NUMBER OF STOCK TO SEND TO OPTIMIZER NBOMIS NUMBER OF BONDS TO SEND TO OPTIMIZER TOWN!Y NUMBER OF STOCKS TO READ PAST IN STOCKIN STOCKIN NUMBER OF STOCKS VIMAL: INDUSTRY MAXIMUM HOLDING	STACK  BULLIT = CLIMBING FOR TARGET  TARGIT = ADJUSTNENT FACTOR  TORN INCLUE: COMMON F.	PARAPETER (MAXTXI - 50, LINES - 24)	CHARICTER HEAD (MAXTXT) LAST* (MAXTXT), OPTIONS (LINES)* (MAXTXT)	** INITIALIZE READ IN FILE: PAST - 'PAST.DAT'	PAST (''PAST DAT' WRITE (*,100)('',1 = 1,5) WRITE (*,100)('',1 = 1,5) WRITE (*,100)('',1 = 1,5)	OPEN 18,FILE - PAST, STATUS - 'OLD', ERR - 10) READ(#.101)TITELET READ(#.101)FILEUIT READ(#.101)FILEUIT	READ(E, 101) LIABIN READ(E, 101) STOCKIN READ(E, 101) SOUDIN	READ (8 102 NRINS READ (8 102 NSIOKS READ (8 102 NSIOKS READ (8 102 NSIOKS)	READ(8.103) YIMAX READ(8.103) YIMAX CLOSE (8)	CONTINUE	GIVI OPTION TO READ FROM SCREEN WITHOUT DUMPING OUT OF PROCRAM OR TO READ FROM DIFFERENT FILE NAME HEAD = ' WARNING: THE PAST DATA FILE DOES NOT EXIST' LAST = ' WARNING: THE PAST DATA FILE OPTIONS(1) = 'INPUT NEW NAME FOR PAST DATA FILE' OPTIONS(2) = 'READ IN NEW DATA FROM SCREEN 'ILE'

FORMAT('0', A1)	WRITE(*,101) FORMAT(' 1) ENTER TITLE FOR SPANNING RUN - ',5) READ(*,'(A30)',END - 1,ERR - 1) TITLE WRITE(*,*)	WRITE(* 102) FORMAT(' 2) ENTER OUTPUT FILE NAME READ(*,'(a30)',END = 2,ERR = 2) FILEOUT WRITE(*,*)	WRITE(*,103) FORMA(* 3) ENTER LIABILITY RETURNS FILE NAME - '.\$) READ(*',(A30)',END = 3.ERR = 3) LIABIN WRITE(*,*)	WRITE(*,104) FORMAT(;4) ENTER STOCK RETURNS FILE NAME,\$) READ(*,(A30).,END = 4,ERR = 4) STOCKIN IF (STOCKIN.EQ.'')STOCKIN = 'STOCKS.PRN' WRITE(*,*)	WRITE(* 105) FORMAT(† 5) ENTER BOND RETURNS FILE NAME - '.5) FEAD(*', (A30)', END = 5, ERR = 5) BONDIN IF (BONDIN.EQ.', ')BONDIN = 'BONDS.PRN'	WRITE (***). 6) ENTER YEAR AND MONTH TO BEGIN	FORMAT (* SIMULATION (e.g. FEB 1987 = 8702) - '.S) READ(*,*,END = 6,ERR = 6) NHSAVE WRITE(*,*)	WRITE(*,107) FORMAT('7) ENTER NUMBER OF MONTHS TO SIMULATE - ',5) READ(*,*,EMD = 7,ERR = 7) NSIMS WRITE(*,*)	WRITE(*, 108) FORMAT(' B) ENTER NUMBER OF STOCKS TO USE . ',\$) READ(*, *, END = 8, ERR = 8) NSTOCKS WRITE(*,*)	WRITE(*,109) FORMAI(' 9) ENTER NUMBER OF BONDS TO USE - ',\$) READ(*,*,END - 9,ERR - 9) NBONDS WRITE(*,*)	WRITE(*,110) FORMAT(*10) ENTER NUMBER OF STOCKS READ PAST - '.\$}
113	101	102	303	104	105	9	106	107	8 108	9 109	011
20 CALL MENU (LINES,HEAD,LAST,NBROPT,OPTIONS,IRESPON)	IF ( IRESPON.EQ.1) THEN WRITE(*,100)(''',1 = 1,5) WRITE(*,104) READ(*, (A30)'.EMD = 20.ERR = 20) PAST GO TO \$\frac{1}{2}\$	ELSE IF (IRESPON.EQ.2) THEN CALL REDSCRN RETURN	END IF RETURN	100 (ORMAT('0', A1) 101 (ORMAT(A5) 102 (ORMAT(14) 103 (ORMAT(F7.2) 104 FORMAT('NAME FOR PAST DATA FILE ',\$)	END  ***********************************	JURKOU INE REDSCRN Attata estatatatatatatatatatatatatatatatatatata	TILE FILEOUT LIABIN STOCKTN	••••	II XUMY S. FOCKMIN Y. FMAX INCTEIDE * COMMON	** DEFAULT NAMES FOR STOCK AND BOND FILES  ** STOCKS.PRN & BONDS.PRN	WRITE(*,113)(' ',1 = 1,12)

READ(*,*,END =10,ERR = 10) IDUMNY MRITE(*,*) li WRITE(*,111)	111 FORMAT('11)'ENTER MINIMUM STOCK HOLDING - % ',\$) READ(*,*,*)END = 11,ERR = 11) STOCKMIN WRITE(*,*,*)	12 WRITE(* 112) 112 FORMAT(* 12) ENTER MAXIMUM INDUSTRY HOLDING - % ' ,\$) READ(* "EMD = 12.ERR = 12) YIMAX WRITE(*,4)	RETURN 100 FORMAT(A35)	END ************************************	erserrisekasekarakarakarakarakarakarakarakarakarakar	* ** THIS ROUTINE MODIFIES THE INPUT DATA IF RECESSARY INCLUDE 'COMMON.F'	10 WRITE(*,100)(' ',1 = 1,5) WRITE(*,*)'******* CURRENTLY SELECTED PARAMETERS ************************************	**************************************	READ(*,'(12)',END = 20,ERR = 10) IRESPON IF(IRESPON.EQ.0) THEN RETURN	201	202 WRITE(*,122) READ(*,122) READ(*,123)',END = 202, ERR = 202) FILEOUT	203 MRITE(* 123) READ(*, 1630)*, END = 203, ERR = 203) LIABIN
204 WRITE(*,124) READ(*,'(A30)',END = 204, ERR = 204) STOCKIN	205 ELSE JF (IRESPON.EQ.5) THEN WRITE(* 125) READ(*, '(A30)', EMD = 205, ERR = 205) ROWDIN	206 EL SE JF (IRESPON.EQ.6) THEN WRITE (*, 126) READ(*, *, END = 206, ERR = 206) WHSAVE	EL.E IF (IRESPON EQ.7) THEN WRITE (*, 127) READ(*, *, END = 207, ERR = 207) NSIMS	ELSE IF (IRESPON.EQ.8) THEN HRITE(*,128) READ(*,*,END = 208, ERR * 208) NSTOCKS	ELS: IF (IRESPON.EQ.S) THEN   IRITE = 129   IRONDS   IRAD = 209, ERR = 209) NBONDS	ELSI IF (IRESPON.EQ.10) THEN   F.	ELSE IF (IRESPON.EQ.11) THEN hRITE(*,131) READ(*,*,END = 211, ERR = 211) STOCKMIN	ELSE IF (IRESPON.EQ.12) THEN WITE(*,132) R.3D(*,*,END = 212, ERR = 212) YIMAX	ELSE IF (IRESPON.EQ.13) THEN WILTE (*,133) RIAD (*, *, END = 213, ERR = 213) SNAX	ELSE IF (IRESPON.EQ.14) THEN WITTE(*,134) READ(*,+,END = 214, ERR = 214) NSTAT	ELSE IF (IRESPON.EQ.15) THEN WRITE(*,135) READ(*,*,END = 215, ERR = 215) WRETS	ELSE IF (IRESPON.EQ.16) THEN WRITE(*,136) RE\D(*,*,END = 216, ERR = 216) BULLET

ELSE IF (IRESPON.Eq.17) THEN  READ(*,*,END = 217, ERR = 217) TARGET  ELSE IF (IRESPON.Eq.18) THEN  MRITE(*,*,END = 218, ERR = 218) TURN  END IF  GO TO 10  20 RETURN	FORMAT ( '0', AI )	OO ENTER OO ENTER ENTER	FORMATION ENTER MUMBER OF MONTHS TO SIMULATE FORMATION FORMATION ENTER NUMBER OF STOCKS FORMATION FORMATION FORMATION ENTER NUMBER OF STOCKS FORMATION ENTER NUMBER OF BONDS	FORMAT (** O. * ENTER MINIME FORMAT (** O. * ENTER MAXIME FORMAT (** O. * ENTER NSTAT (** O. * O. * O. * O. * O. * O. * ENTER NSTAT (** O. *	FORMAT ( 10 ; ) END	tertabbakatosabbab END OF SUBROUTINE MODIFY statesbesses tertabbabatosabbabababababababababababababababababa		* ** INSTRUCTIVE DISPLAYS SELECTED PARAMETERS FOR SPANNING RUN INCLUDE *COMMON.F*	WRITE(*, 100)	WRITE (*, 101) TILLE WRITE (*, 102) LIABIN WRITE (*, 104) STOCKIN
				***		***	************	NER USE		
BONDIN NISAVE NISAVE NISTINS NISODDS NISODDS STOCKNIN STAX SMAX SMAX SMAX SMAX SMAX SMAX SMAX SM		SPANNING RUN TITLE OUTPUT FILENAME LIABILITY STREAM FILE STRCK PETIUM FILE	BOND RETURN FILE MONTH TO BEGIN SIMULATION MUMBER OF MONTHS TO SIMULATE NUMBER OF STOCKS	9) NUMBER OF GONDS 5) STOCKS TO READ PAST () HINIMUM STOCK HOLDING () MAXIMUM SINGLE STOCK HOLDING () RAXIMUM SINGLE STOCK HOLDING () ATTAT	NRTS BULLET TARGET TURNOVER FACTOR	END OF SUBROUTINE DISPLAY	SUBROUTINE SAVOAT ************************************	AVE THE FILE FOR LATER USE	Ĭ.	',1 - 1,7) SAVING DATA TO FILE: PAST.DAT ',1 - 1,5)
MRITE(*, 105) WRITE(*, 106) WRITE(*, 109) WRITE(*, 110) WRITE(*, 111) WRITE(*, 111) WRITE(*, 1115) WRITE(*, 1115) WRITE(*, 1115) WRITE(*, 1115)	•	FORMAT(1X,	F DRMAT (1X, F DRM	10 FURMAT(1X, 9) 11 FURMAT(1X, 10) 12 FURMAT(1X, 12) 13 FURMAT(1X, 12) 14 FURMAT(1X, 13)	FCRMAT (1X, 15) FCRMAT (1X, 16) FORMAT (1X, 17) FORMAT (1X, 18)	END		** THIS ROUTINE SAVE THE FILE	INCLUDE COMPON.F	WF 1TE (*, 100) (*) WF 1TE (*, 100) (*)

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END OF SUBROUTINE SAVDAT
                                                                                                                                                                                                                                                                                                                                                                                                                                                              PURPOSE: TO PRINT A MENU AND READ RESPONSE
                                     CALL SPECIFICATIONS
CHARACTER OPTION(*)*(MAXTXT),HEADER*(MAXTXT),LAST*(MAXTXT)
INIEGER NBROPT,RESPON,LINES
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        SUBREUTINE QUADI (A.KT, RHS, COST, QUAD, INPUT, TOL, TITLE, PFILE
                                                                                                                                                                                                                                                                                                                                                                                                                                BLATK OUT REST OF SCREEN
DO 15 I = 1, IMAX
WRITE(*,*):
INTEGER MAXTXT
PARAMETER (MAXTXT = 50)
                                                                                             LO AL SPECIFICATIONS IN FEGER I, IMAX
                                                                                                                                                                                                                                                                                                                                 DO :0 I = 1,NBROPT
WRITE(*,*(1X,12,2H)
WRITE(*,*)OPTION(I)
CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                        WRITE(*,*) LAST
                                                                               ::
                                                                                                              ::
                         ::
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     30
$ $ $
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(KT(1)--1,0,+1 IF 1-TH CONSTRAINT IS .GE.,.EQ.,.LE.)
THE OBJECTIVE FUNCTION SHOULD BE CONVEX (CONCAVE)
FOR MINIMIZATION (MAXIMIZATION) PROBLEMS.
THIS MEANS THE SYMMETRIC MATRIX QUAD-QUADD [TRANSPOSE)
SHOULD BE NONNEGATIVE (NONPOSITIVE) DEFINITE
FOR MINIMIZATION (MAXIMIZATION) PROBLEMS.
                                                                                                                                                                                                                                                                                                                IN WHAT FOLLONS, MO - NO. OF CONSTRAINTS, NO - NO. OF VARIABLES, DIMENSION SIZES GIVEN ARE THE MINIMUM REQUIRED.
                     SUBROUTINE QUADPR FOR QUADRATIC PROGRAMMING PROGRAMS
                                                                                                                                                                                                                                          CALLING SEQUENCE ....
CALL QUADPR (A.KT.RHS, COST, QUAD, INPUT, TOL, TITLE, PFILE,
* 08J,X,RC,DUAL,SLK,IQUT,MS)
                                                            QUADPR MINIMIZES OR MAXIMIZES COST*X + SUBJECT TO A*X + KT**SLACK*
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         WORK SPACE ARRAY OF SIZE AT LEAST
2*(MO+NO)**2 + 12*(MO+NO) + 16 IF ANY EQUALITY CONSTRAINTS
ARE PRESENT OR 2*(MO+NO)**2 + 8*(MO+NO) + 6
IF ALL CONSTRAINTS ARE INEQUALITIES.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         INTEGER ROW, COL, INDX, MORE, P. P1, PSQ

COM GON (QPRCBI/ INPUTS(14), IOUTS(2), ROW, COL, INDX, MORE, P. P1, PSQ,

CALL, LENREQ, 101, 102, 103

EQUIVALENCE (INPUTS), M. M. (INPUTS(2), M.), (INPUTS(3), MO),

INPUTS(4), MO, (INPUTS(5), MINMAX), (INPUTS(6), LEMBS),

INPUTS(7), MAXIT, (INPUTS(8), MOBJ), (INPUTS(9), JIT),

INPUTS(13), JOATA), (INPUTS(11), JPEWGT), (INPUTS(12), JSOL),

INPUTS(13), JOATA), (INPUTS(14), JMIDTH),
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    TOLERANCE VECTOR OF SIZE 2 CONTAINING...
ROUND-OFF OR ZERO TOLERANCE. IF .LE. 0 RES
PIVOT TOLERANCE. IF .LE. 0 RESET TO 1.E-6
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    COMON /QPRCBR/ TOLS(2)
EQUIVALENCE (TOLS(1),TZERO), (TOLS(2),TPIV)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 IMFLICIT REAL (A-H,0-Z)
                                                                                                                            PFILE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      ξ
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OBJ, X, RC, DUAL, SLK, 10UT, WS)

```
OUTPUT UNITS BOR LINE PRINTER (TERMINAL) AND OUTPUT FILE DATA LUPRNT, LUFILE / 6, 92 /
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      SET OUTPUT UNITS AND OPEN PRINT FILE IF REQUIRED IF (JOUT .NE. 1 .AND. JOUT .NE. 2) GO TO 80 PFILES -
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      £q. 0) 60 TO 24
                                                                                                                                                                                                                                                                                                                                                                                                           TITLES(1:L1) - TITLE(1:L1)
DOUBLE PRECISION PIVOT COMMON /QPRCBD/ PIVOT
                                      CHARACTER*64 TITLES, COMMON /QPRCBC/ TITLES
                                                                              DATA NCALL / 0 /
                                                                                                                                                                                                                                                                                                                                                                  L1 - LEN(TITLE)
L1 - 30
                                                                                                                                                                                       INITIAL IZATIONS
                                                                                                         NCALL - 0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     20 CONTINU
22 CONTINU
MORE = (
60 TO 2
24 CONTINUI
MORE = )
26 CONTINUI
                                                                                                                                                                                                                                                                                                                             10 CONTI
                                                                                                                                                                                                                                                                                                                                                                                                                                                   NCALL, PFILES(1:L2)
5x, 'QUADPR CALL', 14
1x, '*** UNBLE TO OPEN THE FILE ', A)
72) NCALL
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                DPR', 14.4'. LIS', 52X)
.74) PFILES(1:12)
5X', OUTPUT WILL BE FILED ON ',A12)
                                                                            (1:1) .Eq. ' ') GO TO 30
                                                                                                    (12:12) - PFILE(1:1)
                                                                                                                                                                                                                                                                                                                                                        102 - JUPRNT
GO TO 10
CANNOT OPEN FILE. MAKE ONE UP.
CONTINIE
                                                                                                                                                                                                                                                                                                             EQ. 1) GO TO 50
                                                                                                                                                                                                                                                                                                                                                                                                                      (L3 .Eq. 1) 60 TO 76
                                                                                                                   30 CONTINE
                                                                                                                                                                                                                                                                                                                                                                                                                                                             70 FORMAT
                                    822
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            78 F0
                                                                                                                                                                                                                                                                                                                                                     20
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    92
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            74
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  8
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OUTPUT PROBLEM PARAMETERS AND PROBLEM DATA IF REQUESTED.
IF (JIT .NE. 0) CALL GRPRT1
IF (JDATA .NE. 0) CALL GRPRT2 (A,ML,KT,RHS,COST,QUAD,NL)
                                                                                                                                                                                                                                                                                                                                                                                                            OUTPUT HEADER FOR INTERNEDIATE OUTPUT, IF ANY EXPECTED IF (JPIVOT .NE. 0) CALL QRPRT3
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               GET SOLUTION AND OBJECTIVE VALUE IF REQUESTED.
CALL QDSOLN (KT.COST.QUAD.NL,WS,P,WS(L4),X,RC,DUAL,SLK,
WS(L1),OBJ)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                       CONSTRUCT INITIAL TABLEAU FOR QUADRATIC PROGRAMMING.
CALL QDPREP (A,ML,KT,RHS,COST,QUAD,NL,WS,P)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              OUTPUT SOLUTION REPORT IF REQUESTED.
IF (JSOL .NE. 0) CALL QRPRT6 (X,RC,DUAL,SLK,OBJ)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   PERFORM PRINCIPAL PIVOTING TO FINAL TABLEAU.
CALL QDCOMP (MS,WS(L1),WS(L2),WS(L3),WS(L4))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                CLOSE PRINT FILE IF REQUIRED.
IF (JOUT .GT. 0) CLOSE (LUFILE,STATUS-'KEEP')
                                                                                                                                                                                                    CHECK INPUT DATA PARAMETERS FOR CONSISTENCY CALL QDRVER (KT)
                                                                                                                                                                                                                                                               IF (IERR .EQ. 5) 60 TO 200 QUIT IF BAD VALUES (IERR = 5)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    CHECK INPUT DATA FOR QUADPR
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         SET EXIT VALUES, 10UT.
CONTINUE
10UT(1) - IERR
10UT(2) - ITCNT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           SUBROUTINE QDRVER (KT)
103 - LUPRNT
90 CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           RETURN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 200
                                        ںں
                                                                                                        IOUTS(2), ROM, COL, INDX, MORE, P, P1, PSQ,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         KT CONTAINS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            I ILLEGAL VALUES IN KT.
                                                                                                                                                                                                                                                                                       COMION /QPRCBR/ TOLS(2)
EQU:VALENCE (TOLS(1),TZERO), (TOLS(2),TPIV)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    CONTINUE
ERROR: 1) = (NO .LT. 0 .OR. NO .GT. NL)
ERROR: 2) = (NO .LT. 1 .OR. NO .GT. NL)
                                                                                                                                                                                  INPUTS(10), JDATA), (INPUT INPUTS(10), JDATA), (INPUT INPUTS(13), JOUT), (INPUTS(13), IERR), (IOUTS(2)
                                                                                                                                                                                                                                                                                                                                                INTIGER ZERONE(4), ZERO12(3)
LOG: CAL ERROR(10)
DATA ZERONE / 5,8,9,11 /
DATA ZERO12 / 10,12,13 /
                       IMILICIT REAL (A-H,0-Z)
DIPENSION KT(1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     HIDIM
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             ITITLE - 0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     CHECK KT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         20 CONTINU
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  30
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```
CONSTRUCT THE INITIAL TABLEAU FOR QUADRATIC PROGRAMMING.
IT HAS THE FORM
                                         ERONE(1)
(1+3) = (INPUTS(J) .NE. 0 .AND. INPUTS(J) .NE. 1)
                                                                                                          | = ZERĞİZ[1)
|- REROR(1+7) = (INPUTS(J) .LT. 0 .OR. INPUTS(J) .GT. 2)
                                                                                                                                                                                                                                                                                                                                                                                                                       ISTIVE OR EXCEEDS INPUT(2)"
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         SUBROUTINE QDPREP (A.LDA,KT,RHS,COST,QUAD,LDQ,B,LDB)
                                                                                                                                                                                                                                                                                                                                                                                     IE OR EXCEEDS INPUT(1)")
                                                                                                                                                                                                                                                                                                                                                                                                                                                     EQ
FOR THIS PROBLEM,"
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     47 CONTINUE
48 FORMAT (5x, INPUT(',12,') NOT 0, 1, OR 2')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      5X, 'INPUT(',12,') NOT 0 OR 1')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              ROR(1+1) WRITE (101,48) J
(LENWS .LT. LENREQ)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       SO CONTINUE
RETURN
                                                                            33
                                                                                                                                                                                   DOUBL: PRECISION 8
'DIMEN SION A(LDA,1),KT(1),RHS(1),COST(1),QUAD(LDQ,1),B(LDB,1)
                                                                                                 MHERE A', RHS', COST', QUAD' ARE OBTAINED FROM A, RHS, COST
CONVEXTING THE PROBLEM TO MINIMIZATION WITH ALL .GE. C
                                                                                                                                                                                                                                                                                                                                                                                                                                      FILL IOVER TRIANGLE OF [1] AND [3]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                         EQ. 1) 60 TO
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          éó 70 110
                                                                                                                                               IMPLI:IT REAL (A-H,0-Z)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       ...
80
80
80
80
80
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 30
```

```
S, EXPRESS AS R+1 .GE. CONSTRAINTS, OF THE OTHERS.
     S CONTINUE - QUAD(K,L) - QUAD(L,K)
                                                                                                                                                                            CHECK FOR CASE OF NO CONSTRAINTS.
CONTINUE
IF (MO .EQ. 0) GO TO 240
                                                                                                                                                                                                                                                                                                                                                                                                                                                      .LT. 0) GO TO 170
.GT. 0) GO TO 190
RAINT
                                                                        FILL UPPER TRAINGLE OF [1].
CONTINUE
DO 100 L = 2, NO
                                                                                                                                           90 CONTINUE
                                                                                                                                                                                                                                                                                120 CONTINUE
                                                                                                                                                                                 110 č
                                                                                                                                                                                                                                                                                                                                                                                          150
                                                                                     8
                                                                                                                                                                                                                                                                                                                                                                         140
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            160
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  170
                                                                                                                                                                                                                                                                                                                                                                                                               ROW, COL, INDX, P.P1, PSQ
PRCBI/ INPUTS(14), 10UTS(2), ROW, COL, INDX, MORE, P.P1, PSQ,
                                                                                                                                                                                                                                                                                                         COMPUTE THE FINAL TABLEAU FOR QUADRATIC PROGRAMMING GIVEN THE INITIAL TABLEAU USING THE METHOD OF PRINCIPAL PIVOTING
                                                                                                                                                                                                                                                                                                                                                                DOUILE PRECISION B,TEMP,U
INTIGER JZ,JW
DIMINSION B(1),TEMP(1),U(1),JZ(1),JW(1)
                                                                                                                                                                                                                                                                                     SUBROUTINE QDCOMP (B, TEMP, U, JZ, JW)
                     B(K, P1) = - RHS(1)

GO TO 210

-LE. CONSTRAINT

CONTINUE

DO 200 L = 1, NO

B(K, L) = - A(1, L)
                                                                                                                                                                                                                                                                                                                                           IMP.ICIT REAL (A-H,0-Z)
CONTINUE - A(1,L)
                                                                                                 210 CCNTINUE
                                                                                                                                     FILL [2].
D0 230 [
D0 220
                                                                                                                                                                                   220 CONTI
                                                     190
                                                                                          200
           180
                                                                                                                                                                                                                                240
```

```
] = 1, P
= 13 + 1
(B(13) .LT. (-TZERO)) ITEMP = 1TEMP + 1
                      THEN THE DRIVING VARIABLE
                                                                                                                                    IF (B(KJ)) 130, 140, 130

BOM = J

BOT 150

BOT = -BST / B(KJ)

I: (BST - LE. BS) GO TO 140

B; = BST
                                                                                                                                 140 CONT
```

.GE. 2) GO TO 230

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IF (JFLAG .EQ. 1) GO TO 290

JFLAG = 1

C*****EXCHANGE ROWS AND COLUMNS FOR COMPLEMENTARITY

Z30 LLL = 0
                                                                                                                                                                                                                                                                                     K = IABS(JW(I))
IF (K EQ. I) 60 TO 250
IJ = K
KJ = I
DO 240 J = 1. P1
   101 FORMAT('+', A50, 15)
                                                                                                                                                                                                                                                                                                                                                                                                                250
                                                                                                                                                              290 ROLL LL LL LL L TCNT + 1

C****ATLEMPT TO PROGRESSIVELY RELAX THE CONVERGENCE PARAMETER
                                                                                                                                                                                             C TFIV = TPIV + TOLS(2)/50.
C****INDICATE THE NUMBER OF ITERATIONS
WRITE(*,101)'OPTIMIZATION ITERATION
                                    TO 280
                                                                                                                                                       .GE. 2) GO TO 260
                                                                                                                                                                                                                                            C*****NORIJAL TERMINATION
300 IERI: - 1
GO 10 600
C****EXCHANGE COLUMNS
260 LLL 0
D3 280 J = 1, P
                                                                                                                                                                                                                                                                                   C****ERRCR TERMINATION
                                                                                                                                                                                                                                                                                           400 K = 1
IERR = 6
GO TO 460
                                                                                                                                               280 COLITI
1F (L
290 ROL
                                                                                                         270
                                                                                                                                                                                                                                                                                                                       410
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NORMAL JORDAN PIVOT.
IN SAVE MEMORY BY USING THE ELEMENTARY MATRIX.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               RACK OF BASIC AND NONBASIC VARIABLES
                                                                                                                                                                                                                                                                                                       LL COLUMNS EXCEPT PIVOT COLUMN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  PUTE NEW PIVOT ELEMENT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      - -TEMP(1)
                                                                                                                                                                                                                                                    - 32(cor)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    560 CONTINU
C****COMPUTE
                                                                                                                                                                                                                510 CONTINUE
13 - RC
10 - S20 1
10 - 13 1
                                                           RETURN SOLUTION TO QUADRATIC PROGRAMNING PROBLEM FROM FINAL TABLEAU AND COMPUTE OBJECTIVE VALUE IF REQUESTED. CONVERTING THE PROBLEM TO MINIMIZATION WITH ALL .GE. CONSTRAINTS.
                                                                                                                                                       DOUBLE PRECISION B, TEMP
DIMENSION KT(1), COST(1), QUAD(LDQ,1), B(LDB,1), JW(1), X(1), RC(1),
DLAL(1), SLK(1), TEMP(1)
                                                                                                                                                                                                                  NDX, WORE, P. P1, PSQ
PUTS(14), TOUTS(2), ROW, COL, INDX, WORE, P. P1, PSQ,
         SUBRCUTINE QDSOLN (KT.COST,QUAD,LDQ,B,LDB,JW,X,RC,DUAL,SLK,
TIMP,OBJ)
                                                                                                                                                                                                                                                                                                                                                                       COMMON /QPRCBR/ TOLS(2)
EQUIN NLENCE (TOLS(1),TZERO), (TOLS(2),TPIV)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               . 0) GO TO 150
. NO) GO TO 130
                                                                                                                                                                                                                                                                                                                                                                                                                    DOUBL: PRECISION DART, BB
                                                                                                                         IMPLICIT REAL (A-H, 0-Z)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    120 CONTI (I
DART -
DO 17)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         110 CONT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 8
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               130
```

```
COMPUTE OBJECTIVE VALUE ONLY IF REQUESTED. CONTINUE IF (KOBJ .EQ. 0) GO TO 250 OBJ = 0.000 TEMP(1) = 0.000
 K = J - NO
IF (K : Eq. KART) GO TO 140
DUAL(K) = BB
GO TO 170
140 CONTINUE
DART = BB
GO TO 170
150 CONTINUE
IF (J : GT. NO) GO TO 160
RC(J) = RB
GO TO 170
160 CONTINUE
K = J - NO
IF (K : Eq. KART) GO TO 170
IF (K : Eq. KART) GO TO 170
IF (K : Eq. KART)
                                                                                                                                                                                         ADJUST DUALS IF ANY EQUALITIES
IF (MORE .EQ. 0) GO TO 200
DO 190 I = 1, MO
                                                                                                                                                                                                                                                                                                                                                                                        210 CONTINUE CONTINUE CONTINUE CONTINUE CONTINUE CC. FINISHED
                                                                                                                                                                                                                                                                          DUAL(I) - DART - DUAL(I)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     200 C
                                                                                                                                                                                                                                                                 180
SUIROUTINE QSET(NUM, MAXWS, ITURN)
                 INCLUDE 'COMMON.F'
INCLUDE 'COMMON,F'
REAL QC(NDID,ND),QRHS(NDID),QTOL(2),QRC(ND),DZX(ND),XOLD(ND),
QDUAL(NDID),QSLK(NDID),QMS(ISIZEQ)
                                                             INTEGER QKT(NDID), INPUT(14), QIOUT(2), NUM, MAXWS
CHARACTER*30 PFILE
                                                                                                                                                                                                                                           GRHS(1) - D(1-NUM)
                                                                                          DO 10 I = 1,10
DO 10 J = 1,NUM
QC(I+NUM,J)-C(J,I)
CONTINUE
                                                                                                                                            DO :0 1 = 1,NUM
DO :0 3 = 1,NUM
F(1.EQ.3) THEN
G(11,3) = -1.0
IND IF
CON'IND
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     QTOL(2) - 0.000001
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         QTOL(2) = 0.0001
                                                                                                                                                                                                                                                                                               END IF
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 QTOL(1) - 0.0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          . E-4
. E-4
                                                                                                                           2
                                                                                                                                                                                                                        20
                                                                                                                                                                                                                                                                                                                    30
```

- TURN\*ABS(X(1)-OLDNT(1))

9

WRITE(\*,'(1X,A12,F9.3)')'TURN OVER = ',DXTOTAL\*50. '

IF {ABS(DXTOTAL-DXLAST).GT. 0.01 .OR. ITURN .LT. 1) THEN

ITURN = ITURN + 1

DXLAST = DXTOTAL

GO TO SOO

FIND IF

TURN = 0.0

22

```
C *** PARAMETERS ARE USED TO DIMENSION THE COMMON ARRAYS
   C *** IN EACH SUBROUTINE.
  [ ***
              ND - TOTAL NUMBER OF STOCK WEIGHTS BEING COMPUTED.
  C ***
             ID - THE MAXIMUM NUMBER OF CONSTRAINT EQUATIONS.
N2D - THE DIMENSION ON WORKING AREAS ( 2 * ND )
  C ***
  C ***
             KEQ - NUMBER OF CONSTRAINTS WHICH WILL BE EQUALITIES
  ( ***
             NRT = NUMBER OF RETURNS
  C ***
             NST = USED FOR STATISTICS
  [ ***
             ISIZEQ = 2 * (ND*2 + ID)**2 + 8*(ND*2+ID) +6
  ( ***
             NDID = ND + ID
  [ ****<del>*</del>
             FOR CASH RUNS (AT LEAST 1 EQ CONST. )

ISIZEQ = 2 * ( ND*2 + ID )**2 + 12*(ND*2+ID) +16
  C ***
  ( ***
             NDID = ND + ID
 LAST UPDATED: November 19, 1988
          IMPLICIT REAL (A-H,O-Z)
          IMPLICIT INTEGER (I-N)
          PARAMETER (KEQ = 0)
 C 280
          PARAMETER (ND = 280, ID = 6 , N2D = 560)
PARAMETER (NDID = 286, ISIZEQ = 645246)
 C
    250
         PARAMETER (ND = 250, ID = 6 , N2D = 500)
PARAMETER (NDID = 256, ISIZEQ = 516126)
   100
 C
         PARAMETER (ND = 100, ID = 6, N2D = 200)
PARAMETER (NDID = 106, ISIZEQ = 86526)
         PARAMETER (NRT = 48, NST = 3)
PARAMETER (LENGTH = 40)
         CHARACTER* (LENGTH) FILEOUT, TITLE, NAME (ND), PORTRETS, GARB, ANSWER,
                         OLD, LIANAME, LIABIN, STOCKIN, BONDIN, IDC (ND), SIC (99)
        COMMON /ARRY/ A(ND,ND),C(ND,ID)
COMMON /VECT/ B(ND),D(ID),BDL(ND),BDU(ND),X(ND),OLDWT(ND)
COMMON /RETS/ RET(NRT,ND),ANIM(NRT),PRET(NRT),ISIC(ND),AVE(ND)
COMMON /TRAC/ COV(NST,NST),STAT(NRT,NST),COREL(NRT,NST)
COMMON /TRA2/ PRICE(ND),VOL(ND),CUM(ND),VAR(3),LIANAME,TITLE
COMMON /RTNIN/FILEOUT,LIABIN,STOCKIN,BONDIN,IDC,NAME,SIC
COMMON /DAT/ NMSAVE NM NSIMS NSTOCKS.NBONDS.NSTAT.NRETS,IDUMM
        COMMON /DAT/ NMSAVE, NM, NSIMS, NSTOCKS, NBONDS, NSTAT, NRETS, IDUMMY,
                             IHOLD
        COMMON /MAX/ STOCKMIN, YIMAX, SMAX, SCALE, BRET, XFACTOR, XBUPPER,
                  XBLOWER, BULLET, TARGET, TURN, BULL1, TARG1, TURN1, PORTVAL
E END OF COMMON.F
```

WO 91/02326 PCT/US90/04328

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# APPENDIX II

# LIABILITY RETURN PROGRAM

To create a return series for a liability stream from yields.

(Appendix II pp. 1-2)

```
LIABILITY RETURN PROGRAM
AUTHOR JOE DADA III
LAST UPDATE 3-21-88
COPYWRITE 1988 NATIONAL INVESTMENT SERVICES OF AMERICA INC.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          HIS SECTION TO BE REMOVED AND BY SUB INTRO
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         CALL SUBS TO GET INPUT DATA
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 WRITE(*, $1500) GARB
IF(GARB.EQ.'Y'.OR.GARB.EQ.'y') THEN
OLDOUT-1
WRITE(*,*)' ENTER NAME OF OLD RETURN FILE'
READ(*,1500) OLDO!
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            (*,*)' ENTER LIABILITY STREAM FILENAME'

(*,*)' ENTER NEW OUTPUT FILENAME'

(*,*)' ETTOUT

(*,*)' RETOUT', RETOUT

(*,*)' ENTER YIELD TO MATURITY FILENAME'

*,1500)YIELDS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     ITYPE-1,A80;-2,PB0
                                                                                                                                                                                                                                                                                                                                                                                                                        PROGRAM SPANRATE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      OLDOUT-0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    SINCLUDE: 'RATE.FOR'
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        UPDATE RETURN FILE CHECK YIELDS FILE*
                                                                                                                                                                                                                                                                                                                                                                                                                                                                               OPEN (.O, FILE-RETOUT, STATUS-'NEW')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                               1F(OLDUUT.EQ.1)THEN
OPIN (8,FILE-OLDFILE)
RE/D(8,1500)TITLE
RE/D(8,1500)GARB
RE/D(8,1500)GA
READ(11,1500)GARB
READ(11,1500)GARB
READ(11,17)IYLD2
D0 333 I-1YLD1,IYLD2
D0 333 I-1YLD1,IYLD2
CONTINIE
CLOSE (11)
```

```
IF OLDFILE EXIST CHECK LAST RETURN IN IT
VERSUS NEW CALC TO CHECK PARAMETERS
                                                                                                                                                                                                                                                                           FORMAT(A10,14,4X,F17.0,4X,F13.0,4X,F10.6,3X,F5.2)
FORMAT(A40)
FORMAT(F13.10,2F15.0,14,3X,F5.2)
                                                                                                               NYEARS=1-1
MHONTHS=NYEARS*12
IF(NYEARS.GT.90)THEN
WRITE(*,*)' ERROR LIA STREAM HAS TOO MANY YRS 90 IS MAX'
STOP
ENDIF
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            SKIP TO END OF LOOP FIRST TIME THROUGH IF (FRI.EQ.O)GO TO 100 PROD IS DENOMINATOR TO CONV FUTURE TO PV
                                                                                                                                                                                                                CALCULATE MONTHLY YIELDS AND SLIDE OLD YIELD BACK TO BEG OF MONTH
                                                                                                                                                                                                                                                                                                                                                                                             | ISTART=IYLD1
| ENDIF
| ICHECK=ISTART+1
| DO 100 | ISTART-IYLD2
| WITE(* *)'I', I, 'YLD', YTH(1)
| FRI=FR
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               FR-(1+YTM(1))**(0.083333)-1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         PV1=0.0
PV2=0.0
PR0D1=1.0
PR0D2=1.0
DUR=0
DO 300 J=1,NYEARS
DO 300 L=1,12
PR0D1=PR0D1=
                                                                                                                                                                                                                                                                              DO 222 I-1 NYEARS
XLIA(I)-XLIA(I)/12
CONTINUE
                                                                                                                                                                                                                                                                                                                                               IF (OLDOUT.EQ.1)THEN
ISTART-IRET2-1
ELSE
                                                 READ(CONTINUE CLOSE(9)
                                                                 448
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                300
```

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## APPENDIX III

### CORRELATION PORTFOLIO PROGRAM

To create an optimal index correlation portfolio with securities.

(Appendix III pp. 1-30)

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C UPDATED December 6, 1988 C sassabatates transfer of the contract of the cont	INCLUDE 'COMSUC.F' LOGICAL ICOUNT DATA INPUT SECTION ************************************	5 CONTINUE C DEFAULT READ IN OF 24 MONTHS PRIOR = NSTAT, NRESTS FOR B() **** NSTAT = 24		C ***************** CALL FLASH TO INTRODUCE S P A N **** CALL FLASH	C ********* IF 'COUNTS' EXISTS THIS IS A MULTIPLE RUN **** INQUIRE (FILE * 'COUNTS', EXIST * ICOUNT) IF (ICOUNT EDV. FALSE.) THEN	C ***************** CALL INTRO TO INPUT PARAMETERS **** CALL INTRO CALL MANAGEMENT CALL MODIFY TO CHANGE PARAMETERS ****. CALL MODIFY	C ************************************	CALL SAVDAT	NH = NMSAVE NH = (INT(NM/100)-80)*12+(NM-INT(NM/100)*100) IREAD = NSTAT+NSIMS IF(NSTOCKS.GT.0)THEN XBUPPER = SMAX
END IF C************************************	NUM = N:TOCKS+NBONDS IF(NUM.ii.ND)THEN WRI'E(*,*)' WARNING NUM >',ND,' TOO BIG FOR PROGRAM' STO! END!F	ICOL = ID KE = KEI KX = KI IX = MI ICC = MI	IH = NZf. IFIRST - NM-NSTAT ILAST - NM-NSIMS-1 BULLI - BULLET TARGI - TARGET TURNI - TURN	BULLET - BULLET*ABS(BULLET)/1000. 1F (TURN).EQ.100.)THEN TURN = 0.0	ELSE ELSE END 1F ************************************		HRITE(*, 101) CALLING MATRIX CALCULATE INPUT ARRAYS * CALL MATRIX (WW, IREAD)	WRITE(*, 101)'CALLING BOUNDS 'CALL BOU'US (NUM, ICOL, MEW)	WRITE(*,  01)'CALLING OPTIMIZER ** ' IF (ICOUTT.EQV. TRUE.) THEN WRITE(*, 102)'WORKING ON RUN NUMBER ', ISKIP END IF

MAXWS = 2*(2*NUM+ID)*(2*NUM+ID)+8*(2*NUM+ID)+6  ITURN = 0  CALL QET ( NUM, MAXWS, ITURN )  C ******** IF TURNOVER IS CONSIDERED, CALL TURNOV  IF(TURN GT.0) THEN  ITURN = 1  CALL QSET (NUM, MAXWS, ITURN)  END IF	C ************************************	: :	100 WRITE(*,101)'SPANNING SIMULATION COMPLETE'  IF (1COUNT.EQV., TRUE.) THEN WRITE(*,102)'DONE WITH RUN NUMBER ',1SKIP  GO TO 5  END IF  101 FORMAT(*+,*A50,17)  102 FORMAT(*+,*A50,17)	*	INCLUDE 'COMSUC.F' CHARACTER*30 XTITL,XFLOUT,XLIBIN,XSTKIN,XBNDIN OPEN (13,FILE ='MULTIN',STATUS = 'OLD') IF (ISKIP.EQ.O) GO TO 30 DO 10 1 = 1, ISKIP
20 3 - 1, NTÍNUÉ NUÉ NUÉ NUÉ NUÉ 3 101, END 3 101, END 3 101, END 3 101, END 8 101, END 8 100 - END	~~~~~	(A20)	CLOSI:(13) RETUIN C **** STOP DONE WITH MULTI RUN ***********************************	**************************************	CHARATER 12 HOLD CHARATER 12 HOLD CHARATER 12 HOLD CHARATER HOLD IS READ FROM FIRST SCREEN RESPONSE: OLD OR HOLDINGS RUN ** IF (IHOLD .Eq. 0) GO TO 999  NRITE(*,*)'INPUT PORTFOLIO #, AND NAME OF HOLDINGS FILE'

```
EQ. D) THEN .*). PORTFOLIO NUMBER NOT FOUND ', IPORT
                                              OPEN (25, FILE - HOLD, STATUS - 'OLD')
                                                                                                                                                                                                                                                                                             25, *, END = 44) GARB
                                                                               XPORT - REAL (1PORT)
                                                                                                                                                                                                                                                                                                                                                         CONTINUE
NIDC = 1
IF (NIDC :E
WRITE(*)
GO TO 11
END 1F
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           THIS SUBROUTINE READS IN STOCK, BOND & LIA DATA *****
                                                                                                                                                                                                                                 IF (ID:TEST.EQ.1) THEN HALL, SYMBOLS NOT FOUND. PROGRAM STOPPING'
                                                                                                                                                     | TEST = 1
| TE(*,*)IDCSYM(1); : SYMBOL NOT INCLUDED IN RETURN FILE'
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        C ************** READ IN LIABILITY RETURNS *************
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           IFIRST IS FIRST MONTH OF DATA NEEDED FOR MATRIX
ILAST IS LAST MONTH OF SIMULATION
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               END OF SUBROUTINE HOLDING
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             SUBROUTINE COVIN (NUM, IREAD, IFIRST, ILAST)
                              (3)(1:4) .Eq. 1DCSYM(1)) THEN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             OPEN (9, FILE - LIABIN, STATUS - 'OLD')
                                                                                                                                 EQ: 0) THEN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               READ (9,111) LIANAME
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                INCLUDE 'COMSUC.F'
                                                                                                                                                                                                                                                                                                                                                      OPEN(21, F11
DO 90 1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  UPDATE 8/9/88
                                                                                                                                                                                                                                                                                                                                                        666
                                                                                                                                                                                                                                                                                                                                                                                                                                       8
```

```
READ IN STOCK DATA
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                CUT OUT BLANKS FROM GARB TO GET AN IDC AND TICKER
READ (4,111) GARB
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       ---GARB(1:LENGTH) - NAME(1)(1LEN:LENGTH)
END 1F
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               WRITE (* 112) I.NAME(!)
FORMAT('+','STOCK # ',15,' IS ',A3O)
READ (4,111) GARB
                                                                                                                                                                                                                                        IF (NSTOCKS.GT.0) THEN OPEN (4,FILE - STOCKIN, STATUS - 'OLD')
                                                                                                                                                                                                                                                                                                                                                                                                                                          C **** CUT OFF LEADING BLANKS OF NAME(1)
11EN = 1
GARB = .
790 IF (LILEN: ILEN) . Eq. '') THEN
11EN = 1 LEN+1
GO TO 790
                                                                                                                                                                                                                                                                                                                                                                                                       DO 700 I = 1,NSTOCKS
READ (4,111,END = 785) NAME(I)
                                                                                                 DO 300 1 - 1, IFIRST-ISTART
READ (9,111) GARB
CONTINUE
                                                                                                                                                                                                                         ASTOCKS, GT. ...

OPEN (4,FILE - ...

DO 600 I = 1,IDUMMY

READ (4,*) ISTP

READ (4,*) ISTP

READ (4,*) ISTP

READ (4,*)

CONTINUE

600

CONTINUE

1111 FORMAT (A30)

DO 700 7
  WRITE(*,*)LIANAME
DO 200 I = 1,5
READ (9,111) GARB
CONTINUE
                                                                                                                                                 DO 400 I - 1,1READ
READ (9.4) ANIM(1)
CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         NAME(I) - GARB
                                                             READ (9,*) ISTART READ (9,*) ISTOP
                                                                                                                                                                                                   CLOSE(9)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 **** ]
                                       200
                                                                                                                           300
                                                                                                                                                                             400
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               112
                                                                                                                                                                                                                                                                                                                      READ (4.*) ISIC(1)
IF(ISIC(1), 61.99) ISIC(1) = INT (ISIC(1)/100)
READ (4.11) (GARB.L = 4.5)
READ (4.*) ISTOP
READ (4.*) ISTOP
                                                                                                                                                                                                                                                                                                                                               ICHECK = NM-NRETS-1START
|F(ICHECK.LT.0) NRETS = NM - ISTART
|F(NRETS.LT.NSTAT) ICHECK = IFIRST-ISTART
1F (GARB(ILEN:11EN).EQ. ") THEN ILEN + 1 IF (ILEN + 3).GT.LENGTH) GOTO 793
                                                                                             | DC(1)(1:4) = GARB(1LEN:1LEN+3)
                                                                                                                                                                                  ENDIF
1)C(1)(6:9) - GARB(1LEN:1LEN+3)
                                                                                                                                                                                                                                                                                                                                                                                                                                                 DO 801 J = 1,NRETS-NSTAT
READ(4,*)GARB
CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                 DO 800 J = 1, ICHECK
READ (4,111) GARB
CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            DO 810 K = 1, IREAD
READ (4,*) RET(K,1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   JJ - NRETS-NSTAT
                                                                                                                                                                                                                     CONTINUE
                                                                                                                                                                                                                                                                                                                      ***** 3
                      791
                                                                                                                                 792
                                                                                                                                                                                                                      793
                                                                                                                                                                                                                                                                                                                                                                                                                       800
                                                                                                                                                                                                                                                                                                                                                                                                                                                                         801
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              810
```

DO 1200 J = 1,1STDP-1LAST READ (4,111) GARB CONTINUE RND1F CONTINUE CONTINUE READ IN BOND DATA	IF (NBONDS.GI.0) THEN OPEN (7; FILE = BONDIN, STATUS = '0LD')  DO 900 I = NSTOCKS+1 NSTOCKS+NBONDS  DO 900 I = NSTOCKS+1 NSTOCKS+NBONDS  READ (7,113) I NAME(1)  READ (7,113) GARB,L = 1.5)  READ (7,1) STOP  FORMAT(1,1,150ND 0.15,15,15,15)  FORMAT(1,1,150ND 0.15,15,15)  TEST ICHECK FOR ENOUGH RETURNS FOR BRET  FORMAT(1,1,150ND 0.15,15)  TEST ICHECK = NM-NRETS-ISTART  FORMAT(1,10) THEN	•	DO 1010 K = 1, 1READ READ (7,*) RET(K,1) J = 33 + K CONTINUE DO 1300 J = 1, 1STOP-1LAST DO CONTINUE GENDIE
85 NSTOCIS = I-1 READ OF FILE WAS HIT ON STOCKS - RESET NUM AND CONTINUE *** DO 1200 J = 1,15 READ (4,111) NUM = NSTOCKS+NBONDS GOTO 1400  END  END  END  CONTINUE  END  CONTINUE  END  CONTINUE  CLOSE(4)	13 90 90 13	UANIM = 0.  UANIM = 1.NSTAT  DO 12: 1 = 1.NSTAT  END 1 = 1.NSTAT  CONTINUE  END 3 = 1.1CH  DO 13C I = 1.NUM  ELAD (7.111)  ELAD 1 = 1.NUM  ELAD (7.111)  1000 CONTINUE  DO 1001 3 = 1.NRE  EMD 3 = 3.NSTAT  DO 1001 3 = 1.NRE  EMD 3 = 3.NSTAT  EMD 3 = 3.NSTAT  DO 1001 3 = 1.NRE  EMD 7 = 1.NRE  EMD 7 = 1.NRE  CONTINUE  CONTINUE  END 7 = 1.NRE  CONTINUE  NRETS-NSTAT	TO USE SIGNA DIFF 1010 1300 *** TARGET 900 CON

```
DO 51 J = 1,1COL

DO 52 1 = 1,NUM

C(11,3) = 0.0

IF (3.Eq. 2) C(1,3) = 1.0

IF (3.Eq. 2) C(1,3) = 1.0

IF (3.Eq. 3) C(1,3) = 1.0

IF (3.Eq. 4.ND 151C(1) Eq. 49) C(1,3) = -1

IF (3.Eq. 5.ND 151C(1) Eq. 49) C(1,3) = -1

IF (3.Eq. 5.ND 151C(1) Eq. 49) C(1,3) = -1

IF (3.Eq. 5.ND 151C(1) Eq. 49) C(1,3) = -1

IF (3.Eq. 5.ND 151C(1) Eq. 60) C(1,3) = -1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                  SIC60S = SIC60+SIC63+SIC67
IF(SIC49*100.GI.YIMAX.AND.SIC49*100.LI.SCAL*YIMAX)D(4)
IF(SIC60S*100.GI.YIMAX.AND.SIC60S*100.LI.SCAL*YIMAX)D(6)
IF(SIC67*100.GI.YIMAX.AND.SIC67*100.LI.SCAL*YIMAX)D(6)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        IF SIC69*100.6T.SCAL*VIMAX) D(4) - D(4)*SCAL
IF SIC60S*100.6T.SCAL*VIMAX) D(5) - D(5)*SCAL
IF SIC67*100.6T.SCAL*VIMAX) D(6) - D(6)*SCAL
                                                                                                                                                                                                                                   END 1F
1F (1.61.NSTOCKS) BDU(1) = 1.
                                                                                                                                                                                      ELSE
BDU(1) = OLDWT(1)
END 1F
                                                                                                                                                                                                                                                                    IF (1SIC(1) . EQ. 48) $
IF (1SIC(1) . EQ. 49) $
IF (1SIC(1) . EQ. 63) $
IF (1SIC(1) . EQ. 63) $
CONTINUE
SCAL = 1.25
S1C49 = 0.0
S1C60 = 0.0
S1C63 = 0.0
S1C67 = 0.0
                                                                                                                                                                                                                                                                                                                                                                               200000
200400
                                                                                                   DO 80 1 - 80L(1) 80U(1) 1F(0L0
                                                                                                                                                                                                                                                                                                                                                       8
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                END OF SUBROUTINE HATRIX

SUBROUTINE BOUNDS (NUM, ICOL, WEW)
                                                                                                                                                                                                                                                                                                                                                                                                                                                      ********
                                                                                                                                                                                                                                                                                                                                                             A(1,3) - A(1,3)+(TEMPI-AVE(1)*3.)*(TEMPJ-AVE(3)*3.) / XXX
                                                                                                                                                                                                                                                                                                                    TEMPI = {1+RET(K,1)}*{1+RET(K-1,1)}*{1+RET(K-2,1)}-1.0
TEMPJ = {1+RET(K,3)}*{1+RET(K-1,3)}*{1+RET(K-2,3)}-1.0
                                                                                                                                                                                                                                                                                                                                                                                                            1F(A(1,3).GT.50)WRITE(*,*)'COV TOO BIG',A(1,3),1,3
                                                                                                                                                                    *********
                                             TURN IS USED TO ADJUST IMPORTANCE OF DELTA X
                                                                     DO 213 I = 1.NUM
AVE(1) = 0.0
DO 214 J = 1.NSTAT
AVE(1) = AVE(1)+RET(J,1)/DBLE(NSTAT)
CONTINUE
                                                                                                                                                                                                                       XXX = DBLE(NSTAT-1)

XXX = DBLE(NSTAT-1)

DO 215 1 = 1,NUM

DO 215 J = 1,NUM

A(1,3) = 0

A(1,3) = 0

A(1,3) = 0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           INCLUDE 'COMSUC.F'
                                                                                                                                                                                                                                                                                                                                                                                                          A(3,1) = A(1,3)
                  CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 RETURN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         387
```

IF (J.Eq.5.AND.ISIC(I).Eq.67) C(I.J) = -1.0 IF (J.Eq.6.AND.ISIC(I).Eq.67) C(I.J) = -1.0	52 CONTINUE 51 CONTINUE	C C10SE (6)	MATA = 2*NUM+ICOL	RETURN	C END OF SUBROUTINE BOUNDS		SUBSOUTINE FORT (NUM).	INCLUDE 'CONSUC.F'	C MARKARARARARARARARARARARARARARARARARARAR	DO 129 I = 1,NRETS UANIM = UANIM + ANIM(I)/DBLE(NRETS)	129 CONTINUE UANIM-TARGET	XTOT=0.	DO 130 I=1 MUM	CUM(1) = X(1)  IF(X(1)   1	* * * * * * * * * * * * * * * * * * *		RETURN END IF	130 CONTINUE	S	WRITE(*,*) TOTAL WEIGHT IN PORTFOLIO = X: XTOT*100.	- 1
NGIIII		CONTRACTOR TO THE PRINT SPANNING SIMULATION RESULTS ***	OPEN(10,FILE=FILEOUT,STATUS='UNKNOWN') REWIND(10)	WRITE(10,*)' NATIONAL INVESTMENT SERVICES SPANNING TECHNOLOGY' WRITE(10,*)'	.,	WRITE 10. + . LIABILITY STREAM LISED ', LIANAME WRITE 10. + .	WRITE 10. * NUMBER WISHT WEIGHT SENSITIVITY SIC # 1DC ',	•	****** CALCULATE THE PORTFOLIO RETURNS ****** FIRST CALCULATE RETURNS FOR NOTAT DERION ******	DO 80( 1 - 1,NSTAT PFET(1) - 0:0	DC 900 J = 1,NUM DC	800 CONTINUE 4***** NOW CALCULATE RETIIONS AND WEIGHTS IN SIMILIATION BEDIOD *	DO 801 1-1, NSINS PRET (1-NSINS) -0.0	UU 901 0-1,NUM PRET(1+NSTAT) = PRET(1+NSTAT)+CUM(J)*RET(1+NSTAT,J) 901 CONTINUE	DO 1001 K = 1,NUM CIMIKN = CIMIKN*() + DET/(14NCTAT MY)/// - DDET/(14NCTATA)	1001 COVTINUE STATE CONTINUE STATE C	. *** WRITE OUT THE NEW WEIGHTS TO A FILE CALLED 'OLD'****** OPEN(13), FILE = 'OLD', STATUS = 'OLD')	NEMIC 13) DO 140 1 = 1,NUM WRIFF 5,940	40 CONTINE 40 FORMATI 1X, F15.8)	CLUSE(13) ****** CALCHIATE DADITALS AND UDITE PHITBIT **********************************	R = 0.0 VAR = 0.0 T = 0.0

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C BO 1300 1-1,NSTAT  C RET(1,3)-RET(1,3)+ANIH(1)+TARGET  C 1300 CONTINUE  C ***** SET AVERAGES AND COVARIANCES TO ZERO ************************************	·	AVE(1)-AVE(1)ANIM(1)/DBLE(NSIM) AVE(2)-AVE(2)+PRET(1)/DBLE(NSIM) AVE(3)-AVE(3)+(PRET(1)-ANIM(1))/DBLE(NSIM)	C **** CALCULATE COVARIANCES ************************************	DO 950 K-NSTAT+1, IREAD 950 CONTINUE CALCULATE THE COVARIANCE MATDIX: CALCULATE THE CALCULATE TH	DO 960 1-1, 3  DO 960 J-1, 3  DO 960 J-1, 3  DO 986 J-1, 3  COV(1, J)-COV(1, J)+((STAT(K, I)-AVE(I))*(STAT(K, J)-AVE(J)))  COV(1, J)-COV(1, J)/DBLE(NSIM-I)  960 CONTINUE  CALCULATE CORRELATIONS ************************************
11:0UNT-0  D() 131 1-1, NUM  IF (BULLET. ME. 0. 0)B(1) = B(1)/BULLET  C(1, 1) = 0.0  D() 132 -3-1, NUM  C(1, 1) = C(1, 1) + X(3) + 2.0 + A(1, 3)  132 CONTINUE  XRET = AVE(1) + UANIM  XRET = XRET + X(1) + X(1) + B(1)  131 CONTINUE  XCOVAR = XCOVAR + X(1) + B(1)	DO 150 I = 1,NUM C(I,1) = B(I)*XVAR**(-0.5)-0.5*XCOVAR*C(I,1)*XVAR**(-1.5) ICOUNT-ICOUNT,X ARITE(10,16)ICOUNT,X(I)*100,CUM(I)*100,C(I,1)*100, 150 CONTINUE 16 FORIGIT(IX,I4,1X,2F8.3,F10.6,I4,2X,A9,2X,A30)	STD. (XVAR*12)**(.5)*100 XRET = XRET*12.0*160.0 XCOVAR = XCOVAR*1200	WRITE(10,649) STD, XRET, XCOVAR 649 FORMAT(1X; MINIMUM STD DEV =, F10.4, EXPECTED RETURN =',F10.4, WRIT:(10,*)	C IF("TYPE.EQ.1.AND.XTOT.LT995)WRITE(10,*)' ERROR *********************************	END  C ***********************************

•

DO 951 1-1,3  DO 951 J-1,1  EFVAR[1].LE. 0.0 .OR. VAR(J).LE. 0.0) GO TO 951  COREL(1,J)-COV(1,J)/(VAR(I)**.5*VAR(J)**.5)  951 CONTINUE CACULATE CUMULATIVE RETURNS ANIM(NSTA)-100 ANIM(NSTA)-100 DO 569 I=NSTAT-11READ	XX=PREY(1) YY-ANIN(1)=PRET(1-1)*(1+XX) PRET(1)-PRET(1-1)*(1+XX) ANIN(1)=ANIN(1-1)*(1+XY) 569 CONTINUE 1F(VAR(1).NE. 0.0) BETA = COV(1,2)/VAR(1) ALPHA # AVE(2) - BETA *AVE(1)	SST = 0.0 SSE = 0.0 DO 952 I = NSTAT+1, IREAD SSE = SSE + (ALPHA+BETA*STAT(1,1)-STAT(1,2))**2 SST = SST + (STAT(1,2)-AVE(2))**2 952 CONTINUE	IF(NSIMS.G.C.2) STDERR = (SSE/DBLE(NSIMS-2))**.5  IF(SST.ME.O.0) RSQ = 1 - SSE/SST  C****** BEGIN WRITING THE TRACKER OUTPUT **********************************	WRITE(10,*) WRITE(10,*) C ***** WRITE MONTH, LIABILITY RET, PORTFOLIO RET, DIFFERENCE **** DO 700 1=NSYAT+1.1READ	41 (1) E (1) WRITE	WRITE(10,*) WRITE(10,886) WRITE(10,886) BB6 FORMAT(1X,'CUMMULATIVE VALUES OF LIABILITIES AND ASSETS'/, ',' MONTH LIABILIIES PORTFOLIO',')
DO (47 I-NSTAT, IREAD  1STAT = 1-NSTAT-1  WRITE(10,328)!STAT+NM, ANIM(1), PRET(1)  328 FORMAT(1X,15,7X,F7.3,10X,F).3)  847 CONTINUE  837 CONTINUE  837 CONTINUE  848 MRITE STATISTICS BASED ON SIMULATIONS MONTHS ************************************	WRITE(10,*) WRITE(10,*) WRITE(10,985)NM,NM+NSIMS-1 985 FORMAT(/, STATISTICS BASED ON MONTHS ',14,' THRQUGH',14)  C ***** WRITE ALPHA,BETA,STDERR,CORREL,AND R-SQUARED	WRITE(10,*) WRITE(10,987)'ALPHA', ALPHA, 'ANNUAL', ALPHA*1200 WRITE(10,989)'STD ERA', STDERR, STDERR*100 WRITE(10,999)'STD ERR', STDERR, STDERR*100 WRITE(10,999)'STD ERR', STDERR, STDERR*100 WRITE(10,998)'STD ERR', STDERR', STDERR*100 WRITE(10,998)'STD ERR', STDERR', STDER	1	DO 910 1 - 1,3 AFE(1) = (AVE(1)*12)*100 VIR(1) = ((VAR(1)*12)**.5)*100	WRITH: (10.916) 'LIABILITY', AVE(1), VAR(1) WRITH: (10.916) 'PORFFOLIO', AVE(2), VAR(2) WRITH: (10.916) 'DIFFERENCE', AVE(3), VAR(3) 916 FORMA' (1X,3X,A11,9X,F9.2, 'X,10X,F9.2, 'X,) C **** WRITE PARAMETERS FOR THE RIN ***********************************	WRITI(10,*) WRITI(10,*) WRITI(10,*) WRITI(10,*) WRITI(10,*) WRITI(10,*) WRITI(10,*) WRITI(10,*)

```
* PORTFOLIO CONSTRUCTED UPON THE FOLLOWING DATA:
                                                                                                                                                                                                                                                                                                                                                                                 DO 300 I-1,NSTAT
WRITE(10,612)1+NM-(NSTAT+1),(STAT(1,J),J-1,3)
CONTINUE
                                                                                                                                                                                                                                                                                                                                   WRITE HISTORICAL DATA USED TO MAKE RUN
                                                                                                                                                                                                                                                                                                                                                                                                         300
                                                                                                                                                          DELTA IS THE PERCENTAGE IMPROVEMENT IN VARIANCE ******
                                                                                                                                                                                DELTA - (VOLD - VNEW)/VNEW

DELTA - (VOLD - VNEW)/VNEW

C ******** IF THE OLD VARIANCE IS ZERO USE THE NEW PARTIALS TO SORT **

If (VOLD.EQ.0) KVAR = 1
                                                                                                                                                                                                                                                                                                                                                                                                                 AR).GT.CC(BUY(I),KVAR)) THEN
                                                                                                                                                                                                                                                                                                                             SELL(ISELL) - I
END IF
TURN JV - TURNOV + ABS(X(I)-OLDWT(I))
DO 10 1-1, NUM
CC(1,1) =
CC(1,2) =
DO 20 3-1,
                                                                                                                                                                                                                                      IBU! - 0
ISE!.L - 0
TURIOV - 0.0
                                                     VNEW = 0.0
                                                                                                                                                                                                                                                                                                                                                                                                                                                     END II
CONTINE
                                                                                                                                                                                                                                                                                                                                                                                                                                                              40
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TURNOVER - ', TURNOV*50,' X'
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          SENSIT CODE!
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 WRITE THE BUYS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   WRITE(10,102)('*',1-1,78)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              BUY(1))*100
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              WRITE(10,102)('*', 1-1,78)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 DO 90 1 - 1, ISELI
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        WRITE(10,*);
WRITE(10,102)('
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       DO BO I - 1, IE
XOLD - OLDWICE
XNEW - X(BUY)
WRITE(10, 101)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            WRITE(10,*);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              WRITE(10, +);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     WRITE(10,*)
WRITE(10,*)
WRITE(10,*)
                                                                                                                                                                                                                                                                                                                                       WRITE 10. WRITE 
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     ...........
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     CONTINUE
                                                                                                                                                                                                                                                                       CONTINUE
                                                                                                                                                                                                   2
                                                                                                                                                                                                                                                                       60
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        M(1) ET. 0.001) WRITE(10,135) 1,SIC(1),CUM(1)*100.
(1x,15,3x,A30,F10.2, '%')
                                                                                                                                                                                                                                                                                                                                                                       *** INDUSTRY WEIGHTINGS ***
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 SIC(3) \cdot Eq.1) CUM(1) = CUM(1) + X(3)
                                                                                                                                                                                                   WRITE OUT THE INDUSTRY WEIGHTS INDUST
                                                                                            FOR AT (1X, 4F7.3, 14, 4X, A9, 2X, A30)
FOR AT (1X, 80A1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   DO 1:8 1 = 1,4
WF1TE(10,102)(' ',I=1,78)
CONTINUE
CLOSE(10)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        SUMMINT = 0.0
DO 1:6 1 = 1, NUM
SUINGHT = SUMMGHT + X(1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       WRITH(10,137)'
FORMUT(1X,A38,F10.2,' %')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       INCLUDE 'COMSUC.F'
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            END
CONTINUE
                                                                                        101
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     135
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          138
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                136
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        137
                        8
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 134
```

SI(19)
SI(11)
SI

```
CHARACTER HEAD*(MAXTXT), LAST*(MAXTXT), OPTIONS(LINES)*(MAXTXT)
CHARACTER*30 PAST
                                                                                                                                                                                                                   ELSE WRITE(*,*)'NO OPTION SELECTED - PLEASE TRY AGAIN' 60 TO 10 10
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               - PAST.DAT'
                                  CALL MENU(LINES, HEAD, LAST, NBROPT, OPTION, RESPON)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              PARAMETER (MAXTXT - 50, LINES - 24)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  INITIALIZE READ IN FILE: PAST
                                                                                                                                         ELSE IF (RESPON.EQ.2) THEN IHOLD = 1 CALL REDPAST
                                                                         IF (RESPON.EQ.1) THEN IHOLD = 0 CALL REDPAST
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              NCLUDE "COMSUC.I
LAST . . .
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       :::
                                            ខ្ព
                                                                                                                                                                                                                                                                                                                                                           GIVE OPTION TO READ FROM SCREEN WITHOUT DUMPING OUT OF PROGLAM OR TO READ FROM DIFFERENT FILE NAME
                                                                                                                                                                                                                                                                                                                                                                                                                     HEAD - ... WARNING: THE PAST DATA FILE DOES NOT EXIST
LAST - ( CTRL-C TO ABORT )
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            CALL ME (U (LINES, HEAD, LAST, NBROPT, OPTIONS, IRESPON)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                   NBROPT .. 2
OPTIONS 1) - INPUT NEW NAME FOR PAST DATA FILE'
OPTIONS (2) - READ IN NEW DATA FROM SCREEN '
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 IF ( IR:SPON.EQ.1) THEN WRITE(*,100)(''',1 = 1,5)
WRITE(*,104)('',104)'',END = 20,ERR = 20) PAST
GO T) $
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          ELSE IF (IRESPON.EQ.2) THEN
CALI REDSCRN
RETURN
                    MRITE(*, 100)(' ',1 = 1,5)
                                                                                                                                                                                                                                                                                                                                            CONTINUI:
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    RETURN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     END 1F
```

	SUBROUTINE REDSCRN	TITLE FOR THIS ROUTPUT FILE LIABILITY RETURN STOCK RETURNS FI		IN BUSTRY HOUSTRY P.		WRITE(* 113)(' .1 = 1.16) FORMA!('0',A1) WRITE(* 101) FORMA!(' 1) ENTER TITLE FOR SPANNING RUN - '.5) FORMA!(' 1) ENTER TITLE FOR SPANNING RUN - '.5)	READ(*) WRITE(*) WRITE(*) READ(*) WRITE(*)	•	WRITE(*104) 4 FORMAT(*4) ENTER STOCK RETURNS FILE NAME 5 FORMAT(*14) END = 4 ERR = 4) STOCKIN 1 F (\$10ckIN Eq.**) STOCKIN = *\$TOCKS.PRN' WRITE(*,*)	WRITE(*,105)
•				,	::	13	102	103	104	w
ILE NAME,s) BONDIN S.PRN'	NTH TO BEGIN . 1987 <b>–</b> 8702) - ',\$)	IS TO SIMULATE - ',\$)	KS TO USE - '.\$)	S TO USE - ', \$)	S READ PAST - ',S)	JLDING - % ', \$)	/ HOLDING - x · , s)	REDSCRW ************************************		
105 FOR 4AT(' 5) ENTER BOND RETURNS FILE NAME REA 3(*, (A30)', END = 5, ERR = 5) BONDIN IF (BONDIN EQ.', 9) BONDIN = 'BONDS. PRN' MRI'E(*,*)	WRITE(*,*); 6) ENTER YEAR AND MOI FORBAT SIMULATION (e.g. FEB REAL(*,*END = 6,ERR = 6) NMSAVE WRITE(*,*)	WRITE(*, 107) FORMAT(* 7) ENTER NUMBER OF MONTH READ(*, *, END = 7,ERR = 7) NSIMS WRITE(*, *)			WRITE (*, 110) FORM*I(*10) ENTER NUMBER OF STOCKS READ(*, *, END =10, ERR = 10) IDUMHY WRITE(*, *)	WRITE(*,111) FORMA(*11) ENTER MINIMUM STOCK HOLDING READ(',*,*,EKD = 11,ERR = 11) STOCKMIN WRITE(*,*)	WRITE *, 112) FORMA'('12) ENTER MAXIMUM INDUSTRY READ(',*,*EMD = 12,ERR = 12) YIMAX WRITE('*,*) RETURN	FORMAT(A35) END AAAAAAAAAAAAAAAAAAAAAAAAAAAAAAAAAAA	**************************************	
=_	6 106	107	108	109	55	111	112	2		

```
CALL SPECIFICATIONS
CHARACTER OPTION(*)*(MAXTXT), HEADER*(MAXTXT), LAST*(MAXTXT)
INTEGER NBROPT, RESPON, LINES
SUBROUTINE MENU (LIMES HEADER, LAST, NBROPT, OPTION, RESPON)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                PRINT BLANK UPPER SCREEN
IMAX = (LINES-NBROPI-7)/2+1
IF (IMAX.LI.0) THEN
WRITE(*,*) TOO MANY OPTIONS TO FIT SCREEN SIZE'
                                                                                                    PURPOSE: TO PRINT A MENU AND READ RESPONSE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    OVERALL SPECIFICATIONS
INPLICIT REAL (A-2)
INTEGER MAXTXT
PARAMETER (MAXTXT - 50)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      LOCAL SPECIFICATIONS INTEGER I, IMAX
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   DO 20 I - 1, NBROPT WRITE(*, '(1x, 12, 24) WRITE(*, ')OPTION(I) CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           (KT(1)=-1,0,+1 IF I-TH CONSTRAINT IS .GE.,EQ.,.LE.)
THE OBJECTIVE FUNCTION SHOULD BE CONVEX (CONCAVE)
FOR MINIMIZATION (MAXIMIZATION) PROBLEMS.
THIS MEANS THE SYMMETRIC MATRIX QUAD-QUADGITRANSPOSE)
SHOULD BE NOWNEGATIVE (NONPOSITIVE) DEFINITE
FOR MINIMIZATION (MAXIMIZATION) PROBER EME
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     40 X NO - CONSTRAINT MATRIX
40-VECTOR OF CONSTRAINT TYPES, -1,0,+1 MEAN .GE.,.Eq.,.LE.
RESPECTIVELY
440-VECTOR OF RIGHT-HAND-SIDE VALUES
460-VECTOR OF LINAR COSTS
410 X NO MATRIX OF QUADRAIIC COSTS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           IN WHAT FOLLOWS, MO - NO. OF CONSTRAINTS, NO - NO. OF VARIABLES, DIMENSION SIZES GIVEN ARE THE MINIMUM REQUIRED.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        SUBROL TINE QUADI (A,KT,RHS,COST,QUAD,INPUT,TOL,TITLE,PFILE,OB. X,RC,DUAL,SLK,IOUT,MS)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         SUBROUTINE QUADPR FOR QUADRATIC PROGRAMING PROGRAMS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        QUADDR MINIMIZES OR MAXIMIZES COST*X + X*QUAD*X SUBJECT TO A*X + KT**SLACK" = RHS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            CALLING SEQUENCE.
CALL QUADPR (A.KT, RHS, COST, QUAD, INPUT, TOL, TITLE, PFILE,
OBJ, X, RC, DUAL, SLK, IOUT, WS)
                                                                                                                                                                                                                         WRITE *** (*)
WRITE *** (*)
WRITE *** (*)
WRITE ** (*)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         CTIVELY
CTOR OF RIGHT-HAND-SIDE VALUES
CTOR OF LINEAR COSTS
NO MATRIX OF QUADRATIC COSTS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         BLANK OUT REST OF SCREEN
DO 25 1 - 1, 1MAX
WRITE ( +, +) .
                                                                                                                                                                           REQUEST RESPONSE
                             WRITE (*,*) LAST
```

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HOUT --- FIXED CONSTANTS VECTOR OF LENGTH 21 CONTAINING ...

ROW DIMENSION OF A IN CALLING PROGRAM. MINIMUM IS MO.

2 ROW DIMENSION OF QUAD IN CALLING PROGRAM. MINIMUM IS MO.

3 NUMBER OF CONSTRAINTS.

4 NUMBER OF VARIABLES.

1 F OBJECTIVE IS TO BE MINIMIZED.

1 IF OBJECTIVE IS TO BE MINIMIZED.

1 IF OBJECTIVE IS TO BE MINIMIZED.

1 IF OBJECTIVE IS TO BE MINIMIZED.

2 **(MOHON) **-2 + 12**(MOHON) + 16 IF ANY EQUALITY CONSTRAINTS

ARE PRESENT OR 2**(MOHON) **-2 + 8**(MOHON) + 6

ARE PRESENT OR 2**(MOHON) **-2 + 8**(MOHON) + 6

AND THOUSE OBJECTIVE AT SOLUTION OPTION. —0 NO. —1 YES.

5 **OUTPUT PROBLEM PARAPHERS OFTION. —0 NO. —1 YES.

1 **D OUTPUT PROBLEM PARAPHERS OFTION. —0 NO. —1 YES.

1 **OUTPUT MITH A AND QUAD MATRICES IN DENSE FORM.

1 **OUTPUT MITH A AND QUAD MATRIX IN SPARE FORM.

1 **OUTPUT MITH A AND QUAD MATRIX IN SPARE FORM.

1 **OUTPUT MITH A AND QUAD MATRIX IN SPARE FORM.

1 **OUTPUT MITH A REPORT OFTION. —0 NO. —1 YES.

1 **OUTPUT MITH A REPORT OFTION. —0 NO. —1 YES.

1 **OUTPUT MITH A REPORT OFTION. —0 NO. —1 YES.

1 **OUTPUT MITH A MOUTPUT OF OUTPUT. —2 OUTPUT.

1 **OUTPUT MITH MAN MIDTH OF OUTPUT. —1 PRINT PROBLEM PARAPHERS AND FINAL OUTPUT. —1 PRINT MAXIMUM OF 72 AND A MAXIMUM WIDTH OF OUTPUT LINES. A MINIMUM OF 72 AND A MAXIMUM WIDTH OF MOTH OF MOUTPUT. —2 HIND MAXIMUM OF 72 AND A MAXIMUM OF 132 WILL BE USED.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  --- TOLERANCE VECTOR OF SIZE 2 CONTAINING...
I ROUND-OFF OR ZERO TOLERANCE. IF .LE. 0 RESET TO 1.E-7
2 PIVOT TOLERANCE. IF .LE. 0 RESET TO 1.E-6
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      TITLE PRINTED IN OUTPUT. TYPE CHARACTER.

MAY CONTAIN UP TO 64 CHARACTERS.

TRUNCATED TO 64 CHARACTERS.

ILE --- FILE WHE QUADPR WRITES DITOUT ONTO IF REQUESTED.

TYPE CHARACTER. MAY CONTAIN UP TO 64 CHARACTERS.

IF FILE CANNOT BE OPENED. A FILE WILL BE CREATED AND A HESSAGE PRINTED. IF THE WAME IS ALL BLANKS,

OUTPUT TO BE FILED WILL BE DISCARDED.

--- NO-VECTOR THAT WILL CONTAIN THE SOLUTION.

--- NO-VECTOR THAT WILL CONTAIN THE SLACK VALUES.

MO-VECTOR THAT WILL CONTAIN THE SLACK VALUES.

MO-VECTOR THAT WILL CONTAIN THE SLACK VALUES.

--- NO-VECTOR THAT WILL CONTAIN THE SLACK VALUES.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           JP1V07 11 (
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MINNAX
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ITCM
                                                                                                                           ANY EQUALITY CONSTRAINTS (MO+NO) + 6
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              OUT UT UT UNITS FOR LINE PRINTER (TERMINAL) AND OUTPUT FILE DAIA LUPRNT, LUFILE / 6, 92 /
                                                                                                                                                                                                                                                                                                                                              DI 4ENSION A(1), KT(1), RHS(1), COST(1), QUAD(1), INPUT(1), 1 TOL(1), X(1), YC(1), DUAL(1), SLK(1), 10UT(1), WS(1) CH NRACTER*64 TITLE, PFILE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              COPMON /QPRCBR/ TOLS(2)
EQLIVALENCE (TOLS(1),TZERO), (TOLS(2),TPIV)
                                                                                  WORK SPACE ARRAY OF SIZE AT LEAST
Z= (MO+NO)+2 + 12-(MO+NO) + 16 IF A
ARE PRESENT OR Z= (MO+NO)++ 8+6
IF ALL CONSTRAINTS ARE INEQUALITIES
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             CHARACTER*64 TITLES, PFILES COMMON /QPRCBC/ TITLES, PFILES
                                                                                                                                                                                                                                                                        IMPLICIT REAL (A-H,O-Z)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             DOLBLE PRECISION PIVOT COPHON /QPRCBD/ PIVOT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    DATA NCALL / 0 /
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             INITIAL IZATIONS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           101 - LUPRNT
IERI: - 0
17217 - 0
17217 - 701(1
1711 - 701(2)
NCAIL - NCALL
DO 0 1 - 1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   NCALL = 0
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LUFILE, FILE—PFILES, STATUS—"UNKNOMN", ERR—60)
UFILE, FILE—PFILES)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           (L2 .GT. 0) GO TO 40
ANK FILE NAME, DISCARD OUTPUT TO BE FILED.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    i.I) .Eq. ' ') GO TO 30
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     (L2:L2) - PFILE(1:1)
                                                                  TITLES(1:L1) - TITLE(1:L1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             1) 60 TO 50
L1 - LEN(TITLE)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   L1 - LEN(PFILE)
                                                                                                                                                                                                    22
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        3
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                OUTPUT PROBLEM PARAMETERS AND PROBLEM DATA IF REQUESTED. IF (311 .NE. 0) CALL GRPRII IF (3DA MA .NE. 0) CALL GRPRIZ (A.M.KT.RHS.COST.QUAD.NL)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               OUTPUT H:ADER FOR INTERMEDIATE OUTPUT, IF ANY EXPECTED IF (JPI'IOT .NE. 0) CALL QRPRT3
                                                                                                                                                                                                              PR', 14.4', LIS', 52X)
74) PFILES(1:12)
5X, OUTPUT WILL BE FILED ON ',A12)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       CHECK INPUT DATA PARAMETERS FOR CONSISTENCY CALL QDRVER (KT)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          PERFORM PRINCIPAL PIVOTING TO FINAL TABLEAU.
                                             OPEN FILE. MAKE ONE UP.
                                                                                                                                                                                                                                                                                             PEN THIS FILE EITHER.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              IF (IERR .EQ. 5) GO TO 200
QUIT IF 3AD VALUES (IERR = 5)
                                                                                    .Eq. 1) GO TO 76
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 L1 = 1 + 2*(PSQ+P)
L1 + 2*P1
L2 = L2 + 2*P1
L4 = L3 + P1
LENKEQ = L4 + P1 - 1
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GET SOLUTION AND OBJECTIVE VALUE IF REQUESTED.
CALL QDSOLN (KT,COST,QUAD,NL,WS,P,WS(L4),X,RC,DUAL,SLK,
WS(L1),OBJ)
                                                                              OUTPUT SOLUTION REPORT IF REQUESTED.
IF (JSOL .NE. 0) CALL QRPRTG (X,RC,DUAL,SLK,OBJ)
                                                                                                                                                                                              CLOSE PRINT FILE IF REQUIRED.

IF (JOUT .GT. 0) CLOSE (LUFILE,STATUS-'KEEP')
CALL QDCCMP (WS,WS(L1),WS(L2),WS(L3),WS(L4))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       COMMON /QPRCBR/ TOLS(2)
EQUIVALENCE (TOLS(1),TŽERO), (TOLS(2),TPIV)
                                                                                                                                                                                                                                                                                                                                       CHECK INPUT DATA FOR QUADPR
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 INTEGER ZERONE(4), ZERO12(3)
                                                                                                                       SET EXIT VALUES, IOUT.
D CONTINUE
IOUT(1) = IERR
IOUT(2) = ITCNT
                                                                                                                                                                                                                                                                                                                                                                   IMPLICIT REAL (A-H,0-Z)
DIMENSION KT(1)
                                                                                                                                                                                                                                                                                                            SUBROUTINE QDRVER (KT)
                                                                                                                                                                                                                                      RETURN
                                                                                                                                                                                                                                                  "ILLEGAL VALUES IN KT. KT CONTAINS"
                                                                                                                                                                                                                                                                                                                                                                              33 CONTINIE
DO 34 [= 1, 3
                                                                                                                                                                                                                                                                                                                                                                                                                                       VE OR EXCEEDS INPUT(1)")
                                                                                                                           CHECK I:T

DO 10 | - 1, MO

IF | TABS(KT(1)) .GT. 1) GO TO 20

10 CONTINIE

20 CONTINIE

WHITE | 101,222, WGALL
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  34 CONTINIE
DO 35 (= 1, 10
IF ERROR(I)) GO TO 38
35 CONTINIE
GO TO 10
                                IF (TZ:RO .LE. OF LE . OF .LE. OF .LT. IF (3W DTH .LT. IF (3W DTH .GT.
                                                                                                                                                                                                                  WRITE (101,22
22 FORMAT (///
WRITE (101,24
24 FORMAT (/ I)
16 (12) )
IERR 5
ITITLE - 1
                                                                                                    ITITLE - 0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       38 CONTINUE
                                                                                                                                                                                                                                                                                                                                            9
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.P.P1, PSQ
.1OUTS(2), ROM, COL, INDX, MORE, P, P1, PSQ
                                                                                                                                          DOUBLE PRECISION 8
DIMENSION A(LDA,1),KT(1),RHS(1),COST(1),QUAD(LDQ.1),B(LDB.1)
WHERE A', RHS', COST', QUAD' ARE OBTAINED FROM A'RHS,
CONVERTING THE PROBLEM TO MINIMIZATION WITH ALL '
                                                                                   IMPLICIT REAL (A-H,0-Z)
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FILL LOWER TRIANGLE OF [1] AND [3]. NI = NO - 1 IF (MINWAX .Eq. 1) GO TO 40

CHECK FOR CASE OF NO CONSTRAINTS. CONT...NUE IF (HO .EQ. 0) GO TO 240

90 CONT (NUE

60 CONT INU

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AINTS, EXPRESS AS R+1 .GE. CONSTRAINTS, SUM OF THE OTHERS.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  SUBROUTINE QDCOMP (B, TEMP, U, JZ, JW)
                                                                                                                                                                                                            60 TO 170
60 TO 190
                                                                                                                                                                                                                                                                                                     CONTÍNUE

8(P.1) - RHS(I)

8(P.1) - RHS(I) - B

60 TO 210

GE. CONSTRAINT

CONTINUE

B(K, P.1) - A(I, L)

CONTÍNUE

B(K, P.1) - A(I, L)

CONTÍNUE

B(K, P.1) - RHS(I)

G(F) - RHS(I)

CONTÍNUE

B(K, P.1) - RHS(I)

CONTÍNUE

B(K, P.1) - A(I, L)

CONTÍNUE

B(K, P.1) - A(I, L)

CONTÍNUE

CONTÍNUE

B(K, P.1) - A(I, L)

CONTÍNUE

B(K, P.1) - A(I, L)
220 CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                       170
                                                                                                                                                                                                                                                                                                                                                                                                                                         380
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     240
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      390
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      200
                                                                                                                                                                     INT GER ROW, COL, INDX, P. P1, PSQ
COM TON /QPRCB1/ INPUTS(14), IOUTS(2), ROW, COL, INDX, MORE, P, P1, PSQ,
ICALL, LENREQ, IO1, 102, 103
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     40 ITEMP = 0
C****CHECK FOR NONDECREASING INDEX (ALLOW UP TO 5 EQUAL INDEXES FOR
C****TOLER UNCE PURPOSES).
13 = 350
10 50 1 = 1, P
13 = 13 + 1
                       COPPUTE THE FINAL TABLEAU FOR QUADRATIC PROGRAMMING GIVEN THE INITIAL TABLEAU USING THE METHOD OF PRINCIPAL PIVOTING
                                                                                                    DOUBLE PRECISION B.TEMP,U
INTEGER JZ,JW
DIM:NSION B(1),TEMP(1),U(1),JZ(1),JW(1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     DATA MSG / 'ALGORITHM ERROR. INI
'NO SOLUTION' INI
'NO SOLUTION' INI
'ERROR', ITERATIOI
                                                                                                                                                                                                                                                                                                                                                                                                                                     DOUELE PRECISION 2, BS, BST
CHARACTER*48 MSG(4)
                                                                      IMPLICIT REAL (A-H,0-Z)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       SO CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      30 CONTINUE
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DIAGONAL ELEMENT (NOT ALLOWED IF POS. SEMIDEF.)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     - -Q(R)/B(R,R), THE INCREASE IN THE DRIVING VARIABLE.
                                                                              GO TO 400
                                                                                                                                                                                                                                                                                                                                                                                     B(IJ) .LT. (-TZERO)) GO TO 70
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               (ROW. Eq. 0) GO TO 420
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          90 CONT
) 60 TO 140
-TZERO)) 60 TO 120
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    JFLAG . 0

C****PUT TO ERANCE ON B(1,P1) AFTER A MONPRINCIPAL PIVOT.

13 - P3Q + 1

14 (B(13) .LT. (-TZERO)) GO TO 170

GO 10 10

C****THE NE! DRIVING VARIABLE IS THE COMPLEMENT OF THE OLD BLOCKING
C****THE NE! DRIVING VARIABLE IS THE COMPLEMENT OF THE OLD BLOCKING
170 DO 180 JJ = 1, P

180 CONTINIE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         150 III = JUROW)
NFLAG = 1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  180 CONTINIE CONTINIE CONTINIE CONTINIE CALLONED IF POS. SEMIDEF.)
60 TO 410
190 COL 4,0
C****HE DESTINGUISHED VARIABLE IS STILL THE I-TH ROW.
13 - P'(COL-1) + I.
(B(KJ) .LT. (-TZERO) .OR. BST .GE. (-TPIV))
(DABS(B(KJ)) .LT. TZERO .AND. B(IJ) .LT. {-;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                TPIV = TPIV + TOLS(2)/50.
****INDICATE THE NUMBER OF ITERATIONS
NRITE(* 101) OPTIMIZATION ITERATION
101 FORMAT(**, A50, 15)
                                                                                                              IF (B(KJ)) 130, 140, 130

RGI = J

GO TO 150

BS = -BST / B(KJ)

IF (BST -LE. BS) GO TO 140

RGI = J
                                                                                                                                                                 120
130
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      200
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Z = B(13) = B(x3)
B(13) = B(x3)
B(13) = Z
CONTINUE
11 = JZ(3)
JZ(3) = JZ(4)
JZ(3) = JZ(4)
JZ(3) = JZ(4)
Z 
                                                                                                                                                                                                                                                                        C*****NUST REARRANGE THE ROWS AND COLUMNS FOR COMPLEMENTARITY
60 TO 500
CONTINUE
IF (JELAG .EQ. 1) GO TO 290
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 GO TO 280
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      GO TO 230
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       ĬĀBŠ(JW(I))
K .EQ. I) ĜO TO 250
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         240 CONTINUE

11 = 34(1)

34(1) = 34(1)

34(1) = 34(1)

34(1) = 11

250 CONTINUE

260 LILL + 1

260 LILL + 0

260 LILL - 0

260 
                                                                                220
                                                                                                                                                                                                                                                                                                                                                                                                                   230
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       *****QUADPP USES A NORMAL JORDAN PIVOT.
*****QUADPP USES A NORMAL JORDAN PIVOT.
*****HOWEVER, WE CAN SAVE MEMORY BY USING THE ELEMENTARY MATRIX.
*****STORE PIVOT ELEMENT
500 CONTINUE.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  510 CONTINUE
13 = 'C
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KJ = VC + ROW

PIVOT = NC + ROW

Z = 1.000 / PIVOT

-****STORE ELEMENTARY-VECTOR AND U-VECTOR.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         - 1, P1
.NE. COL) GO TO 530
3 + P
                                                                                                                                                                                                                                                                                                            IF (JPIVOT .EQ. 1) CALL QRPRTS
IF (IND. .GT. 1) GO TO 40
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          **NORMAL TERMINATION
10 IERR = 1
GO TO 600
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 ***ERROR TERMINATION
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                460 WRITE (101,
1F (30)T .N
470 FORMAT ( / 1
GO TO 500
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             1 ERR 6 6 60 TO 460
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   10 K = 2
1ERR = 4
60 TO 460
120 K = 3
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         ... K = 3
IERR = 2
GO TO -60
440 K = 4
```

```
IF (LLL .GE. 2) GO TO 260
290 ROW = LL
ICOT = ITCNT + 1
C****ATTEMPT TO PROGRESSIVELY RELAX THE CONVERGENCE PARAMETER
                                    JELAG = 1
C*****MUST REARRANGE THE ROWS AND COLUMNS FOR COMPLEMENTARITY
C*****EXCHANGE ROWS
                             JFLAG .EQ. 1) GO TO 290
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             .GE. 2) GO TO 260
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           280 CONTINUE
                                                                                                                                                                                                                                                                               250 CONTINUE
IF (LLL
C*****EXCHANGE
260 LLL = 0
CONTIN
                                                                              230
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   270
                                                                                                                                                                                                                                                                                                                                                                         A NORMAL JORDAN PIVOT.
CAN SAVE MEMORY BY USING THE ELEMENTARY MATRIX.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    COL) 60 TO 530
                                                                 IF (JPIVOT .EQ. 1) CALL QRPRTS
IF (INDX .GT. 1) GO TO 40
                                                                                                           **NOFMAL TERMINATION
)0 IEIR = 1
GO TO 600
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        510 CONTINUE
13 - KC
10 520 1
13 - 13 13 15 15
                                                                                                                                                                                                                                                                                                                        460 W
```

DOUBLE PRECISION DART, BB

CENTINUE

CONTINUE

DO 110 J = 1, NO

R(JJ) = 0.0

R(JJ) = 0.0

LOORTHUE

DO 120 I = 1, NO

LOORTHUE

LOO

C\*\*\*1F X(I]

20

C\*\*\*IF X(

```
IF THE OPTIMAL PORTFOLIO IS WITHIN TURNOVER LIMIT, RETURN **** F (ITURN .EQ. 1) THEN OS 1 = 0.00 S 1 = 1.NUM
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   REAL QC(NDID,ND),QRMS(NDID),QTOL(2),QRC(ND),QMS(ISIZEQ),QB(ND)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   INTEGER QKT (NDID), INPUT (14), QIOUT (2), NUM, MAXWS CHARACTER*30 PFILE
                                                            OBJECTIVE VALUE ONLY IF REQUESTED
                                                                                                                                                                                                                                                                                                                                           1) - TEMP(1) + X(J)*QUAD(1,J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             S 1 = 1,NUM
COST = COST + ABS(X(1)-OLDWT(1))
                                                                                                                                                                                                                                                                                                                                                                                                                                                      230 CONTINUE

240 CONTINUE

240 CONTINUE

240 CONTINUE

240 CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             SUBROUTINE QSET(NUM, MAXMS,
                                                                                                                                                                   .Eq. 0) GO TO 250
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     REAL O(4), S(4), XMAX(ND)
INTEGER KK(4)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    DO 10 1 - 1, ID
DO 10 3 - 1, NUM
QC(1+NUM, 3)-C(3, 1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               Constitutes and a second to the contract of the contract and the contract 
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 C FINISHED
250 CONTINUE
RETURN
END
                                                                                                                                                                                                                                                                                                                                                                                                                               220 CONTINUE
DO 230 J
190 CONTINUE
                                                                                                                              200
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        2
                                                                                                                                                                                                                                                                                                                                  C***1F THI OLD WEIGHT EQUALS ZERO
1F (OLDWT(1) .LT. 0.001) THEN
0C/1..31 = -1.0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      C***IF THE OLD WEIGHT EQUALS ZERO
II (OLDWT(I) .LT. 0,001) THEN
                                                                                                                                                                                                                                                            . 1 F(ITURN. EQ. 1) THEN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           11:(1TURN.EQ.1) THEN
                                              DO ::0 1 - 1.N
DO ::0 3 - 1.N
IF(| :Eq.3) TH
QC(| :3) - -1.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             C***IF THE OLD W
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           E:0 1F
```

C+++1F X(1)

```
IF (ITURN.EQ.1) QRHS(NUM+6) - -TURN
DO 40 I = 1,NUM
IF(ITURN.EQ.1) THEN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        C***IF THE OLD WEIGHT EQUALS ZERO
IF (OLDWT(1) .LT. 0.001) THEN
                               QRHS(1) = OLDWT(1)
END IF
                                                                                                                                                                                                                                           ELSE
QRHS(1) = D(1-NUM)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     C E-4 070L(2) = 0.000001
C E-4 070L(2) = 0.0001
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 PFILE - 'TEMP.Q'
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     QTOL(1) - 0.0
                                                                                                                                           END 1F
OKT(1)
CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            C*** IF THE OLD
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       C***1F X(I)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         9-3 J
                                                                                                                                                                                                                                                                                                                                                                                           30
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      SECOND PART CCCCCCCCCCCCCCCCCCCCCCCC
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                C **** LOOP FOR CORRELATION *****************
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      C*** CHE.X IS THE PERCENTAGE CHANGE IN OBJ FUNCTION
CH.CK = 5.0
IF (ITURN .Eq. 0 .AND. TURN .GT. 0.0) CHECK = CHECK*2.5
CH.CK = CHECK /100.
                                                                                                                   - -1.0
- QRHS(NUM+6) - OLDWT(1)
                                                                                                                                                                                                                               = -1.0
= QRHS(NUM+6) - OLDWT(1)
0C(NUM+6.1) = -1.0
QC(NUM+6.1) = -1.0
QRHS(NUM+6) = npur
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    CHANG2 = (SCALE - SCALMAX)/ABS(SCALMAX)
ICOUNT = ICOUNT + 1
                                                                                                                                   C(NUM+6) - (CNUM+6) - 
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        - 1, NUM
[ - -B(I)*SCALE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              WFITE(*,150)ITURN+1
FGRMAT(1X,T55,14)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      2222222222222222222
                                                                                                                                                                                                                                                                                                                                                                                                                                      CC NT INUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            CON TINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                DO 15 1
CONTINUI
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           28
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      150
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    8
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   46
```

```
XVAR = 0.0

COST = 0.0

DO 60 1 = 1,NUM

COST = COST + ABS(X(1)-OLDWT(1))

DO 70 J = 1,NUM

DO 70 J = 1,NUM

XVAR = XVAR + X(1)*X(J)*A(I,J)

CONTINUE

CONTINUE
                                                          CALL QUAD! (QC, QKT, QRHS, QB, A, INPUT, QFILE, OBJ, X, QRC, QDUAL, QS
                                                                                                                     CONTINUE INPUT(5) = 1
IF(010UT(1).NE.1) RETURN
COVAR = 0
CO 1 = 14NUM
COVAR = COVAR + X(1)*B(1)/BULLET
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               END IF

***** CALCULATE THE CHANGE IN X ***
DELTA = DO I = 1, NUH
DO BOLTA = DELTA + ABS(X(I)-F(I))
                                                                                              C *** CALCULATE CORRELATION *****
990
0990
1
                                                                                                                                                                                                                                                                                            29
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         75
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  CON'ÎNÚE
**** SIT F( ) EQUAL TO X( ) TO SAVE THE OLD X( ) *****
CONTINIE
                                                                                                                                                                                                                                                                                                                                                                                                                                                  C ****** TiKE 1/2 OF THE HESSIAN TO SEND TO OPTIMIZER ****
                                                                                                                                                                                                                                                                                                               C ******* CALCULATE GRADIENT G( ) AND HESSIAN H( , )
VARI = 1.5GRIF(XVAR
VARS = VAR2*1.5/XVAR
VARS = VAR2*1.7/XVAR
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   END C ******* E)D OF SUBROUTINE SUCCESS ********
                                                                                                                                                                                                                                                                                                                                                                                                                                                                               (1,3) = 0.5*H(1,3)
      CONTINUE
ICOUN - ICOUNT +
GO TO 49
                                                                                                                                                                                                                                                                                                                                                                                                                                    C ******* AND -X(
                                                                                                                                                                                                                                                                                                                                                                         00 30 | - 1;
6(1) - B(
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    CONT THIE RETURN
                                                                                     C UPDATED: Dice
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               DO 50
                                                     RETURE
END
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                40 CONTI
         8
                                                                                                                                                                                                                                                                            82
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          S
```

```
C *** PARAMETERS ARE USED TO DIMENSION THE COMMON ARRAYS
 C *** IN EACH SUBROUTINE.
 C ***
 C ***
            ND = TOTAL NUMBER OF STOCK WEIGHTS BEING COMPUTED.
C ***
            ID = THE MAXIMUM NUMBER OF CONSTRAINT EQUATIONS.
   ***
            N2D = THE DIMENSION ON WORKING AREAS ( 2 * ND )
   ***
            KEQ - NUMBER OF CONSTRAINTS WHICH WILL BE EQUALITIES
   ***
            NRT = NUMBER OF RETURNS
   ***
            NST - USED FOR STATISTICS
 [ ***
            ISIZEQ = 2 * (ND*2 + ID)**2 + 8*(ND*2+ID) +6
C ***
           NDID = ND + ID
   ****************
            LAST UPDATED: November 19, 1988
         IMPLICIT REAL (A-H,O-Z)
         IMPLICIT INTEGÉR (I-N)
         PARAMETER (KEQ = 0)
C 280
         PARAMETER (ND = 280, ID = 6, N2D = 560)
         PARAMETER (NDID = 286, ISIZEQ = 645246)
C
   250
         PARAMETER (ND = 250, ID = 6, N2D = 500)
PARAMETER (NDID = 256, ISIZEQ = 516126)
C
C 100
        PARAMETER (ND = 100, ID = 6 , N2D = 200)
PARAMETER (NDID = 106, ISIZEQ = 86526)
        PARAMETER (NRT = 48, NST = 3)
PARAMETER (LENGTH = 40)
CHARACTER*(LENGTH) FILEOUT, TITLE, NAME (ND), PORTRETS, GARB, ANSWER,
                        OLD, LIANAME, LIABIN, STOCKIN, BONDIN, IDC (ND), SIC (99)
        COMMON /ARRY/ A(ND,ND),C(ND,ID), H(ND,ND), G(ND), F(ND)
COMMON /VECT/ B(ND),D(ID),BDL(ND),BDL(ND),X(ND),OLDWT(ND)
COMMON /RETS/ RET(NRT,ND),ANIM(NRT),PRET(NRT),ISIC(ND),AVE(ND)
COMMON /TRAC/ COV(NST,NST),STAT(NRT,NST),COREL(NRT,NST)
COMMON /TRA2/ PRICE(ND),VOL(ND),CUM(ND),VAR(3),LIANAME,TITLE
COMMON /RTNIN/FILEOUT,LIABIN,STOCKIN,BONDIN,IDC,NAME,SIC
COMMON /DAT/ NMSAVE,NM,NSIMS,NSTOCKS,NBONDS,NSTAT,NRETS,IDUMMY,
                            IHOLD
        COMMON /MAX/ STOCKMIN, YIMAX, SMAX, SCALE, BRET, XFACTOR, XBUPPER,
                  XBLOWER, BULLET, TARGET, TURN, BULLI, TARGI, TURNI, PORTVAL
E END OF COMMON.F
```

#### APPENDIX IV

"FASTTRACK" PROGRAM FOR ANALYZING
LARGE NUMBERS OF SECURITIES IN A RAPID,
EFFICIENT MANNER TO PROVIDE OPTIMUM
CORRELATION OF ASSET RETURN TO A TIME DEPENDENT
FINANCIAL INDEX. SUBSTANTIAL COMPUTER
MEMORY STORAGE REDUCTION IS ALSO ACHIEVED.

CALI DIFAULT	C UPDATED July 10, 1989
,我也是我们我们的我们的我们的我们的我们的我们的我们的我们的我们的我们的我们的我们的我们	C COPYWRITE 1989 NATIONAL INVESTMENT SERVICES OF AMERICA
: ****** THIS IS SPOT MULTI RETURNS TO FOR NEXT RUN ******	
: CONTINUE	
. seese win Timin in the Name of the states of the states .	
•	C sassassassassas WRITE COPYRIGHT TO SCREEN sassassassassassassassassassassassassas
IF (IFLAG(1).EQ.1) THEN	. Y.
CALL REDPAST TO READ IN PARAMETERS	
	(*,*) 'Created.
	*,*) maintain this work confic
CALL MODIFY TO CHANCE DABANTIEDS	
- Charles Lens	
	*, * Vorks. Those having access to this work
Chestestatestates   FLAG(1)>= THEW MILITIDIE ONLY	WRITE(*,) was, or discloss the incomments in this work unless uping the properties of the properties o
THEN	WRITE(*,*) WRITE(*,*) WRITE(*,*)
Wilte(*,101)'CALLING HULTRUN	) PROPERTY OF NATION
END 1.:	WRITE(*,*)' HRITE(*,*)'
******:*******************************	HRITE(*,101)'CALLING COPTRIGHT
57.	CALL COPYRIGHT
	C ******** READ FLAG FILE TO FIND OUT WHAT KIND OF RUN *
**************************************	WRITE(*,101) 'CALLING READFLAG
	CALL READFLAG
CALL CILCPARAH	
	C ******** SET UP DEFAULT PARAMETERS ************
sections introduced and CALL LIABIN TO DEAD IN DETINDUC	NRITE(*,101)'CALLING DEFAULT

WRIT :(10,102)('\*',K

109 108 11:

••

CC

DO 40 1 = 1,18UY-1 DO 50 J = 1+1

WRITE THE SELLS

BUY \$ ', TOTBUY

WRITE(10, '(127, A12, F14.0)')'TOTAL WRITE(10, \*)
WRITE(10, \*)

WRITE(10,\*)'

OF THE FORCED SELLS (STKS NOT AVILABLE)

SOLD

NE1GHT

WRITE WRITE WRITE WRITE

```
CALCULATE THE ROUND LOT PURCHASE " + + + +
                                                                                                                                                                                                                                                                                                                                         1F(DVOL(BUY(1)).GT.0)THEN
DAYSVOL = 100.*SHARES*PRICE(BUY(1))/DVOL(BUY(1))/1000.0
ELSE
                                                                                                                                                                                                                                                                                                                    ** DVOL 1S IN DAILY DOLLAR VOLUME (000'S)
                                               DELTA SENS CODE IDC TICK', (S) VOL NAME'
                                                                                                                                                                                                                                                  + SHARES*PRICE(BUY(1))*100.0
          SIC SYMBOL',
SECURITY'
                                                                                                                                                                                                                           PORTVAL /PRICE (BUY(1))
          ** NEIGHTS **
SHARES PRICE
                                                                                                                                                                                                                                                                                                                                                            DAYSVOL = 99.9
ENDIF
IF(RHS(BUY(1))-X(BUY(1))
ELSE
                                                                                       - 1,78)
                                                                                                                                                                                                                                                                      SHARES - 0.0
ENDIF
                                                                                                                                                                                                                                                                                                                                                                                                                               ABOUND . ' '
                                                WRITE(10,*)' OLD (00)
                                                                                       WRITE(10,102)('*',K
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            EKO 15
            WR1TE(10,.)'
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      CONTINUE
                                                                                                                                                                                                                                                                                   OLD VERSION DAYSYOL - 100. SHARES/DYDL(SELL(1))/1000.0
                                                                                                                                                                                                        COT SALE
                                                                                                                                                                                                                                                                                                                            IF(DVDL(SELL(1)).GT.0)THEN
DAYSVOL = 100.*SHARES*PRICE(SELL(1))/DVOL(SELL(1))/1000.0
ELSE
ENDIF
                                                                                                                                                                                                                                                                                                          ** DVOL 15 IN DAILY DOLLAR VOLUME (000'S)
                                                                                                                                                                                                                                                      TOTSELL - TOTSELL + SHARES*PRICE(SELL(1))*100.0
                                                             OLD NEW DELTA SENS CODE 1DC TICK', (00) ($) VOL NAME'
                                                                                                                                                                                                                                                                                                                                                                                                              .LT. 0.00001) THEN
                                                                                                                                                                                                       SHARES - 0.01*DELTA*PBRYAL/PRICE(SELL(1))
SHARES - REAL(HINT(SHARES/100.))
                      ** WEIGHTS **
SHARES PRICE
                                                                                                       - 1,78)
                                                                                                                                                                                                                                                                                                                                                                                                                 IF(RHS(SELL(1))-X(SELL(1))
ABOUND - '*,
- 1,78)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            IF (DELTA .ST.
WRITE(10,101)
                                                                                                       WR. TE(10,102)('*',K
 JR. TE(10, 102) ('*', K
                                                                                                                                                                                                                                                                                                                                                                                                                                                  ABOUND
END 1F
                                                                                                                                 TO SELL • 0.0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            END 1F
                                                               WR.TE(10,*)'
                           WR TE(10,*)'
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        COP TINUE
```

G

WO 91/02326	•	1#	PCT/US90/04328
, TOTSELI , TOTBUY , TOTBUY , JX, F4. 1	SROUTINE READS IN STOCK DATA FROM AN UNFORMATTED FILE BINSTIN IFIRST IS FIRST MONTH OF DATA NEEDED FOR MATRIX COMMON.F.	CAPS=XCONS(4)  CAPS=XCONS(4)  SET UP CAP TO BE REPRESENTATIVE OF TIME PERIOD  IF (MYSAVE.LI.7401)CAP-CAPS  IF (MYSAVE.E.7501)CAP-CAPS  IF (MYSAVE.E.7701)CAP-CAPS  IF (MYSAVE.E.7701)CAP-CAPS  IF (MYSAVE.E.7701)CAP-CAPS  IF (MYSAVE.E.7701)CAP-CAPS  IF (MYSAVE.E.7801)CAP-CAPS  IF (MYSAVE.E.7801)CAP-CAPS  IF (MYSAVE.E.80101)CAP-CAPS  IF (MYSAVE.E.80101)CAP-CAPS  IF (MYSAVE.E.8201)CAP-CAPS  IF (M	
F(I.M.SAVE.EE.801) CAP-CAPS* 0.769173     F(I.M.SAVE.EE.802) CAP-CAPS* 0.846097     F(I.M.SAVE.EE.803) CAP-CAPS* 1.00000     F(I.M.SAVE.EE.803) CAP-CAPS* 1.00000     F(I.M.SAVE.EE.803) CAP-CAPS* 1.00000     F(I.M.SAVE.EE.803) CAP-CAPS* 1.00000     F(I.M.SAVE.EE.803) CAPS* 1.00000     F(I.M.SAVE.EE.803) C	1011 NUI 1517 - 0 110 700 1 NE 1 NE 1 LE 1 LE 1 LE	790 IF (NAME(1)(11EN:11EN) . EQ. ' ')THEN  LLSE GO TO 790  ELSE GARB(1:LENGTH) = NAME(1)(1LEN:LENGTH)  END IF (*,1)2   1,NAME(1)  READ (9,END = 785) GARB  READ (9,END = 785) GARB  READ (9,END = 785) GARB  READ (10C(1) = 1  TEN = 1  TEN = 1  TEN = 1  THEN = 11EN + 1  GOTO 793	ENDIF

\*\*\*\*\*\*\*\*\*\*\*\*

\*\*\*\*

112

. 155 253

1 CONTINUE	;	MAHLL, SM (MALMAIL MAT MAI THAIR OF MAH
DO 810 K = 1,1READ READ (9) RET(K,1) ADJUST OCIOBER 1987 ************************************	167	
~		.)(1:1EN) - GARB(11EN:11EN+1EH-1)
*** IF STOCK NON GOES AWAY DURING SIM PERIOD *** THEN THE RETURNS TO MONEY MARKET TYPE LEVEL	792	11EN = 11EN + 1EN + 1
IF (K. GT. MSTAT. AMD. RET (K. 1) . LT1.0) THEN FET (K. 1)-0.005 ENDIF	÷.	
CONTI	492	IEN " ) THEN IF I I I I I I I I I I I I I I I I I I
DO 1200 J = 1,1570P-1LAST READ (9) XGARB		6010 492
		IDC(1)(6:6+IEN-1) • GARB(ILEN:ILEN+IEN-1)
	793 C	READ
N ITOCKS - NSTK M PM - NSTOCKS+NBGNDS	U	D= 785) ISIC(I), IGARBI, IGARBZ, GT.99) ISIC(I) = INT (ISIC(I)/100) READ IN LINE
ENDIF	<b>U</b>	READ(9, END - 785) PRICE(1), SPREAD(1), MANDIA, MANDE READ IN LINE 6 (MARKET CAP, VO
CLOSE(1)		:
RETURN		IF (XMXTCAP(I).LT.CAP)INEXT-1
*** IF END OF FILE WAS HIT ON STOCKS - RESET NUM AND CONTINUE *** NUM = NSTOCKS+WBONDS	ن ن	
CLOSE(1)		NEAU (9, ENU - 703) 13101 IEST FOR EMOUGH RETURNS' TO SATJSFY NRETS
RETURN		
		IF (ICHECK.LT.O) NRETS - NM - ISTART IF (NRETS.LT.NSTAT) ICHECK - IF INST-ISTART
FORMAT('+','STOCK # ',15,' 15 ',A40)		DO 800 J - 1, ICHECK
	800	READ (9) XGARB CONTINUE
sondwhere END OF SUBROUTINE BINSTIN serves and serves a		DO 801 J = 1, NRETS-NSTAT
化二甲基甲基甲基甲基甲基甲基甲基甲基甲基甲基甲基甲基甲基甲基甲基甲基甲基甲基甲基		

```
ENTER NAME OF MULTI FILE(1.e. LTSIG)
                  SUBROUTINE MULTRUN
                                                    INCLUDE 'COMMON.F'
CHARACTER*30 XTITL,XFLOUT,XLIBIN,XSTKIN,XBNDIN,MULTIH
                                                                                                                                                                       OPEN (13, FILE - MULTIN , STATUS - 'OLD')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           OPEN(13,F1LE='PAST.DAT',STATUS='OLD')
READ(13,*)GARB
                                                                                                                                                                                                                                                    DO 10 1 ... 1, 15KIP
DO 20 3 ... 1,18
READ(13,'(A1)',END
CONTINUE
                                                                                     IF(INITIAL.EQ.O)THEN WRITE(*,*)
WRITE(*,*(IX,A40.5)')'
READ(*,'(A30)')HULTIN
INITIAL(*,'(A30)')HULTIN
                                                                                                                                                                                           IF (INITIAL.EQ.O)THEN ISKIP-0 GOTO 30 ENDIF
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               ISKIP - ISKIP+1
                                                                                                                                                                                                                                                                                         22 2
                                                                                                                                                                                                                                                                                                                                                                                                   WARNING NUM >', NHAX,' TOO BIG FOR PROGRAM'
                                                                                                                                                                                                          STOP DONE WITH MULTI RUN
                                                                    WITH MULTIPLE RUN **************
                                                                                                                                                                       MULTRUN
                                                                                                                                                                                                                                                                    NH = NNSAVE
NH = (INT(NH/100)-80)*12+(NM-1NT(NH/100)*100)
IR:AD = NSTAT+NSINS
                                                                                                                                                                  END OF SUBROUTINE
READ(13, '(A30)') DLDF1LE
CLOSE(13)
                                                                                                                                                                                                                                                                                                                                                                          NUP = NSTOCKS+NBONDS
IF(NUM.GT.NMAX)THEN
WRITE(*,*)' WARN
STOP
                                                                                                                                                                                                                                                                                                                IF 'NSTOCKS.GT.O) THEN KBUPPER - SHAX ENI IF
                                                                                                                                                                                                                                              IN CLUDE 'COMMON.F'
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              IFIEST - NM-NSTAT
                                                      :LOSE(13)
                                                                                                               FORMAT (A20)
                                  RTURN
                                             ე წ
                                                                                                                 101
```

READS IN FLAG FILE secondences contracted \* ELSE .... 0.10 (100./(TURM1+.01)-100.0/100.01)
TURM = .0001 \* (100./(TURM1+.01)-100.0/100.01)
A TURM OF .2 YIELDS A TURM CALCPARAM BULLET - BULLET\*ABS(BULLET)/1000. 1F (TURN).EQ.100.)THEN TURN - 0.0 OPEN(9, FILE-, FLABINIS')
DO 100 1-1,10
REAG(9,\*) IFLAG(1)
CONTINUE
D 800 1-1,10
READ(9,\*) XCONS(1)
CONTINUE
D 300 1-1,10
READ(9,\*) XCONS(1)
CONTINUE
CONTINUE
CONTINUE C \*\*\*\*\* END OF SUBROUTINE SUBROUTINE READFLAG CLOSE(9) END 1F RETURN RETURN 댎 9 300 90 200 IN 1989 DOLLARS BOUNDS READS IN STOCK DATA \*\*\*\*\*\*\*\*\*\*\*\*\* READ IN DUMMY STOCK DATA THIS IS TO READ PAST SET UP CAP TO BE REPRESENTATIVE OF TIME PERIOD THE SCALARS ARE REP OF CAPS HISTORYS IFIRST IS FIRST MONTH OF DATA NEEDED FOR MATRIX ILAST IS LAST MONTH OF SIMULATION PRTVALS IS PORTVAL I \*\*\*\*\*\* END OF SUBROUTINE DEFAULT - XCONS(1) INCLUDE 'COMMON.F' CAPS-XCCNS(4) PRTVALS RETURN 몶

- NSTAT, NRESTS FOR B( ) \*\*\*\* SUBROUTINE SERVILL SETS UP DEFAULT PARAMETERS SUBROUTINE DEFAULT STATEMENT S 24 MONTHS PRIOR \*\*\*\*\* END OF SUBROUTINE DEFAULT READ IN OF

1F(CAP.EI).0)CAP-2000000000.0

```
READ IN LINE 2 (CUSIP)
                                                                                                                                                                                                                                                                                                                                                                                                     READ (9,111,END - 785) GARB
READ (9,111,END - 785) GARB
                                                                                                                                                                                                                                READ IN LINE 1 (NAME)
                                                                                                                                                                                DATA
                                                                                                                                                                                IN STOCK
                                                                                                                                                                                                                                                                                                                                       - NAME(1)(ILEN:LENGTH)
                                                                                                                                                                                                                                                                                           .EQ. ' ')THEN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           6010 793
                                                                                                                                                                                READ
                                                      OPEN (9, FILE - STOKFIL, STATUS - 'OLD')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                - GARB(ILEN:ILEN+IEN-1)
       WRITE(*,*)'IN BOUNDS AND MKTCAP - ', MKTCAP
                                                                                                                                                                                                                                       INEXT-0
READ (9,111,END - 785) MAME(1)
ILEN - 1
GARB - 1
ILEN - ILEN+1
GO TO 790
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 Y) THEN
                                                                            DO 600 I = 1,100MY

READ (9,111) (GARB.L = 1,6)

READ (9,*) ISTAT

READ (9,*) 1STOP-1START+1

DO 610 K = 1,1STOP-1START+1

READ (9,*) KGARB

CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       JEN - 1
JF(GARB(JLEN+JEN: JLEN+JEN).NE.'
                                                                                                                                                                                                                                                                                                                            NSTK-0
DO 700 1 - 1,NSTOCKS
                                                                                                                                                                                                                                                                                                                                                                                                                              READ (9.111, END 10c(1)
                               THEN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               IDC(1)(1:1EN)
                                 IF (NSTOCKS.6T.0)
                                                                                                                                                     88.'
                                                                                                                                                                                                                                 783
                                                                                                                                                                                                                                                                                             39
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 791
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      491
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            NON GOES AWAY DURING SIM PERIOD
Returns to money market type level
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  DO 810 K = 1,IREAD
READ (9.*) RET(K,1)
LEAD (9.*) RET(K,1)
LEAD (9.*) RET(K,1)
LEAD (9.*) RET(K,1)-RET(K,1)/2.97
                                                                                                                                                                                                                      READ IN LINE 5 (PRICE, SPREAD)
                                                                                                                                                                                                                                           READ(9,*,END = 785)PRICE(1),SPREAD(1)

READ(9,*,END = 785)XWKTCAP(1),DVOL(1)

IF(XMKTCAP(1),LT.CAP)INEXT-1
                                                                                                                                                                                                                                                                                       READ (9,*,END - 785) ISTART
READ (9,*,END - 785) ISTOP
                                                                                                                                                                                                 READ IN LINE 4 (SIC)
                                                                                                                                                                                                                                                                                                                                                                 $
                                                                                                                                                                                                                                                                                                                                                        TEST FOR ENOUGH RETURNS TO SATISFY NRETS
                                                                                                                                                                                                                                                                                                                                                                                ICHECK = NM-NRETS-ISTART
IF(ICHECK.LT.0) NRETS = NM - ISTART
IF(NRETS.LT.NSTAT) ICHECK = IFIRST-ISTART
                                                                                                                                                           - GARB(ILEN:ILEN+IEN-1)
                                                                                                      SHEY.
                                         60T0 793
                                                                                                                                                                                                         READ (9,*,END- 785) ISIC(I)
IF(ISIC(I).GT.99) ISIC(I) -
                                                                                   IEN ... 1
IF (GARB(ILEN+IEN:ILEN+IEN).NE.'
IEN ... 1EN + 1
GOTO 492
ENDIF
ILEN = ILEN + IEN + 1

IF (GARB(ILEN:ILEN).EQ.'

ILEN + 1

IF ((ILEN+3).GT.LENGTH)

GOTO 792

ENDIF
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 DO 801 J = 1,NRETS-NSTAT
READ(9,*)GARB
CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                 DO 800 J = 1,ICHECK
READ (9,111) GARB
CONTINUE
                                                                                                                                                        IDC(1)(6:6+1EN-1)
                                                                                                                                                                                 CONTINUE
           792
                                                                                              492
                                                                                                                                                                                                                                                                                                                                                                                                                                                         8
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          88
```

WO 91/02326		116	PCT/US90/04328
F(K.GT.NSTAT.AND.RET(K,1).LT1.0)THEN   RET(K,1)-0.005   ENDIF   EN	ENDII CLOSI RETUI NSTO NUM	CLOSE(9) 111 FORMAT (A40) 112 FORMAT (++,*,*STOCK # ',15,* IS ',A40) END C ************************************	C IFIRST IS FIRST MONTH OF DATA NEEDED FOR MATRIX C ILAST IS LAST MONTH OF SIMULATION C INCLUDE 'COMMON.F' READ IN BOND DATA C
			·
1F (*BONDS.GT.0)   THEN   OPEN (9,FILE = BONDFIL, STATUS = '0LD')	END IF  If (MRETS.LT.NSTAT) ICHECK = IFIRST-ISTART  DO 1000	CCNTI ENDIF CLOSE(9) RETURN	END OF SUBROUTINE BONDIN
U	5 5	1300	30 0

```
SUBROUTINE PORT
                                                                                                                                                                                                                    DO 1300 'I-1,NSTAT
CONTINUE
CONTINUE
                                                                                                                                                                                                                                                                                                                                           BEGIN OUTPUT PROCEDURES
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        CALCULATE THE PORTFOLIO
FIRST CALCULATE RETURNS
                                                                                                                                                                                                                                                                                                                                                                                            UANIM = 0.0
DO 129 I = 1,NRETS
UANIM = UANIM + ANIM(I)/REAL(WRETS)
                                                                                                                                                           RESET THE RETURNS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      .GT. 0.005) THEN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                           IFLAG(7)-1

X101-0.

X101-0.

X101-0.

X101-0.

X101-0.

X111E(***)

X111E(****)

X111E(****)
                                                                                                 INCLUDE 'COMMON.F'
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            IF (ABS(XTOT-1.0)
WRITE(***)
WRITE(***)
WRITE(***)
WRITE(***)
IFLAG(7)-2
RETURN
IF
                                                                                                                                                                                                        DO 1300 3-1,NUM
DO 1300 I-1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      END
CONT INUE
                                                                                                                                                                                                                                                                                          1300
                                                                                                                                                                                                                                                                                                                                                                                                                                                                              129
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            130
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       WRITE OUT THE NEW WEIGHTS TO A FILE CALLED 'OLD'
                                                                                                                                                                                                                                                                                                                                                                                PERIOD
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         NATIONAL INVESTMENT SERVICES SPANNING TECHNOLOGY'S SIMULATION RESULTS'
                                                                                                                                                                                                                                                                                                                                                                                                     DD E01 1-1,NSINS
PRET(1+NSTAT)-0.0
DO 901 J-1,NUM
PRET(1+NSTAT) = PRET(1+NSTAT)+CUM(J)*RET(1+NSTAT,J)
CONTINUE
JO 1001 K = 1,NUM
CUM(K) = CUM(K)*(1.+RET(1+NSTAT,K))/(1.+PRET(1+NSTAT))
CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             WRITE(10,*)' NATIONAL INVESTHENT SERVICES SPANNING TECHN
WRITE(10,*)'

                                                                                                                                                                                                                                                                                                                                                       NOW CALCULATE RETURNS AND WEIGHTS IN SIMULATION
DO 900 J = 1,NUM
PRE([] = PRET([] + RET([,J)*X(J)
CONTINUE
OBJ = 08J + (PRET([)-ANIH(]))**Z/REAL(NSTAT)
CONTINUE
CONTINUE
OBJ + (PRET([)-ANIH(]))/REAL(NSTAT)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           - 'OLD', STATUS - 'OLD')
                                                                                                                                                                                         IF 08J .GT. 0.0)THEN 08J-((08J-AVEDIFF**2)*12.)**(0.5)*100
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          OPEN(1), FILE-FILEOUT, STATUS-'UNKNOWN')
REWIND(10)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         WRITE OUTPUT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       OPEN(15,FILE - 'OLD', STA

REWIN(015)

DO 140 1 - 1,NUM

WRIT (15,940) CUM(1)*100

CONT. NUE

CONT. NUE

CLOSI (15)
                                                                                                                                                                                                                                                      083-99.9
                                                                                                                                                                                                                                                ELSE
                                                         8
                                                                                                                                        800
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 8
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     100
100
100
```

XRET-0.0  DO 131 1-1.NUM  If (IFLAG(9).EQ.2.AND.X(1).LT. 0.0001)GOTO 631  WRITE(10.16)1.X(1)*100.CW(1)*100,PART(1)*100,  A XRET - AVE(1) + WANIM  XRET - XRET + X(1)*VRE(1)  XRET - XRET + X(1)*VRE(1)	131 CONTINUE  16 FORWAT(1X,14,1X,2F6.3,F7.3,14,1X,A9,1X,A36)  XRET = XRET*12.0*100.0  WRITE(10,*)  WRITE(10,*)  G49 FORWAT(1X,* HINIMM STD DEV =',F10.4,* EXPECTED RETURN -',F10.4)  WRITE(10,*)	END OF SUBROUTINE PORT	C statestatestatestatestatestatestatestat	C ***** SET AVERAGES AND COVARIANCES TO ZERO ************************************	C **** GO AROUND STATISTICS IF NSIM < 3 IF (MSINS.LT.3)GOTO 318 C ***** CALCULATE AVERAGES ************************************
DO 260 I-NSTAT+1,IREAD AVE(1)-AVE(1)+AVIHIJ/REAL(NSIM) AVE(2)-AVE(2)+PRET(1)/REAL(NSIM) 260 CONTINUE CALCULATE COVARIANCES ************************************	DO 9:0 1-1,3 (AR(1)-0.0 10 950 K-NSTAT+1,1READ 950 CONTI (UE C ****** CALCULATE THE COVARIANCE MATRIX'S UPPER OFF DIAGONAL *****	DC 960 1-1,3 D0 960 3-1,8 D0 828 K-NSTA+1,IREAD CMT(1,3)=CMT(1,3)+((STAT(K,1)-AVE(1)) #(STAT(K,3)-AVE(3)))	CMAT(1,3)/REAL(NSIM-1) 960 CONTINUE CMAT(3,1) = CMAT(1,3) C ***** CALCULATE CORRELATIONS ************************************	DO 951 [-1,3 DO 951 J-1,1 DO 951 J-1,1 E(VR(I), LE. 0.0, GO TO 951 C(REL(I,J)-CMT(I,J)/(VAR(I)**,5*VAR(J)**,5) C ***** CALCULATE CURULATIVE RETURNS ************************************	IF(VAR(1). NE. 0.0) BETA - CMAT(1,2)/VAR(1)  ALPHA - AVE(2) - BETA*AVE(1)  SST - 0.0  SSE - 0.0  DO 952 I - MSTA+1, IREAD  SSE - SSE + (ALPHA+BETA*STAT(1,1)-STAT(1,2))**2  SST - SST + (ALPHA+BETA*STAT(1,1)-STAT(1,2))**2

98

986

FORBAT(1X, FORBAT(1X, FORBAT(1X, FORBAT(1X, FORBAT(1X, FORBAT(1X, FORBAT(1X,

*** 666 525 5 67 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6	E RUN ***********************************	TRACKER sestembles to best of sestembles to be sestembles to be ses	
FORMAT(1X, 9) NUMBER OF STOCKS FORMAT(1X, 1) STOCKS TO READ PAST FORMAT(1X, 11) NINIMIN STOCK HOLDING FORMAT(1X, 12) MAXIMIN STOCK HOLDING FORMAT(1X, 13) MAXIMIN STOCK HOLDING FORMAT(1X, 14) NSTAT FORMAT(1X, 14) NRTS FORMAT(1X, 15) BULLET FORMAT(1X, 17) TARGET FORMAT(1X, 17) TARGET	WRITE(10,*) OO 300 1-1, MSTAT WRITE(10,612)1+MM-(MSTAT+1),(STAT(1,3),3-1,3)	END OF SUBROUTINE TRACKER SUBROUTINE INDUST INCLUDE 'COMMUNE'S'	SIC(1) - 'AGRICULTURAL PRODUCTIOM-CROPS' SIC(2) - 'AGRICULTURAL SERVICES' SIC(3) - 'FORESTRY' SIC(3) - 'FISHING HUNTING AND TRAPPING' SIC(10) - 'MET'AL MINING' SIC(112) - 'ATHRACITE MINING' SIC(113) - 'ATHRACITE MINING' SIC(114) - 'MIN. A QUARRY, OF NOMET. MIN. SIC(115) - 'GONSTG. C. & O. B. 'CONSTG. CONSTG. C. & O. B. 'CONSTG. CONSTG. CO
100 100 100 100 100 100 100 100 100 100	1 OE		

PAPER AND ALLIED PRODUCTS'

PRINTING AND ALLIED PRODUCTS'

CHEMICAL AND ALLIED PRODUCTS'

PETROLEUM REFIN. A REL. PROD.

REBBER AND NISC. PLAST. PROD.

REMARY HETAL INDUSTRIES'

STONE CLAY GLASS A CONC. PROD.

REMARY HETAL PROD. EX. H. BT. E. '-
FAB. HATAL PROD. EX. H. BT. E. '
KLE. AND ELE. MACH. PROD.

RAILROAD TRANS. ENTING.

HISC. AND SUB. TRANS. AND WARE.

"MATER TEAMSPORTATION"

```
WE J GHT
                                                                                                                                                                                                                     133 I = 1,99

CUM(1) = 0.0

DO 134 3 = 1,NUM

IF (1SIC(J).Eq.1)

CONTINUE

IF (CUM(1).GT. 0.001) THEN

END IF

END IF
                                                                                                                                                                        *** INDUSTRY WEIGHTINGS
                                                                                                                                                                                                                                                                                                                                                            TOTAL
                                                                                                                                    WRITE OUT INDUSTRY
                                                                                                                                                                               WRITE(10,102)('*',K
WRITE(10,*)' CODE
WRITE(10,102)('*',K
                                                                                                                                                                                                                                                                                END
CONTINUE
                                                                                                                                                                                                                  00 133
                                                                                                                                                                                                                                                                                        133
                                                                                                                                                                                                                                                      134
                                                                                                                                                                                                                                                                                                                                       136
                                                                                                                                                                                                                                                                                                                                                                                           102
135
                                                                                                                                                                                                                                                                                                                                                                              SERVICES OF AMERICA'
                                                                                                                                                                                                                                                                                                                                                                      (c) NATIONAL INVESTMENT
1988'
                                                                                                                                                                                                                                                                                                    LIASUB *****
                                                  STATUS
S IBROUTINE LIABIN
                                                                                                                                                                                                                                                                                            END OF SUBROUTINE
                                                                                                                                         00 300 1 - 1, IFIRST-ISTART
READ (9,111) GARB
CON'INUE
                                          OFEN (9, FILE - LIAFIL,
                                                                                                                                                                             DO 100 I = 1, IREAD
READ (9,*) ANIM(1)
CONTINUE
                         TICLUDE 'COMMON.F'
                                                                                                                READ (9,*) ISTART
READ (9,*) ISTOP
                                                                                                                                                                                                                                                     FORMI (A40)
                                                                                          READ
COP TINUE
                                                                                                                                                                                                                                                                                                   C UPDATED 4/18/88
                                                                                                                                                                                                                  (6):ISOTO
                                                                                                                                                                                                                                    RETU! N
                                                                                              200
                                                                                                                                                              9
                                                                                                                                                                                                                                                     11
                                                                                                                                                                                                 400
```

WO 91/02326		132	PCI
WRITE(**) 'works. Those having access to this work may not copy.' WRITE(**) 'use, or disclose the information in this work unless' WRITE(**) 'expressly authorized by NISA to do so.' WRITE(**) ' WRIT	C ************************************	METER (MS-MD*M2-ND*1D, M3-NRT*ND, M4-NST*NS-NRT*NST)  ***********************************	C DATA (AVE(i),i=1,MD)/MD*0.0/ C DATA (COV(1,J),i=1,MST),J=1,MST)/M4*0.0/ C DATA (STAT(i,J),i=1,MRT),J=1,MST)/MS*0.0/ C DATA (COREL[i,J),i=1,MRT),J=1,MST)/MS*0.0/ C DATA (PRICE[i),i=1,MD)/MD*0.0/
DATA (VOL(1),1-1,ND)/ND*0.0/ DATA (VAR(1),1-1,ND)/ND*0.0/ DATA SFREAG(1),1-1,ND)/ND*0.0/ DATA SFREAG(1),1-1,ND)/ND*0.0/ DATA SFREAG(1),1-1,ND)/ND*0.0/  *********************************	FORTRETS. FORTRETS. ANSFER. GARB. FILEOUT.	######################################	ITYPE-0 ICHANGE-D NUM-O IREAD-0 IF IRST-0

ELSE IF (IRESPON.EQ.15) THEN  WRITE(*,135)  READ(*,*,5ND - 215, ERR - 215) NRETS  ELSE IF (IRESPON.EQ.16) THEN  READ(*,*,END - 216, ERR - 216) BULLET  ELSE IF (IRESPON.EQ.17) THEN  WRITE(*,137)  READ(*,*,END - 217, ERR - 217) TARGET	ELSE IF (JRESPON.EQ.18) THEN  MRITE(*138)  REAQ(*,*,END = 218, ERR = 218) TURN  END IF  GO TO 10	₹ # 55555		139 FORMAT('0', ENTER TARGET 138 FORMAT('0', ENTER TARGET 138 FORMAT('0', ENTER TARGET 139 FORMAT('0', ENTER TARGET 130 FORMAT('0', ENTER TARGET 130 FORMAT('0', ENTER TARGET 131 FORMAT('0', ENTER TARGET 132 FORMAT('0', ENTER TARGET 133 FORMAT('0', ENTER TARGET 134 FORMAT('0', ENTER TARGET 135 FORMAT('0', ENTER TARGET 136 FORMAT('0', ENTER TARGET 137 FORMAT('0', ENTER TARGET 138 FORMAT('0',
215 216 217	218	2 0011211	122 132 133 133 133 133 133 133 133 133	2
	E 'COMMON'E' TÜRNÖVER FACTOR TER (MAXTXT = 50,LINES = 24) TER HEAD*(MAXTXT),LAST*(MAXTXT),OPTIONS TER "30 PAST		READ 8, 101) FILEDOT READ 8, 101) STOKFIL READ 8, 102) MNSAFIL READ 8, 102 NNSAFI READ 8, 103 STOKKIN READ 8, 103 STOKKIN	RETURN (8)  CONTI (UE  GIVE OPTION TO READ FROM SCREEN WITHOUT DUMPING OUT OF  PIOGRAM OR TO READ FROM DIFFERENT FILE NAME  LAST = ' WARNING: THE PAST DATA FILE DOES NOT EXIST'  LAST = ' WARNING: THE PAST DATA FILE TO ABORT )'  NENOP = 2  OPTIONS(1) = 'INPUT NEW NAME FOR PAST DATA FILE'
		::		* * *

2 \*

20 CALL MENU (LINES,HEAD,LAST,NBROPT,OPTIONS,IRESPON) IF (IRESPON.EQ.1) THEN WRITE(*,100){', ', I = 1.5,	<sup>F</sup>	RETURN ENDSCRN END IF	RETURN 100 FORMAT('O', A1) 101 FORMAT(A15) 102 FORMAT(145)	103 FORMAT(F7.2) 104 FORMAT(' NAME FOR PAST DATA FILE ',S) END	SUBROUTINE REDSCRN	FOR THIS RUN	I LIABILI STOCK BOND FIRST	OF STOCK TO SO OF BONDS TO SO STOCKS TO SO STOCKS TO SO STOCKS TO SO	CK AND BOND	7.
(5', -	(\$', .	(\$°.	(\$*,	(3°,	••	(\$*,	(3',	. (8*,	(3,	.,5)
F)BHAT(*, 1) ENTER TITLE FOR SPANNING RUN R:AD(*, (A30)',END = 1,ERR = 1) TITLE	W!:ITE(*,102) F(RMA (' 2) ENTER OUTPUT FILE NAME READ(*,'(A30)',END = 2,ERR = 2) FILEOUT	WRITE(*,103) FOUNT(' 3) ENTER LIABILITY RETURNS FILE NAME RE.DQ**(',030)',END = 3.ERR = 3) LIAFIL WRITE(*,*)	WR! TE(*, 104) FOH MAT(*, 4) ENTER STOCK RETURNS FILE NAME REFO(*, (A30), END = 4,ERR = 4) STOKFIL H (STOKFIL, Eq.' ')STOKFIL = 'STOCKS. PRN' WRITE(*,*)	WRITE(*,105) FOR VAI(* 5) ENTER BOND RETURNS FILE NAME EALI(*,(A30), END	WRITE(*,*)' 6) ENTER YEAR AND MONTH TO BEGIN WRITE(*,106) FORMAT(*, SIMILATION (*, C.C.,	END - 6, ERR - 6) NHSAVE 1987 - 8702) -	WRITI(* 107) FORMIT(* 7) ENTER NUMBER OF MONTHS TO SIMULATE . READO END 7, ERR 7) NSIMS	WRITE(*, 108) FORMAT(' 8) ENTER NUMBER OF STOCKS TO USE READ(*, *, END * 8, ERR * 8) NSTOCKS WRITE(*, *)	09) 9) ENTER NUMBER OF BONDS TO USE END = 9,ERR = 9) MBONDS	(1) ENTER NUMBER OF STOCKS READ PAST
101 F )RHAT(") R:AD(";") WILTE(";")	2 WIJTE(*) 102 F(RNAT(*) READ(*)*	3 WRITE(*) 103 FO MAI(*) RE. DO(*)	4 WRITE(*,1 104 FOIMAT(', REFD(*,'( 1F (STOK) WRITE(*,*	5 WRITE(*, 1 105 FOR IAT(*, 1 REAL)(*, *(, 1 IF (BONDE WRITE(*, *)	6 WRITE(*,*) 106 FORMATE(*,10		7 WRITE (*, 10 107 FORMUT (*, 10 READI *, *, E WRITE (*, *)	8 WRITE (*, 10 108 FORMAT (' READ (*, *, EI WRITE (*, *)	9 WRITE (*, 109) 109 FORMA'(' 9) E READ(', *, END WRITE (*, *)	10 WRITE(*,110) 110 FORMAT(',10) READ(*,*,END
					~ ~	•		₩-	o =	==

WRITE(*,*)  MRITE(*,11) FORMAT(*,11) RADO(*,*,END = 11,ERR = 11) STOCKHOLDING - % '.5) WRITE(*,*)	12 VRITE(*,112) ENTER MAXIMUM INDUSTRY HOLDING 5) FORDIA**, EKD 12, ERR 12) YIMAX WRITE(*,*) RETURN 100 FORWAT(ASS)	END END END OF SUBROUTINE REDSCRY, SUBROUTINE DISPLAY	A MISSERVE SON TO SERVE SON TO
FORUT(1X, 2) FORUT(1X, 3) FORUT(1X, 4) FORUT(1X, 4) FORUT(1X, 6) FORUT(1X, 6) FORUT(1X, 6) FORUT(1X, 6) FORUT(1X, 6)	109 FORMA (1X, 10) STOCKS OF BONDS 110 FORMA (1X, 10) STOCKS TO READ PAST 111 FORMA (1X, 11) HINNUM STOCK HOLDING	Formal (1X, 18)	THE FILE FOR LATE  1,7)  116 DATA TO FILE  1,5)  DAT', STATUS

101 FORMAT (A35) 102 FORMAT (F7.2) 103 FORMAT (F7.2) 104 FORMAT (**, A50)	END ************************************	CARRARAMENTAL CONTRACTOR CONTRACT	* ** PURPOSE: TO PRINT A NEKU AND READ RESPONSE	* ** HEADER TITLE OF SCREEN  * ** HEADER TITLE LINE OF WENU  * ** LAST LAST LINE OF MENU  * ** NRROPT WANBER OF OPTIONS	LIST OF DIMENSION OF CHARAC CALLING	* ** OVERALL SPECIFICATIONS IMPLICIT REAL (A-2) INTEGER MAXTXT * ** PARAMETER (MAXTXT = 50)	* ** CALL SPECIFICATIONS CHARACTER OPTION(*)*(MAXTXT), HEADER*(MAXTXT), LAST*(MAXTXT) * ** INTEGER NBROPT, RESPON, LINES * ** LOCAL SPECIFICATIONS * ** INTEGER 1, IMAX		- 1. IMAX
10 WFITE(*,*)' ' * ** PRINT HENU WRITE(*,*)HEADER WRITE(*,*)	DO 20 I = 1,NBROPT WR.TE(*,(1X,12,2H) ARTTE(*,*)OPTION(1)	:	* ** BLAVK OUT REST OF SCREEN  DO 25 I = 1, IMAX  25 WRITE(*,*)'	30 WRITE(*.99) 999 FORMAT(* SELECT NUMBER OF OPTION> '.\$) *** RESPINSE SET TO ZERO IN CASE OF CARRIAGE RETURN	READ (*,'(12)',END = 40,ERR = 5) RESPON IF (RESPON.LT.O.OR.RESPON.GT.NBROPT) THEN h RIFE(*,*)' OPTION OUT OF RANGE' G 170 30	END OF SUBROUTINE MENU examinations of SUBROUTINE MENU examinations of STEP UP PROBLEM FOR OPTIMIZER examinations of STEP STORE SOLVE SOLV	WRITE(*,"('+',A50)")'IN SOLVE'  C ****** SET THE MAXIMUM SIZE FOR THE OPTIMIZER ************************************	C *******   SOLVE COUNTS THE NUMBER OF RUNS, ICOUNT THE ITERATIONS *** ICOUNT 0 ITEST 0	C ******* CALL BOUNDS TO SET INDUSTRY AND SECURITY BOUNDS *********

CALC COVARS \*\*\*
FOR OUTLIER REMOVAL AT START TO NEXT POINT FUNCTION 1 OBJECTIVE FUNCTION CALL STARTPT \*\*\*\* CALL COVAR:INITIALIZE LI(I), CALC AVERAGES,
\*\*\*\* IFLAG(S)-1 FOR FULL COVARIANCE, IFLAG(S)-2
IF(IFLAG(S)-E0.1)THEN
ELSEIF(IFLAG(S)-E0.2)THEN
CALL COVAR OBJECT IVE ICOUNT - ICOUNT + 1
DELTA - 100.
08J1 - 08J + 1000.
IF (08JLAST .NE. 0.0) THEN
DELTA - -100.\*(08J-08JLAST)/ABS(1+08JLAST)
END IF TO CALCULATE CALL CALCOBJ CALL CALCOBJ OBJLAST - 08J CONTINUE EXOIF ----C seeker 666

IF (ICOUNT .EQ. ICNT+1) THEN (DELTA .LE. DELSTAR) THEN ICNT - ICOUNT ITEST END IF ELSE 4

WRITE(\*, "('+', 12X, 215, A15, F10.5, A15, E10.5)")
A | 150LVE, ICCUMT, 'OBJ - ', OBJ1, 'DELTA(X)

IF (DELTA .LT. 0.0) THEN DISTMAX \* 0.4

TO BE REPRESENTATIVE REP OF SAP ANNUAL

UP PORTVAL 1 SCILLARS ARE 몵

BOUNDS...

WRITE(\*,"('+',A50)")'IN

ANDREAS END OF SOLVE SUBROUTINE BOUNDS INCLUDE 'COMMON.F' DAYSVOL-XCONS(2) PCNT-XCONS(3)

END

RETURN

DOLLAR

CALL BOUNDS

2

NBEST DO 10

| IF (ITEST . ST. 20 . OR. DISTMAX . LT. 0.00005)
| CALL PARTAL
| IF (OLIVERAL . TEMHINAL SIPE SIPE STATE

RETURN ENDIF

GO TO 999. END 1F 02 02

```
C ******* PCNT - PARAMETER FOR MAX HOLDING IN A COMPANY: 4% ******* C ******* DAYSVOL - PARAMETER FOR MAX # TRADING DAYS IN A STOCK *****
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            至
                                                                                                                                                                                                                                                                                         VECTOR ********
                                                                                                                                                                                                                                                                                                                   (XMKTCAP(I) .GT. 0.) THEN
IF ((PCHT/100.)*1000.*XMKTCAP(I)/PORTVAL
RHSMAX = (PCHT/100.)*1000.*XMKTCAP(I)/PORTVAL
END IF
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                PORTVAL
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               BY USING
                                                                                                                                                                                                                                                                               RHS(1) IS THE RIGHT HAND SIDE CONSTRAINT RHS(1) = 0.0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            INVESTED IN A STOCK 1.0E+9) THEN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         - 0.0055 - (5.0E-12)*PORTVAL
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      © 0.0005
| PORTVAL .LT. 1.0E+8) THEN
| © 0.005
                                                                                                                                                                                                                                             UP RHS VECTOR
                                                                                                                                 BOUNDS AND PORTVAL
         IF (NYSAVE.GE. 8401) PORTVAL-PRTVALS*
IF (NYSAVE.GE. 8501) PORTVAL-PRTVALS*
IF (NYSAVE.GE. 8001) PORTVAL-PRTVALS*
IF (NYSAVE.GE. 8701) PORTVAL-PRTVALS*
IF (NYSAVE.GE. 8801) PORTVAL-PRTVALS*
IF (NYSAVE.GE. 8901) PORTVAL-PRTVALS*
                                                                                                     IF (PORTVAL.EQ.0)PORTVAL-100000000.0
                                                                                                                                                                                                                                             SET
                                                                                                                                                                                                             DO 10 1 - 1, KUM
                                                                                                                                WRITE(*,*)' IN
WRITE(*,*)
                                                                                                                                                                                                                                                                                                                                                                                                                                                         END END
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         END I
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               ELSE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   Ŧ
                                                                                                                                                                                                                                                                              -----
                                                                                                                                 υU
                                                                                                                                                                                                                63 .OR. ISIC(1)
                                                                                                         (2) - SUM OF SIC CODES 48,49 LT INDUSTRY BOUND ******
IF (3 .Eq. 2) THEN
IF (151C(1) .Eq. 48 .OR. ISIC(1) .Eq. 49)CONS(3,1)
END IF
                                                                                                                                                                         (3) - SUM OF SIC CODES 60,63,67 LT INDUSTRY BOUND IF (3, Eq. 3) THEN IF (1SIC(1) Eq. 60 .OR. ISIC(1) .Eq. 63 .OR. END IF
                                                                                                                                                                                                                                                                                                                                       SET TYPES
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  SUBROUT INE
                                                                                                                                                                                                                                                                                                                            IGHT HAND SIDE FOR CONSTRAINTS
1,000
1,000
1,100
1,100
1,100
1,100
                                                                                                                                                                                                                                                                                                                                                                                                              UP XLHS VECTOR
                                                                  (1) ... SUM OF THE WEIGHTS EQUALS
IF (3 .EQ. 1) CONS(3,1) ... 1.0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               CALCULATION
                                                                                                                                                                                                                                                                                                                                                                                                                SET
                       DO 20 J = 1, 10
CONS(J,I) = 0.0
                                                                                                                                                                                                                                                                                                                                                                                                                               IF(IFLAG(2).EQ.1)THEN
D) 30 1-1,NUM
XLHS(1)-0LDMT(1)
C,NTINUE
ELSEIF(IFLAG(2).EQ.2)THEN
D) 40 1-1,NUM
RHS(1) - RHSMAX
                                                                                                       (2)
IF
                                                                                                                                                                                                                                                           CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                C NT INU
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    CONT. NUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       RETURN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             ENDIF
                                                             .......
                                                                                                         -----
                                                                                                                                                                                                                                                                                                                                                                                                                                                                          3
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               $
                                                                                                                                                                                                                                                        20
                                                                                                                                                                                                                                                                               2
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INCLUDE 'COMMON'F'	WRITE(*,"('+',ASO)")'IN COVAR' C ******* INITIALIZE LI(!), CALC AVE(!), CALC COV(!) ************************************	DO 10 I = 1, MUM C LI(I) VECTOR ************************************	AVE(1) = 0.0 COV(1) = 0.0	Eq. 1, NSTA1 Eq. 1) NIM UAN RANIM V F	20 CONTINUE COV(I) + RET(3,1)**NANH(3)*TARGET	IF (1 EQ. 1) THEN UANIM - UANIM - NEAL(NSTAT)  END IF AND IT AND	RETURN	END C SUBROUTINE COVAR C C C C C C C C C C C C C C C C C C C	<pre>INCLUDE 'COMMON.F' WRITE(*,*('+',A50)*)'IN STARTPT' : ************************************</pre>
C ********  :IRST SORT THE COVARIANCES ************************************	25 CONTINUE  25 CONTINUE  25 CONTINUE  26 CONTINUE  27 CONTINUE  28 CONTINUE  28 CONTINUE  29 CONTINUE  20 CONTINUE  20 CONTINUE  30 CONTINUE  31 CONTINUE  32 CONTINUE  33 CONTINUE  34 CONTINUE  35 CONTINUE  36 CONTINUE  37 CONTINUE  38 CO	DO 30 O 141, MON LIF (COV(LI(1)) THEN LITEMP LI(1) LI(1) LI(2) LI(1) LITEMP	30 CONTINUE	NBEST 10 NBEST 10 THE X() VECTOR AND SWITCH THE LI() VECTOR	C ****** FILL X(I) IF NOT CONSTRAINED ************************************	SLOW W = RHS(LI(J))-KUHS(LI(J))  D	50 CONTINUE	C ******* SEI THE VARIABLE = TO THE MOST SLACK AVAILABLE ************************************	NBEST - NBEST + 1 LITEMI - LI(NBEST) LI(NBST) - LI(J) LI(J) - LITEMP X(LI(NBEST)) - SLKWAX + X(LI(NBEST)) XO(LI(NBEST)) - SLKWAX + X(LI(NBEST)) IF (SLK(1) .LE. 0.00001) RETURN

```
IF (IFLAG(4) .EQ. 2) THEN MOVING QUARTERLY CALCULATIONS DO 5 I - 3, NSTAT PRET(I) - 0.0
                                                                                                                                                                                                                                                                DO 6 J = 1, NUM

IF (X(J) .GT. 0.0) THEN

PREI(1) = PRET(1) +

X(J)*((1+RET(1.J))*(1+RET(1-1,J))*(1+RET(1-2,J))-1.)

CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                          END IF FOR MOVING QUARTERLY
                                                                                                                                                                                                                                                                                                                                               PRET(I) - PRET(I) - (1+ANIM(I))*(1+ANIM(I-1))*(1+ANIM(I))*(1+ANIM(I))*(1+ANIM(I-2))-1.)*TARGET PAVE - PRET(I)/REAL(NSIAT-2)
                                                                                                                                                                                                                                                                                                                                                                                                                                        - PAVE**2 - PAVE*BULLET
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                FOR MONTHLY RETURNS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    DO 20 J = 1, NUM
IF (X(J) .GT. 0.0) THEN
PRET(I) = PRET(I) + X(J) * RET(I,J)
CONTINUE
                                                                                                                                        CALCOBJ
                                                                                                                                                                                                                                                                                                                                                                                                                   OBJ - VARPORT / REAL(NSTAT-2)
OBJS - OBJ
C *******
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     JF (IFLAG(4) .EQ. 1) THEN DO 10 I - 1. NSTAT PRET(1) - 0.0
                                                                                                                                WRITE(*,"('+',A12)")'IN
                                                                                                                                                        PAVE 0.0
VARPORT 0.0
COVPORT 0.0
      CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                          CONTINUE
                                                                                                                                                                                                    . ********
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           -----
       $
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  2
                                                                                                                                                                                                                                                                             *******************
                                                                                                                                                                                                                                                                                                                                               WR)TE(*, "('+', A12)")'IN PARTIAL ...' COV1, 3)). BUT THIS ... COV1, 3)). BUT THIS ... C ******** COV(1,P) WHER P IS THE PORTFOLIO RETURN. ... CALCULATE PORTFOLIO RETURN.
                                                                                                                                                                                                                                 +1.0E-7)
                                                                                                                                                                                                                                                                IF TURNOVER IS A FACTOR ADD IN ITS COST
                                                  (18J) = VARPORT / REAL(NSTAT) - PAVE**2 - PAVE*BULLET
(18JS = 08J
(1700 IF
                                                                                                             END IF FOR HONTHLY
                                                                                                                                                                DO 30 I = 1, MUM
OBJ = 0BJ + TURN*( ((X(1)-OLDWT(1))**2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                       IF (0BJ2 - 0BJ .LE. 0.0001*EPS) NTEST - -1
PRET(1) - PRET(1) - ANIM(1)*TARGET
PAVE + PRET(1)/REAL(NSTAT)
VARPORT - VARPORT + PRET(1)**2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  IUMB INT(1.1*REAL(NBEST))
F (NIMB GT. NUM) NUMB
F (NTEST GT. 8) NTEST
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             IF (NTEST .LE. 0) THEN
                                                                                                                                                                                                                                                                                                                                                                                                              DO 10 I = 1, ID

$LK(I) = RMS(NUH+I)

RC(I) = -9999.

CON INUE
                                                                                                                                                   IF(TURN.GT.0)THEN DO 30 I = 1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           NTES! - NTEST + 1
                                              CONTINUE
                                                                                                                                                                                                EIDIF
                                             2
                                                                                                                                                                                    8
                                                                                                                                                                                                                                                                                                                                                                                                                                                 2
```

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· x((1)))
                                                                                                 IF MOVING QUARTERLY RETURNS
                                                                                                                                                                                                                                                                                                                                                                                                                          STOCK
                                                                                                                                                                                                                                                                                                 PART(L1(1))-2.0+(PART(L1(1))/REAL(NSTAT)-RAVE+PAVE)-RAVE+BULLET
                                                                                                                                                                                    PART(LI(I))=2*(PART(LI(I))/REAL(NSTAT-2)-RAVE*PAVE)-RAVE*BULLET
                                                                                                                                                                                                                END MOVING QUARTERLY
                                                                                                                                                                                                                                                                                                                                                                                                                      FIND WORST PARTIAL FOR A POSITIVE WEIGHT
                                           - SLK(K)
                                                                                                                                                                                                                                                                                                                                              IF TURNOVER IS A FACTOR ADD IN A COST
                                                                                                                                                                                                                                                                                                                             END MONTHLY
                                                                                                                                                                                                                                    IF HONTHLY
                                          .EQ. 1.0) SLK(K)
                                               CONTINUE
END IF
                                                                             PART(L1(1))
RAVE - 0.0
             DO 20 1 - 1.
IF (X(L1(1)
DO 30
                                                                                                                                                                                                                                                                                                                                                                                                                                                                              2
                                                                                                                                                                                                                                                                                                                                                                                                                              2
                                                                                                                                                                                                                   . ......
                                                                                                                                                                                                                                                                                49
                                                    39
                                                                                     SLK(K) .LT. 100.*EPS)THEN
                         F (Q.LT.PART(LI(JHEAP)))THEN
                                  NBEST = 0
00 60 1 = 1, NUMB
                                                                                                CONTINUE
                                                                                                                                                                                                                                                                                                                      ELSE
CONTINUE
                                                             18
18
18
18
18
                                                                                                                                                               END LIA
                                                                                                                                                                                         CONTINU:
                                                                                                        ۶ ِ
22
                                                                                                                                                                                                                                                                                                                                                                                                                                120
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THEN
                                                                                                                                                                                               CONS(K, LI(1B)). Eq. 0.0)
                                                                                                                            8
                                                                                                                                                                                                                                                                                                                                                                                                        WORST INTO BEST
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      . EPS) 60 70 5
.6T. 0.5*01STXI)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    00 00
                                                                                                                                                                                                                                                                                                                                                                                                                               8
2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           TO RHS AND TOTAL HO
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               .LE. PART(LI(1)))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       (SLK(K).LT.EPS) GO TO 5
                                                                                                                                                                                                                                                                                                                                                                                                                              .LT. EPS)
                                                                                                                                                                                                                                                                                                                                                               MROVES - 0
TOTDIST - DISTMAX
PMAX - 9999-
***** BEGIN THE HOVE BY MOVING OUT O
DO 10 1 - 1, NBEST
IF (RHS(LI(1)) - X(LI(1)) . LT. EPS]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  TEST PROXIMITY TO RHS AND TOTAL
IF (X(L1(1B)) -XLHS(L1(1B)) .LT.
IF (ABS(XO(L1(1B)) -X(L1(1B)) .E.
                                                                                                                                                                                                                                                                    INCLUDE 'COMPRUN.F
PARANETER ( EPS = 0.000001)
WRITE(*,"('+',A12)*)'IN HOVE_X
                                                                                                                                                                                                                                                                                                                    DISTMAX = DISTMAX * 1.05
IF (DISTMAX .GT. 0.4) DISTMAX
DISTXI = 0.15 * DISTMAX
           LI(IHEAP)-LI(JHEAP)
INEAP-JHEAP
JHEAP-JHEAP
                                                                                                                                                                                                                                                                                                                                                                                                                                                           IB - IB - 1
IF ( IB .LE. 1) GO TO 10
                                                 JHEAP-IR+1
                                                                                           ENDIF
LI(IHEAP)-INDXT
0 110
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             IF (PART(LI(18))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     SLKHAX
DO 20 K
                                                                                                                   GOTO 110
CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  ---
                                                                                                                                                                                                                                            IF (XO(LI(18)) .GT. OLDWT(LI(18)) .AND.
X:LI(18))-OLDWT(LI(18)) .LT. DİST )DIST-X(LI(18))-OLDWT(LI(18))
                                                                                                                                                                    F (RHS(LI(I))-X(LI(I)).LT.DIST)DIST-RHS(LI(I))-X(LI(I))

IF (TURN GT. 0.0) THEN

IF (XO(LI(I))

LT. OLDWT(LI(I)) .AND.

OLDWT(LI(I))-X(LI(I)) .LT. DIST-OLDWT(LI(I))
                                                                                                                                                →→ IF THE WORST VARIABLE STILL HAS SLACK, REDUCE IT ↓ (ABS(XO(LI(I))-X(LI(I))) .LT. 0.5*DISTXI ) 60 TO
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   ) SLKWAX - SLK(K)
                                                                                                                                                                                                                                                                                                                                                                        CHANGE THE X VECTOR AND THE CONSTRAINTS
                                                                                        DP = (PARI(LI(IB)) - PARI(LI(I)))*10.
IF (DP .LT. DIST) 01ST = 0P
                                                                                                                          IF (SLKMAX .LT. DIST) DIST - SLKMAX
                                                                                                                                                                                                                                                                                                               60 70 8
                                                                (DIST .LT. 0) WRITE(*,*)'1'
                                                                                                                                                                                                                                                                                                                                    60 70 5
                                            FIND LARGEST MOVE POSSIBLE
                                                                                                                                                                                                                                                                                                                                                 IF (DP .GT. PMAX) PMAX = DP
                                                                                                                                                                                                                                                                                                                                                                                                   - X(L1(1B)) - DIST
- X(L1(1)) + DIST
(SLK(K).LT.SLKMAX
                                                                                                                                                                                                                                                                                                      IF (DIST .LT. 0.0001*EPS)
                                                                                                                                                                                                                                                                                                                            IF (OP .LT. 0.1*PMAX)
                                                                                                                                                                                                                                                                                                                                                                                                                               DO 30 K ... 1, 1D

IF (CONS(K,LI[18])

IF (CONS(K,LI[1])

IF (SIK(K) ..T. E

CON: INUE
                                                                                                                                                                                                                                                                                  E1.0 1F
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  CONTINUE
                                                                                                                                                                                                                                                                                                                                                                        -
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             *******
                    2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                              30
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               2
```

```
AVE(1) = AVE(1) / (REAL(NSTAT)-2.)
COV(1) = COV(1) / (REAL(NSTAT)-2.)
CREATE VECTOR OF COVARIANCES
                                                                                                                                 IF (RHS(LI(1))-X(LI(1)) ... EPS) X(LI(1)) .. RHS(LI(1)) IF (X(LI(1))-XLHS(LI(1)).LI.0.01*EPS)X(LI(1))-XLHS(LI(1))
                                                                                                                                                                                                                                                                                                                                                                                                                                                               + RET(J, I)
+ RET(J, I)*ANIM(J)*TARGET
                                                                                                                                                                                                                                                            OPEN(13,FILE='TENP.PRN',STATUS='UNKNOKN')
                               00 50 I - 1, NBEST
                                                                                                                                                                                                                                                                                 DO 10 1 - 1, MUH
                                                                                                                                                                                                                                                                                                                                                                            $ $ 8
                                                                                      CONTINUE
           CONTINUE
                                                                                     8
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                2
                                                                                                                                                                                                                                                                                                 *****IF THIS IS A SINGLE RUN READ WEIGHT FILE SPECIFIED
                                                                                                                                                                                                                                                                                                                                                                                                      SPAN.WET CONTAINS PORTFOLIO # ', VALUE
                                                                                                                                                                                                                                                                                                                                        PORT. MTS
                                                                                                                                                                                                                                                                                                                                                                      E - WIFILE, STATUS - 'OLD', ERR-999)
END - 888) SYMBL, VALUE
                                                                                                                                                                                                                        RESET OLD WEIGHTS TO 0
                                                                                                                                                                                                                                                                                                                                      ENTER FILENAME CONTAINING
                                                                                                                                                                                                                                                                                                                                                                                                                                                                           END - 888) SYMBL, VALUE
WRITE(13,*)1, COV(1)
                                                                                                                                                                                                                                                                                                                                                                                                                                - 888)GARB
                                                                                                               CHARACTER*9 SYMBL CHARACTER*30 GARB2,WTF1LE
                                                                                                                                                                                                                                                                                                                          IF(IFLAG(1), EQ. 1) THEN WRITE(*,*)' EN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             NIDC - 1
ICASH - 0
PORTVAL - 0.
                                                                                                                                                                                                                                        DO 234 1-1, NUM
0LIMT(1)-0.0
CONTINU:
                                                                                                                                                                                                                                                                                                                                                                                                                                1,*, END
                                                                                                                                                             INCLUDE
                                                                                 뎚
                                                                                                                                                                                                                                                                 234
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       888
                                                                                                                                                                                                                                                                                                                                    666
                  245
```

- 1 - 18€

:

VCOV(1,K)-COV(1)
WRITE(\*,\*)' K L HELD OUT AND COV(1)',K,L,COV(1)

DO ... 0 1-1,NIDC

```
135
                                                                                                                                                                                                                                                                                                                                                                                                                                                          IF MULTI RUN (STD) READ WTS FRO LST RUN
                                                                                                                                                                                                                                                                                                                                                                                                                             CONT INUING
                                                                                                                                                                                                                                                                                                                                                                    NOT INCL IN RET FILE'
                                                                                                                                                                                                                                                                                                                                                                                                                           NT FOUND. PROG
                                                                                                                                                                                                                                                                           THEN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   FORCED SELLS') THEN
                                                                                                                                                       IF (ICASH .EQ. 0) THEN WRITE(*,*)'NO CASH INCLUDED....PROGRAM STOP ENDIF
                                                                                                                                                                                                                                                                         .Eq. IDCSYM(1))
                                                                                                                                                                                                                                                                                                                              .r (17EST .EQ. 0) THEN
1DCTEST 1
1 HRITE(*,*)10CSYH(1),':SYHBL
CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      NUMBER OF OLDSTK
                                                                                                                                                                                                                                                                                                                                                                                                         IF (IDCTEST.EQ.1) THEN WRITE(*,*)NIDC-NCOUNT-1,'SYMLS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                            ELSEIF (IFLAG(1).EQ.2)THEN
IF (1SKIP.GE.1)THEN
IF (1SKIP.GE.1)THEN
OPEN(11.FILE = OLDFILE,STATUS
ERAD(1).102)GARB2
FORMAT(A25)
IF (GARBZ.EQ.') TOTAL FORCI
                                                                                                                                                                                                                                                                                                                                                                                                                             ENDIF
CLOSE(11)
                                                                                                            ENDIF
CONTINUE
PRTVALS-PORTVAL
                                                                                                                      2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         102
                                                                                                                                                                                                                                                                                                                            2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                ວ<u>ເ</u>
                                                                                                                                                                                                                                                                                                                                                                                    2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            TO PRINT OUT IN TRADE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             NOT INCL IN RET FILE'
                                                                                                                                                                                                                                                                                                                                                                                                                          OLDYT(J) = VAL(I)
OLDTOT-OLDTOT-OLDYT(J)
WRITE(*,*)' SYMBOL FOUND ',IDCSYM(I),OLDWT(J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 NOT FOUND', IDCSYM(I), VAL(I)
                                                                                                                                                           ) 91 1-1, NYAXX

RE.ID(11, 92) ITEMP, TEMP1, VAL (ITEMP), TEMP2, ITEMP2,

IF (TEMP1, GT. 0. 0001) THEN

NCOUNT-MCOUNTY,

VAL (NCOUNT)-VAL (ITEMP)/100.0

IDCSYM(NCOUNT)-IDCSYM (ITEMP)

IDCSYM(NCOUNT)-IDCSYM (ITEMP)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         OF IDCSYH() &VAL
                                                                                                                                                                                                                                                     ENDIF

REVIND(11)

DO 90 1-1,10

RIAD(11, (A1),)GARB

CONTINIE

DO 109 1-1,NHAX

VAL(1)-0,0

IGESYH(1)-''

NCOUNT-0

DO 91 1-1,NHAX
                                   G 3T0 101
                                                                                                                                       109
105
                                                         8
                                                                                                                                                                                                                                                               322
```

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E 00;

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ENDIF
              CONTINUE
21
                    WRITE(*,*)' WARNING OLDWTS TOTAL < .99, CONTINUING WRITE(*,*)' OLDTOT = ',OLDTOT
              IF (OLDTOT.LT..99) THEN
              ELSEIF(OLDTOT.GT.1.01)THEN
                                    WARNING OLDWIS TOTAL > 1.01, CONTINUING
                    WRITE(*,*)'
WRITE(*,*)'
                                      OLDTOT = ',OLDTOT
              ENDIF .
              NGONE=NCOUNT
              IF (IDCTEST.EQ.1) THEN
WRITE(*,*)' A TOTAL OF ',VALTURN*100.0, '% OF PORT SOLD'
WRITE(*,*)NGONE,'SYMLS NOT FOUND, PROGRAM CONTINUING'
              ENDIF
                                                      IF THE 1ST TIME THROUGHT SET OLDWT()=0
C
           ELSEIF(ISKIP.EQ.1)THEN
              DO 98 I=1,NUM
                    OLDWT(I)=0.0
  98
              CONTINUE
           ENDIF
                                               IF MULTI RUN (&OLD) READ WTS FRO OLD.
C
        ELSEIF(IFLAG(1).EQ.3)THEN
              OPEN(21, FILE = 'OLD', STATUS = 'OLD')
DO 94 I = 1, NUM
                    READ(21,*)OLDWT(1)

IF (TURN.EQ. 0.0)OLDWT(1)=0.0

THIS NEXT LINE ADDED 4/18/89

OLDWT(1)=0.0
C
                    OLDWT(I) = OLDWT(I)/100.
C
              CONTINUE
94
C
              CLOSE(21)
        ENDIF
        RETURN
        END
                                         OF
                                              SUBROUTINE
                                                               HOLDING
```

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## APPENDIX V

REINVESTMENT OF AVAILABLE CASH BEGINNING FROM CURRENT PORTFOLIO HOLDINGS

IMPROVED SYTEM ANALYSIS: RE-INVEST DIVIDEND FLOWS SIMULATION RESULTS EXAMPLE RUN LIABILITY STREAM USED: EXAMPLE LIABILITY START END SPAN NUMBER WGHT WGHT SENSIT SIC IDC TICK SECURITY NAME	3.475 3.475 1.024 27 GEN GTE 1.693 1.693 1.088 48 SBCA SBC 2.196 1.194 37 BA BA 3.508 3.508 1.021 20 K 0.031 0.031 1.052 56 LINT LTD 0.041 0.041 1.598 34 WAS MAS 1.475 1.475 0.702 67 FBG1 ON 2.680 2.680 1.295 29 PZL PZL	0.883 49 DTE DTE DETROIT F 0.926 49 BRE BGE BALTHORR 1.069 61 FUN FTU FIRST UN 1.276 29 ASH ASH ASHLAND 0.973 49 WPC WEC WISCONSIN 0.773 60 ANN ANNANSON	2.761 2.761 1.043 12 PEL PEL 2.761 2.590 2.690 0.881 49 IPC IPC 2.726 2.726 0.831 67 NES NES 0.563 0.563 0.957 49 TSG TEP 1.142 1.142 1.068 7 TELH IFL 1.187 1.187 1.070 75 AGNC AGNC 0.819 0.899 49 ATA ATG	2.698 2.698 1.082 30 BDG BDG BANDAG INC COM 0.451 0.451 1.349 32 BALL BLL BALL CORP CORP 2.909 2.909 0.882 85 BSTOW EDISON COM 1.155 1.155 0.909 67 CALH CAL CALFED INC COM 1.700 1.700 1.058 73 CMCS CMCSAT CORP CL A NASD INDL 2.093 2.093 1.678 35 LANS COWS 3COM CORP COM NASD INDL 1.190 1.190 1.131 67 FPA FPA FIRST PA CORP COM 3.346 3.346 0.754 67 HCP HCP HEALTH CARE PPTY INVS INC COM	2.418 2.442 1.045 8 1P1 1P1 2.442 2.442 2.442 1.045 8 1P1 1P1 0.182 0.182 0.935 49 KAN KAN 0.182 0.535 0.535 0.1896 65 KOG KOG KOG 0.535 0.535 0.185 52 LCI LOW 3.207 3.207 0.895 45 SAR1 LUV 3.207 3.207 0.895 45 SAR1 LUV 3.205 3.205 1.184 36 NPK NPT 1.238 1.238 0.994 49 IPS RME 1.235 2.755 0.994 47 KCPA RCP 0.846 0.846 1.181 23 RML RML 1.156 1.256 1.256 0.889 49 SIG SIG SIG
D SHARED MED SYS CORP COM QUESTAR CORP COR TEJON RANCH CO DEL COM CU S HEALTHCARE INC COM UNITED STATES SURGICAL CC WASHINGTON GAS LT CO COM WASHINGTON REAL ESTATE IN MCN CORP COM	<b>2</b>	115	0.00 0.00 % % %	0.00 ** ** ** ** ** ** ** ** ** ** ** ** *	. LIR RET PRIN IT
1.035 73 SHED SHED SH 1.086 38 MFS STR QU 1.353 1 TEJN TRC TE, 1.138 80 USHC USHC U (1.00) 0.947 49 MGL WGL MAS 0.995 67 MRE WRE MAS 0.930 49 MFRS MCN MCR	TRACKER OUTPUT FILE  MONTH LIA PORT DIF  "UMMULATIVE VALUES OF LIABILITIES AND ASSETS  HONTH LIABILIES PORFFOLIO	5 8	0.000000 0.000000 0.000000 0.000000 0.000000	RETURNS: MEAN 1ABILITY 0.00 % ORTFOLIO 0.00 % FFERENCE 0.00 % PARAMETERS FOR THIS RUN WERE:	E AOS 7/28/85 temp.nlb temp.nlb trinkosyze \RETYGONDS.
295 2.372 2.372 2.972 2.96 1.889 1.889 2.29 2.29 2.29 2.29 2.29 2.29 3.406 3.406 3.406 3.375 1.375 3.01 1.844 1.844 3.02 1.262 1.262 MINIMUM STD DEV •	TRACKER OUTPUT FILE MONTH LIA "UMPULATIVE VALUES OF	115 -0.005  ********* STATIST STATISTICS BASED ON	ALPHA BETA STD ERR CORRELATION R-SQUARED	ANNUAL RETURNS: LIABILITY PORTFOLIO DIFFERENCE PARAMETERS FOR	SPANNING RUN TITLE  DUTPUT FILENAME  SOLVENT FILENAME  STOCK RETURN FILE  MONTH SIMULATION BEGIN  NUMBER OF NONTHS SIMULATION  NUMBER OF STOCKS  NUMBER OF STOCKS  NUMBER OF BONDS  MUMBER OF BONDS  MAXIMUM INDUSTRY HOLDING  MAXIMUM INDUSTRY HOLDING

OF STOCK IN PORTFOLIO
-----------------------

OIF		0.23945386	0.00/459387	0.01589187	0.00701425	0.0399//38	0.01836689	0.00039821	0.01437908	0.00115482	0.00177903]	0.010773561	0.014289347	0.007060922	0.013620499	0.027462026	3.017530575	0.013141470	0.000298861	0.072932615	1 053411227
PORT	0.0048044603	.1450983137	.0324543230	0913652703	0246/64552	0243650582	0054894658	0558000170	0200813692	0000485850	0430007204	0263595097	01/6053215	0229464527	0407870896	000/46/365	0284809042	0394087993	0458422191-	054350942-	34861132RD
LIA	0235312600	.0943555534	.0178604499	0754733980	04503561932	0287487004	0128774298	0561982282	0344504515	0011062390	044//9/514	03/1330/16	0.10940089	0120033300	106231720	8697617070	7625036010	02626/3292	1461410806	3/836/7101	3048000002
MONTH	93-0	710		~ ~	•	8		36	Š	Š	3 4	? 5	2	g	2	2 -	- 0	٠,	? •	• 1	ត់

PORTFOLIO CONSTRUCTED UPON THE FOLLOWING DATA:

0.91 TURNOVER = TOTAL PURCHASE =

MAXIMUN STOCK HOLDING NSTAT NRETS

13) 14) 16) 116) 118) 118) 120) 121) 131)

29	PETROLEUM REFIN. & REL. PROD.	3.21 %
30	RUBBER AND MISC. PLAST. PROD.	2.70 %
32	STONE CLAY GLASS & CONC. PROD.	0.45 %
35	MACHINERY EXCEPT ELECTRICAL	2.09 %
	FIG AND FIG MACH	3.00 %
36	ELE. AND ELE. MACH,	
37	TRANSPORTATIONS EQUIPMENT	
38	MEAS. ANAL. & CONT. INST. ETC.	6.45 %
45	TRANSPORTATION BY AIR	3.21 %
48	COMMUNICATION	1.69 %
	ELECTRIC GAS AND SANIT. SERV.	17.31 %
49	FLECIKIC BAS AND SANTE SERVE	3.17 %
52	BUILDING MAT. HARD. GAR. SUPP.	
60	BANKING	1.56 %
61	CRED. AGEN. OTH. THAN BANKS.	2.83 %
65	REAL ESTATE	2.69 %
	HOLD. AND OTHER INV. COMP.	17.49 %
67		4 07 4
73	DOTINESS SENATORS	4.07 %
75	AUTO. REPAIR SERV. AND GAR.	1.19 %
80	HEALTH SERVICES	3.63 %
UU	TOTAL =	99.99 %
	IOIAL -	

Prior methods have required the calculation of a covarianc advantage of the current system. The covariance cells evaluated to standard definition and the cells in the matrix are filled. The calculations produce the following array:

## Covariance Matrix

χ	0162	0.0188	0.0525
X	0.0275	0.0525	0.0188
x1	0.0525	0.0275	0162
	×	x5	χ

The prior methodology calculates the partial derivative by partial derivative by partial derivative can be calculated for x2 at the current point following manner:

Partial(x2) = 2 \* (0.3\*0.0275 + 0.5\*0.0525 + 0.2\*0.0;

- 0.0765

The current system calculates the partial derivative by finc portfolio returns at the current weights for the 8 periods and the portfolio. The return in period(1)

Portfolio return(1) = 0.3\*0.8 + 0.5\*0.7 + 0.2\*0.4

79.0

The other returns for periods 2 though 7 are calculated for incidence. Then covariance between x2 and the portfolio is simply in the standard way. The result is the partial derivative of x2:

Covariance (portfolio, x2) = 0.0765

## EXAMPLE ILLUSTRATING DISTINCTIONS BETWEEN CURRENT SYSTEM AND PRIOR ART

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APPENDIX VI

To illustrate the current system's approach to solving an appropriate problem, a simple example is outlined to point out distinctions and improvements over prior art. The example problem objective function is to find the minimum variance portfolior relative to a standard financial target. The constraints are that the sum of the security weights must be 1.0 and the lower bound of 0.0 on each security. This example will illustrate the extraction of a search direction and outline the optimization process.

Beginning with a series of eight returns for three securities, x1, returns represent monthly total returns less the return on a standard financial target for each of the securities in this simple example.

## Net Security Returns After Subtracting Target Returns

였	4.7.20.00.00 4.7.20.00.00	X3	45
X	7.000.00 8.000.00 8.000.00	2	77 0
ᇽ	87.9.00000	Ħ	0.45
Period	<b>しこまれららてき</b>	Average	

This result is identically the same as extracting the partial derivative from the full covariance matrix. However, fewer calculations are required and less computer memory is needed to obtain the partial derivatives. Mathematically, the results prove to be exactly the same.

Once the partial derivatives have been extracted for each of the variables, it is a simple matter to search for a better solution using the partials to indicate a direction which improves the objective function. The simple process of letting the partial derivatives guide a search, recalculating the partials at the new solution, and searching again, leads quickly to an optimal solution. The search proceeds downhill until the objective function can no longer improve. This is the optimal solution.

In summary, the current system requires fewer calculations to determine an optimal point and therefore can solves problems in much less time. The current system also requires much less computer memory and therefore can solve much larger problem. By analyzing more securities at once, a better solution can be achieved.

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OUTPUT FROM PROGRAM

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NATIONAL INVESTMENT SERVICES SPANNING TECHNOLOGY SIMULATION RESULTS	EXAPMLE UPDATE WITH CONTROLLED TURNOVER	LIABILITY STREAM USED	START END SPAN NUMBER WGHT WGHT SENSIT SIC IDC TICK SECURITY NAME		AZH ATA	32 BALL BLL BAL 49 BGE BGE BAI 60 FBGI ONE BAI	BDG BDG BA BA BSE BSE	1.397 0.001 35 BGG BGG BKINGS.R SIKATION 1.276 00.000 67 CALH CAL CALFED INC 0.344 0.001 20 CKE CKE CASTE & COOKE IN	CHCS COMCAST CORP NASD CBU COMMODORE INTL LTD	0.181 0.002 51 COSV COST COST 1.486 0.003 51 DEK1 DKLB DEKA	2.015 0.002 60 FPA 2.628 0.001 61 FUN	3.294 0.001 27 GEN GTE GTE (3.000 0.001 67 HCP HCP HEAL	₹3,	3.002 0.001 20 K 3.000 0.002 65 KOG KOG 0.251 0.002 20 LNE LNCE	52 LCI 67 MTRV	MIDWEST ENERGY CO NATIONAL PRESTO INDS INC	25 OSM OMT OHIO MATTRESS	48 PACB PAC F	
Z		_	至	•		:	4												
YS CORP NASD INI	RLS CO BELL CORP		VASD INDI	7. 888 889	VCS INC 9.0049								×	×	EV	** **			2 88
RML RML RUSSELL CORP SMED SHOED SHARED MED SYS CORP MASD INI STE STATEMEN IND GAS & FLEE FOR	SARI LUV SOUTHWEST AIRLS CO SBCA SBC SOUTHWESTERN BELL CORP	TEUN TRC TEUDN RANCH CO	USHC U S HEALTHCARE INC NASD INDI UIL UNITED ILLUM CO USS UNITED STATES SURGICAL CORP	WGL WGL WASHINGTON GAS LT CO WPC WEC WISCONSIN ENERGY CORP SEFC SEED DEXALB GENETICS CORP	OKLB		MONTH LIA PORT DIF	DILLILES AND ASSELS PORTFOLIO	-0.005	STATISTICAL SUMMARY *******	BASED ON MONTHS 108 THROUGH 107	1000 ANNUAL 0.00 %	0.00000	0.00 × 0.00	MEAN STD DEV	0.00 x x 0.00 x x 0.00 x x x 0.00 x x x 0.00 x x x 0.00 x x x x	0.00	PARIMETERS FOR THIS RUN WERE:	UPDATE A.O.STEEL 12 5 88 TEMP.SFN VLIRAGOSTEEL.LIR NETYADSMOW RET

*** WEIGHTS *** SPAN SIC SYMBOL SECURITY OLD NEW DELTA SENSIT CODE IDC TICK NAME	**************************************		SECURITY NAME Thistophysical actions are a second and a second actions are a second actions as a second action action as a second action actio	*** INDUSTRY WEIGHTINGS ***		4
SECURITY NAME	<u>*</u>		SECURITY NAME		GHT	# ************************************
SYMBOL IDC TICK	KOG KOG MTRV MT	*** 113S ***	SYMBOL TDC TICK	•	WEIGHT	* * * * * * * * * * * * * * * * * * *
SIC 11 CODE	2.124 65 2.508 67	<u>S</u>	SIC II CODE	GHT INGS .		LIGNITE HIN. ON ON ON CTS CTS CTS CTS CTS CTS CTS CTS CTS CTS
*** SPAN			TA SENSIT	STRY WEI	INDUSTRY	ULTURAL PRODUCTION-CR INOUS COAL & LIGNITE GAS EXTRACTION FROMED PRODUCTS A DIH. FIM. PROD. MFF TURE AND FIXTURES A DIH. FIM. B REL. PR ELM REFIN. & REL. PR CLAY GIASS & CONC. P R. ANCH. PRODIEST PR CLAY GIASS & CONC. P REV EXCEPT ELECTRICA AND ELE. MACH. PORTATION EQUIPMENT ANAL. & CONT. INST. MICATION BY AIR ILCATION BY AIR AUCATION BY AIR SEGULATION OF THE TRADE-NONDIR. GO SALE TRADE-NONDIR. GO SERVICES.
WEIGHTS *** NEW DELTA	3.000 0.15 2.944 0.26		WEIGHTS *** NEW DELTA	NON!		AGRICULTURAL PRODUCTION-CROPS FORESTRY BITUMINOUS COAL & LIGNITE MIN. OIL & AGS EXTRACTION FOOD KINDRED PRODUCTS APP. & OTH. FIM. PROD. MFFAOSM FURNITURE AND FIXTURES PRINTING PUBLISHING AND. PETROLEUM REFIN. & REL. PROD. STONE CLAY GLASS. & CONC. PROD. RAUBER AND MISC. PLAST. PROD. STONE CLAY GLASS. & CONC. PROD. MACHINERY EXCEPT ELECTRICAL TRANSPORTATIONS EQUIPMENT MEAS. ANAL. & CONT. INST. ETC. TRANSPORTATION BY AIR COMMINICATION ELECTRIC GAS AND SANIT. SERV. MHOLESALE TRADE-NOWDUR. GOODS BUILDING MAT. HARD. GAR. SUPP. GRED. AGEN. OTH. THAN BANKS. REAL ESTATE HOLD. AND OTHER INV. COMP.
OLD OLD	2.680		QTO		2002	

PORTFCLIO CONSTRUCTED UPON THE FOLLOWING DATA:

84 -0. 0049200002-0. 0091439467-0. 0042239465 85 0.0073779998 0.0500006266 0.042626258 86 0.0044139999 0.029062852 0.022487853 87 -0.0369299985-0.0087748254 0.0281531741 88 -0.0717199966-0. 0408916809 0. 0309283158 99 0.0247970000 0.0432149470 0.0188179470 91 0.0405899994-0. 0030535768 0.0312264226 92 0.0243800003 0.0198711567 0.0442511589 93 0.057399994-0. 0309353768 0.0312264226 94 0.00689500002-0.1454212815-0.2423172891 95 0.0174770007 0.0385430-0.0123335430 95 0.0179789998 0.024398554 0.006414564 100 0.022400001-0.0108487122 0.0188912880 100 0.0256100015-0.0064554564 0.0460145661 100 0.025400001-0.0108487122 0.0188912880 103 0.0376109998 0.050945352-0.0066162646 104 0.00134309999 0.0099289045 0.0213689044 105 0.0356100015-0.0019915070 0.0144688996 106 0.0231340000-0.0009915070 0.0003484893 106 0.0231340000-0.010998100 0.014688996 VARIANCE AT VARIANCE AT

#### WHAT IS CLAIMED IS:

- 1. A method of correlating a future asset return of a portfolio to future financial liabilities variable over time, comprising the steps of:
- (a) determining future payments needed over time to fulfill said future financial liabilities;
- (b) selecting a standard index having a standard asset return over time for meeting said future payments; and
- (c) analyzing a plurality of assets for identifying selected ones of said assets for providing optimum correlation of the future return of said selected assets to said standard asset return, said optimum correlation achieved by calculating a minimum standard deviation for the difference between the future returns of said plurality of selected assets and said standard asset return, ranking said selected assets from smallest to largest covariance, making an iterative change in weights of said selected assets, reordering the rank of said selected assets and continuing said iterative weight and rank change of said selected assets until the covariance converges to an optimal solution,
- 2. The method as defined in Claim 1 wherein said future financial liabilities comprises a pension plan.

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3. The method as defined in Claim 1 wherein said plurality of assets exhibit sensitivity to the same parameter as said future financial liabilities for which said time dependent optimum correlation is determined.

4. A system for correlating a future asset return of a portfolio to future financial liabilities variable over time, comprising:

means for determining future payments needed over time to fulfill said future financial liabilities;

means for selecting a standard having a standard asset return over time to meet said future payments; and

means for analyzing a plurality of assets for identifying selected ones of said assets for providing optimum correlation of the future return of said selected assets to said standard asset return, said optimum correlation achieved by means for calculating a minimum standard deviation for the difference between the future returns of said plurality of assets and said selected standard asset return, said calculating means further ranking said selected assets from smallest to largest covariance, making an iterative change in weights of said selected assets, reordering the rank of said selected assets and continuing said iterative weight and rank change of said selected assets until the covariance converges.

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- 5. The system as defined in Claim 4 wherein said future financial liabilities comprise insurance liabilities and pension plan liabilities.
- 6. The method as defined in Claim 4 wherein a computer performs the functional operations.

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PREPARE INPUT: CREATE FILES WHICH CONTAIN RETURN INFORMATION ON THE SECURITIES TO BE USED, THE TARGET RETURNS, SECURITY IDENTIFIERS, CURRENT PRICE, MARKET CAPITALIZATION AND CURRENT PORTFOLIO WEIGHTS. "ESTABLISH STATISTICAL PROPERTIES OF LIABILITIES."

SET UP PROBLEM: SPECIFY NUMBER AND TYPE OF SECURITIES, TIME PERIOD, NUMBER OF RETURNS USED TO CALCULATE COVARIANCE AND TO CALCULATE AVERAGES, DISTANCE TO MOVE UP AND DOWN COVARIANCE BULLET, SCALING FACTOR FOR TARGET, AND FACTOR FOR CONTROLLING TURNOVER.

READ IN NECESSARY INFORMATION: SECURITY NAMES, IDENTIFIERS, INDUSTRY CODES, PRICES, MARKET CAPITALIZATION, WEIGHT IN CURRENT PORTFOLIO, PERIOD RETURNS; TARGET NAMES, TARGET PERIOD RETURNS.

CALCULATE SPANNING COVARIANCE ARRAY: DEFINED AS THE COVARIANCE OF SECURITY RETURN LESS TARGET RETURN WITH ALL OTHER SECURITIES RETURNS LESS TARGET RETURNS IN SPECIFIED RETURN PERIOD.

CALCULATE AVERAGE RETURN FOR EACH SECURITY.

SET UP CONSTRAINTS ON SECURITY TYPE, SECTOR TYPE, INDIVIDUAL SECURITY WEIGHTS.

FORMAT PROBLEM IN STANDARD FORM FOR SOLUTION BY GENERALIZED QUADRATIC PROGRAMMING TECHNIQUE.

SOLVE FOR OPTIMUM OF PROBLEM WITH QUADRATIC PROGRAMMING SOLUTION ALGORITHM. CHECK SOLUTION FOR FEASIBILITY.

CALCULATE STATISTICS: COVARIANCE OF PORTFOLIO, ALPHA, BETA, AND STANDARD ERROR WITH TARGET IN SIMULATION PERIOD; PORTFOLIO RETURNS ON RETURN PERIOD, PORTFOLIO RETURNS IN SIMULATION PERIOD, TURNOVER, SECTOR WEIGHTS, AND SECURITY TYPE WEIGHTS.

PRINT OUTPUT FILE: SECURITY WEIGHTS, SENSITIVITIES, IDENTIFIERS. AND NAMES: STATISTICS, INPUT PARAMETERS, SORTED BUYS AND SELLS, AND SECTOR WEIGHTS.

Fig. 1a

PREPARE INPUT: CREATE FILES WHICH CONTAIN RETURN INFORMATION ON THE SECURITIES TO BE USED, THE TARGET RETURNS SECURITY IDENTIFIERS, CURRENT PRICE, MARKET CAPITALIZATION AND CURRENT PORTFOLIO WEIGHTS. "ESTABLISH STATISTICAL PROPERTIES OF LIABILITIES."

SET UP PROBLEM: SPECIFY NUMBER AND TYPE OF SECURITIES, TIME PERIOD, NUMBER OF RETURNS USED TO CALCULATE COVARIANCE AND TO CALCULATE AVERAGES, DISTANCE TO MOVE UP AND DOWN COVARIANCE BULLET, SCALING FACTOR FOR TARGET, AND FACTOR FOR CONTROLLING TURNOVER.

READ IN NECESSARY INFORMATION: SECURITY NAMES, IDENTIFIERS, INDUSTRY CODES, PRICES, MARKET CAPITALIZATION, WEIGHT IN CURRENT PORTFOLIO, PERIOD RETURNS; TARGET NAME, TARGET PERIOD RETURNS.

DEFINE VARIANCE AS SUM OF SQUARED DIFFERENCES BETWEEN PORTFOLIO RETURNS AND TARGET.

GENERATE RETURN SERIES FOR TARGET IN TERMS OF ALL ASSETS IN PORTFOLIO.

GENERATE CONSTRAINTS AS SECURITY TYPE, SECTOR TYPE, INDIVIDUAL SECURITY WEIGHTS.

CALCULATE EACH ASSETS' COVARIANCE WITH SELECTED FINANCIAL TARGET.

RANK THE COVARIANCES FOR ALL POTENTIAL ASSETS OF THE PORTFOLIO.

PROCEED FROM FIRST RANKED ASSET TO END, FILLING IN WEIGHT UNTIL A CONSTRAINT IS REACHED, REQUESTING FOR EACH ASSET STEPWISE DOWN THE RANKING.

GENERATE RETURN FOR THE WEIGHTED PORTFOLIO OF ASSETS.

CALCULATE PARTIAL DERIVATIVE FOR EACH ASSET OF THE SELECTED PORTFOLIO WITH REQUEST TO THE TARGET FINANCIAL INDEX.

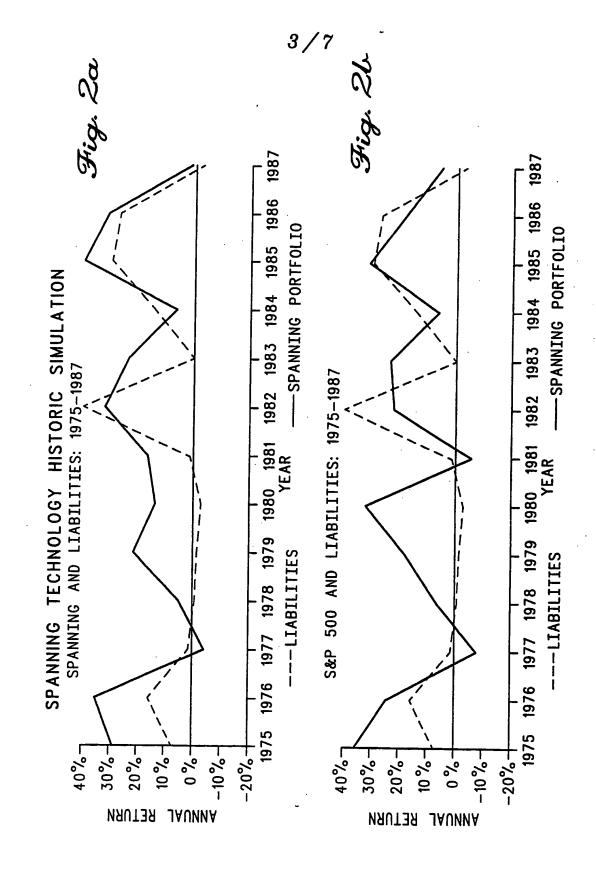
REORDER ALL ASSETS IN ORDER OF COVARIANCE AND MAKE ITERATIVE CHANGE IN WEIGHTS OF ASSETS TO IMPROVE OVERALL COVARIANCE.

REPEAT ITERATIVE IMPROVEMENT OF COVARIANCE BY SELECTED, ALLOWABLE CHANGES IN ASSET WEIGHTS UNTIL CONVERGES.

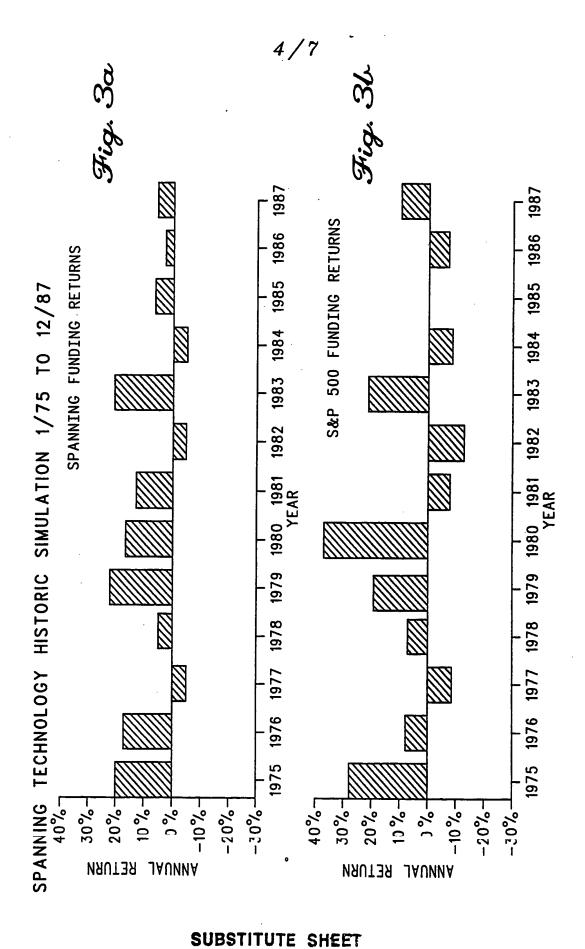
Fig. 16

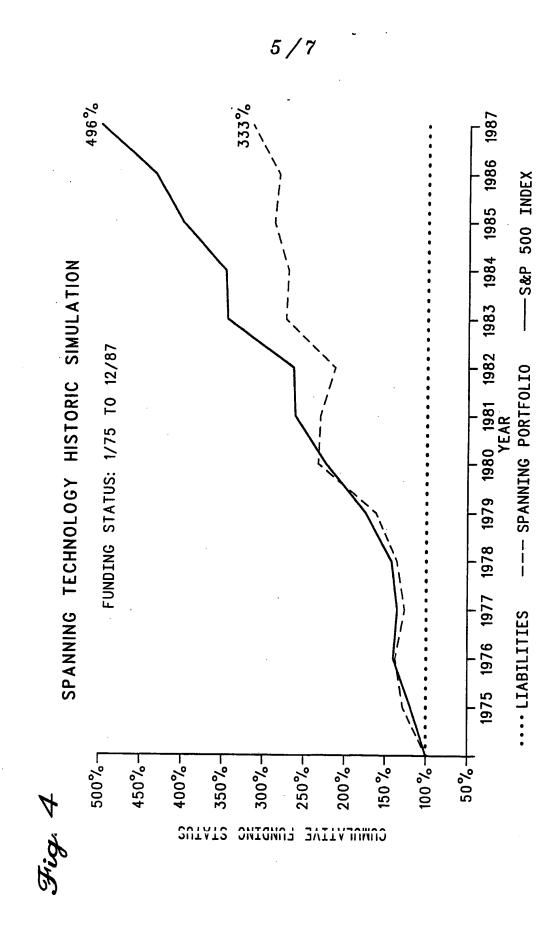
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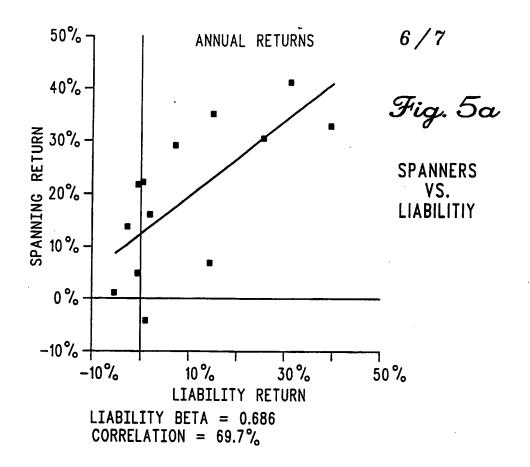


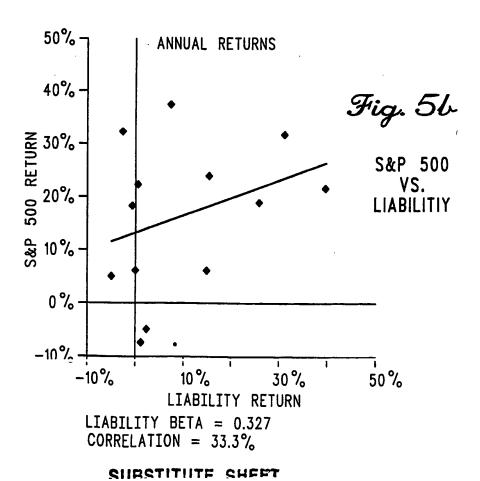
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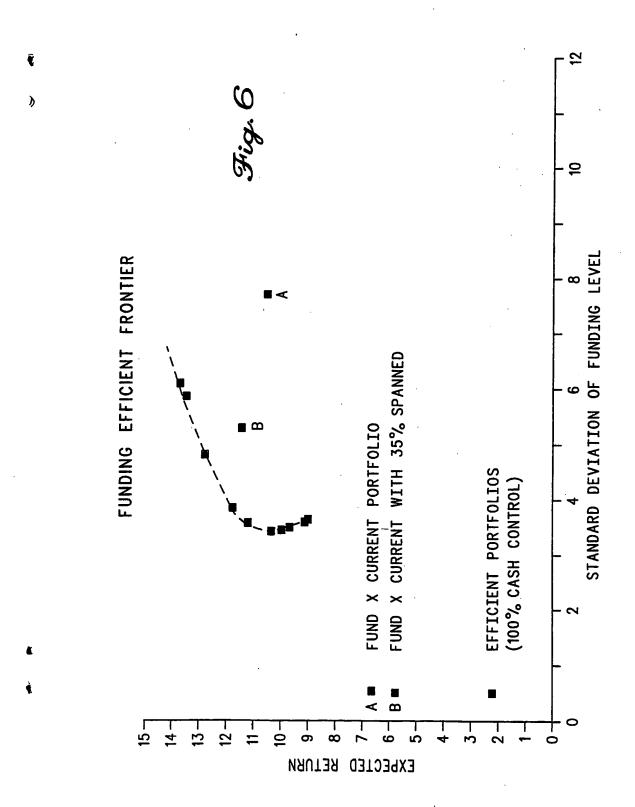
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### INTERNATIONAL SEARCH REPORT

International Application No PCT/US90/04328

I. CLASSIFICATION OF SUBJECT MATTER (if several classification symbols apply, indicate all)										
According to International Patent Classification (IPC) or to both National Classification and IPC IPC(5): GO6F 15/21 US CL.: 364/401, 408										
II. FIELDS	BEARCHED									
	Minimum Docume	intation Searched +								
Clausification	n System 1	Classification Symbols								
US 364/401, 408										
	Documentation Searched other than Minimum Documentation to the Extent that such Documents are Included in the Fields Searched 6									
III. DOCU	MENTS CONSIDERED TO BE RELEVANT 14									
Category •	Citation of Document, 14 with indication, where app	propriate, of the relevant passages 12	Relevant to Claim No. 14							
A	US, A, 4,642,768 (ROBERTS) 10	February 1987	1-6							
A	US, A, 4,648,038 (ROBERTS et a	al.) 03 Marhc 1987	1-6							
A	US, A, 4,722,055 (ROBERTS) 26	January 1988	1-6							
A	US, A, 4,739,478 (ROBERTS et a	al.) 19 April 1988	1-6							
A	US, A, 4,750,121 (HALLEY et al	1.) 07 June 1988	1-6							
A	US, A, 4,752,877 (ROBERTS et a	al.) 21 June 1988	1-6							
A	US, A, 4,839,804 (ROBERTS et a	11.) 13 June 1989	1-6							
A,P	US, A, 4,933,842 (DURBIN et al	l.) 12 June 1990	1-6							
A	Haugen, "Modern Investment The by Prentice-Hall (New Jersey),	eory" published 1985 Chapters 6-8.	1-6							
* Special categories of cited documents: 16 "T" later document outsilahed after the international filling date										
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IV. CERTIFICATION										
Date of the Actual Completion of the International Search 3 Date of Mailing of this International Search Report 7										
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